

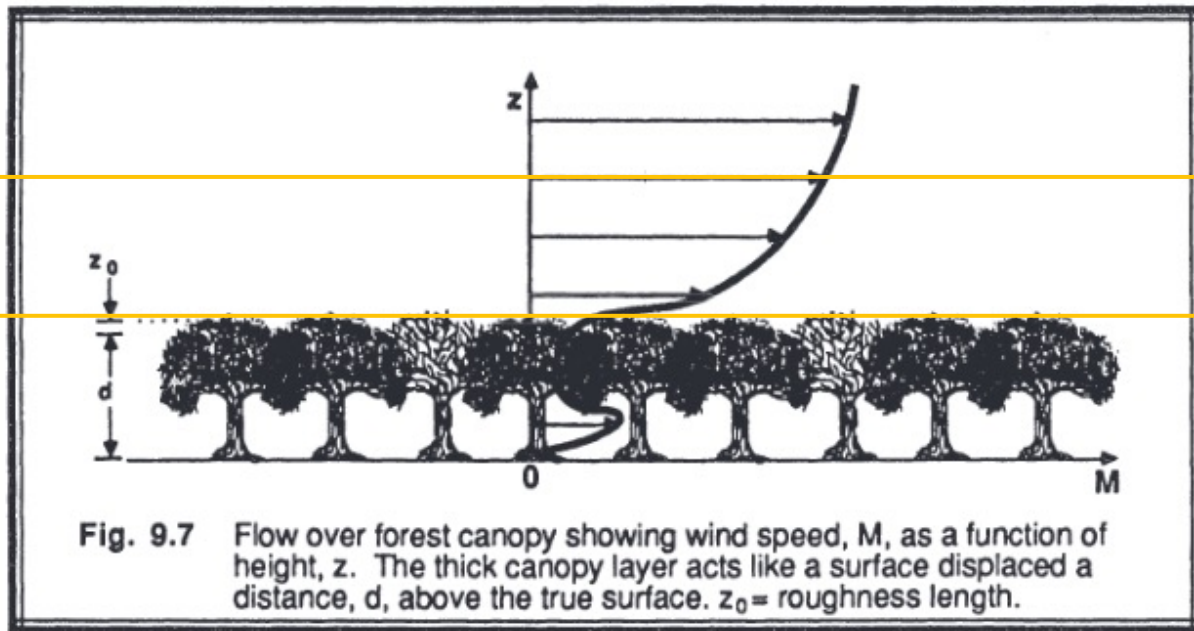


Facing heterogeneities with increasing resolution

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Feb 7, DWD offenbach

Universal log-law



$k = 1$

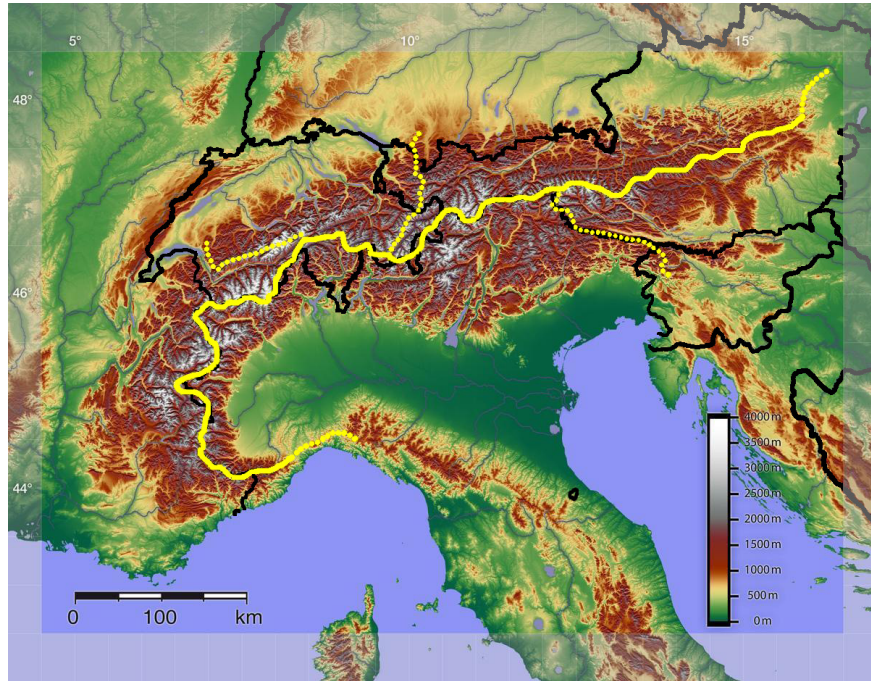
$k = 0$

$U = 0$

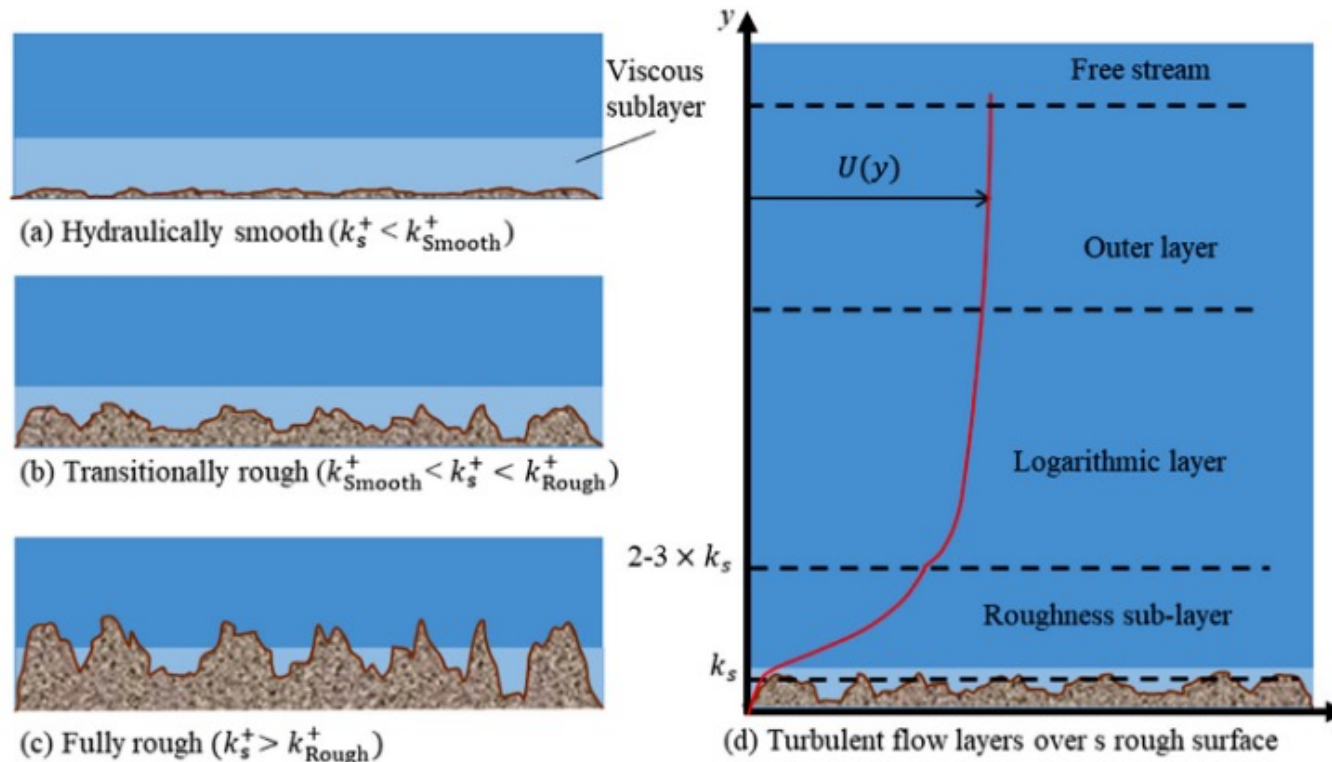
$$U_1 = U_0 + \left(\frac{u^*}{k}\right) \ln \frac{(z - d)}{z_0}$$

Works well when the surface underneath is smooth or, in other words the flow is **locally homogeneous**

But the world where we live



... has rough surfaces



- homogeneous (isotropic) turbulence
- Universal log law
- also called Inertial Sub Layer

- heterogeneous turbulence???
- Profile depends on the underlying roughness

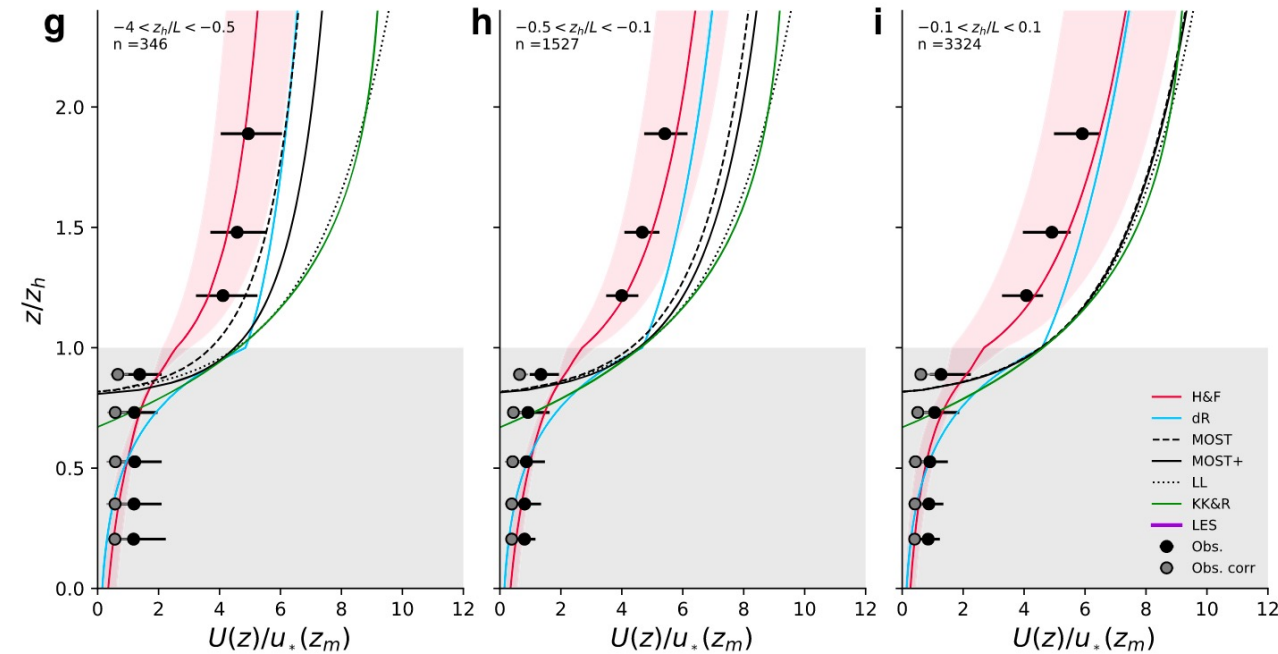
Attempts to extend log-law in RSL over Forest canopies

Table 2 Methods used to calculate profiles for wind speed, with abbreviation (Abr.) used in the text

Abr.	Name	Equation(s)	Assumptions
LL	Neutral logarithmic law	$u(z) = \frac{u_*}{\kappa} \ln\left(\frac{z-z_d}{z_0}\right)$ (7)	z_0 and z_d use Macdonald et al. (1998)
KK&R	Kastner-Klein and Rotach (2004)	$u(z) = \frac{u_*}{0.6\kappa} \left[1 - 0.6 \ln(0.12) - \exp\left[0.6 - 0.072\left(\frac{z-z_d}{z_0}\right)\right] \right]$ (8)	As LL
MOST	Monin-Obukhov similarity theory	$u(z) = \frac{u_*}{\kappa} \left[\ln\left(\frac{z-z_d}{z_0}\right) - \psi_M\left(\frac{z-z_d}{L}\right) + \psi_M\left(\frac{z_0}{L}\right) \right]$ (9)	As LL, stability functions following Garratt (1992)
MOST+	MOST with stability dependent z_0	Equation (9) with $z_0 = z_{0mac} \cdot \exp\left[-\psi_M\left(\frac{z_h-z_d}{L}\right)\right]$, where the aerodynamic roughness length z_{0mac} calculated following Macdonald et al. (1998)	As MOST, with stability dependent aerodynamic roughness length, constant z_d
dR	De Ridder (2010)	Empirical expression for Eq. (5) $\hat{\psi}_M(z) = \phi_M \left[\left(1 + \frac{\nu}{\mu_M} \frac{z-z_d}{z_*} \right)^{\frac{z-z_d}{L}} \right]^{\frac{1}{\lambda}} \ln \left(1 + \frac{\lambda}{\mu_M} \frac{z-z_d}{z_*} \right) e^{-\mu_M \frac{z-z_d}{z_*}}$, (11) with $z_0 = z_{0mac} \cdot \exp\left[-\psi_M\left(\frac{z_h-z_d}{L}\right) + \hat{\psi}_M(z = z_h)\right]$, λ , μ_M , and ν are assumed to be constants. Forest RSL values: $\lambda = 1.5$, $\mu_M = 2.59$, and $\nu = 0.5$. In the canopy: $u(z < z_h) = u(z = z_h) \exp\left[a\left(\frac{z}{z_h} - 1\right)\right]$ (Macdonald 2000)	As MOST+, assuming $z_* = z_m$ corresponding to the highest measurement height

They all take $\langle u \rangle = f(z)$

Seem to work well over urban canopies as well.



Gothenburg Tower, Sweden

Is it fair to assume that $\langle u \rangle = f(z)$ in RSL for modelling purposes?

Zurich city



Inn valley



Local homogeneity

- Implies that the **mean** quantities are invariant to changes in **x**
- Very powerful assumption
- Demonstrated to exist over smooth surface (Garraat 1992; Schlichting 1960)

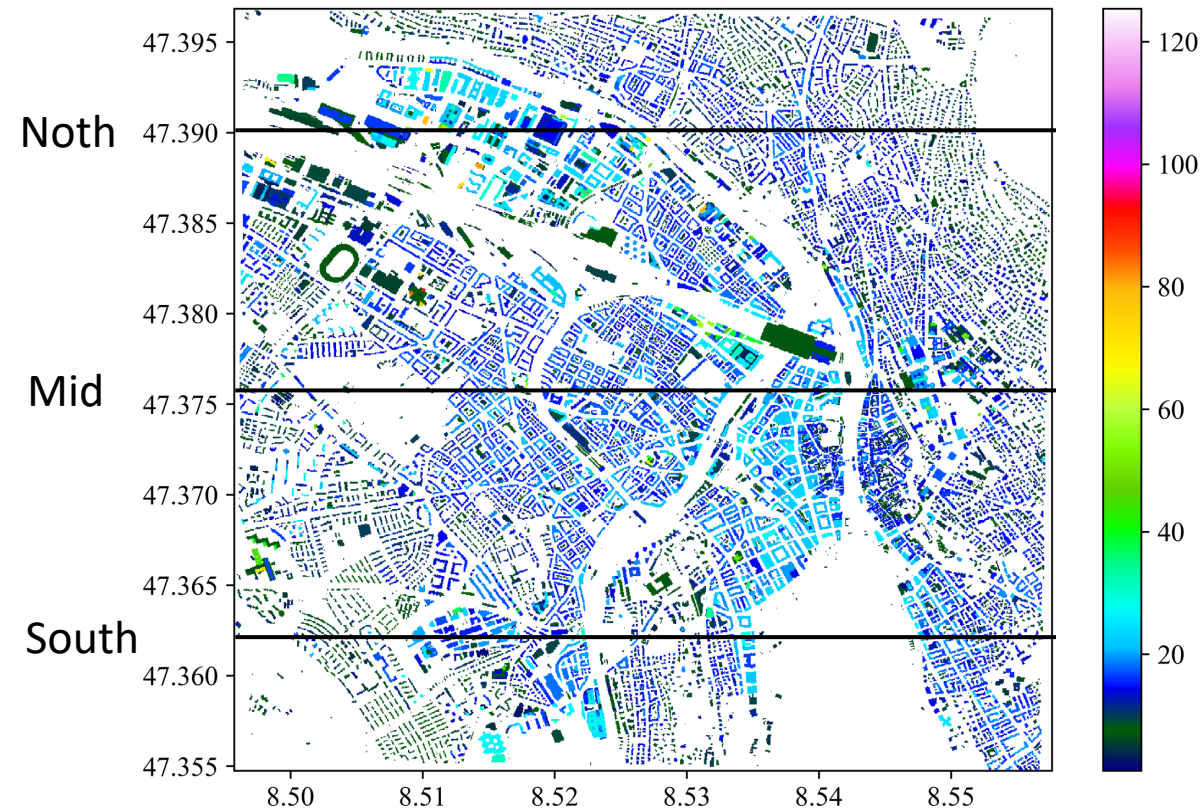
- Unclear about RSL....that too at $O(100\text{m})!$
- Moreover, literature rather vague about **mean**.

$$\langle u(\mathbf{x}, z) \rangle = \langle u(z) \rangle = F(z)$$

Therefore the question

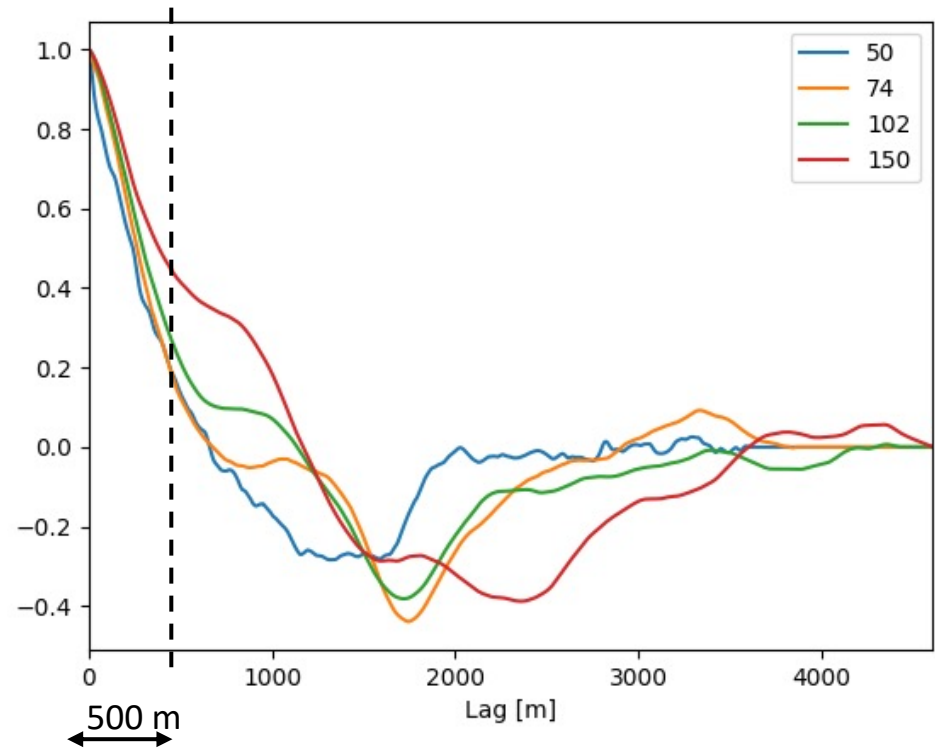
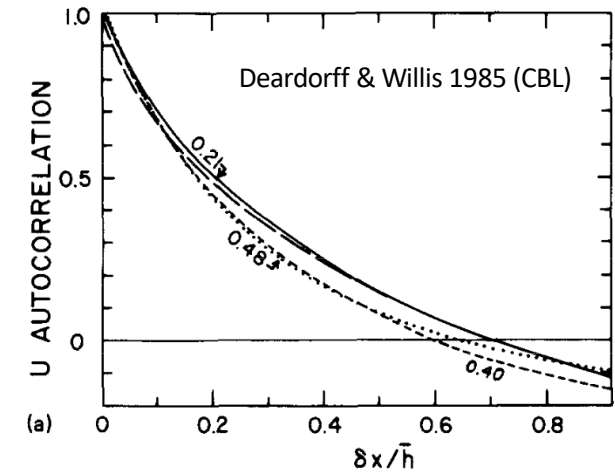
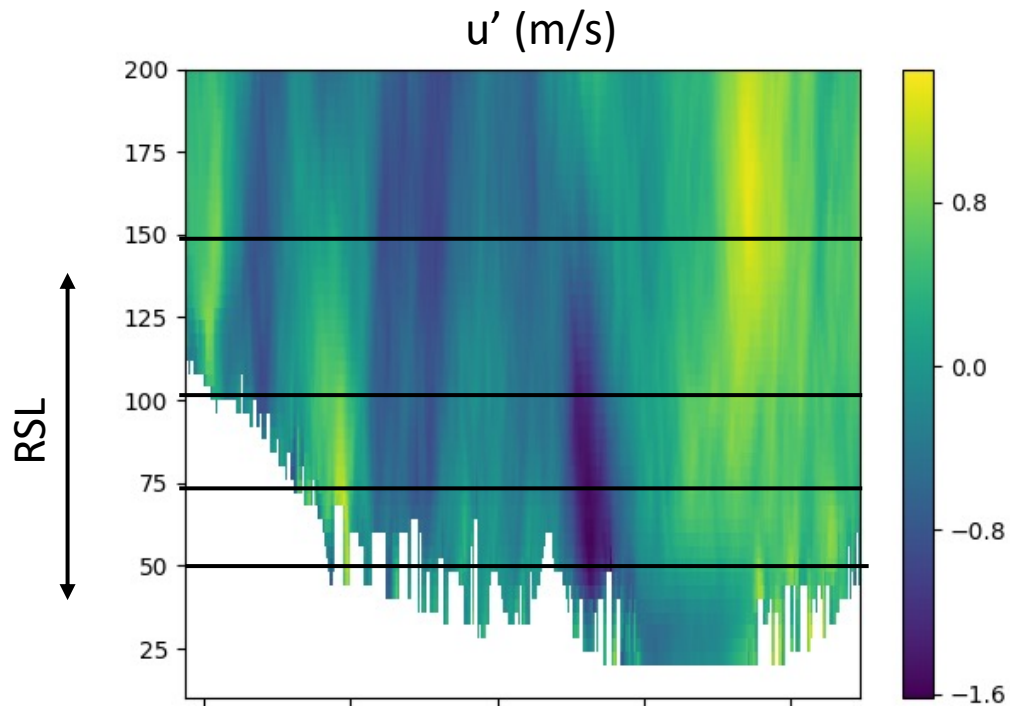
What is the scale of homogeneity (or heterogeneity) over rough surfaces?

Building resolving simulations using PALM

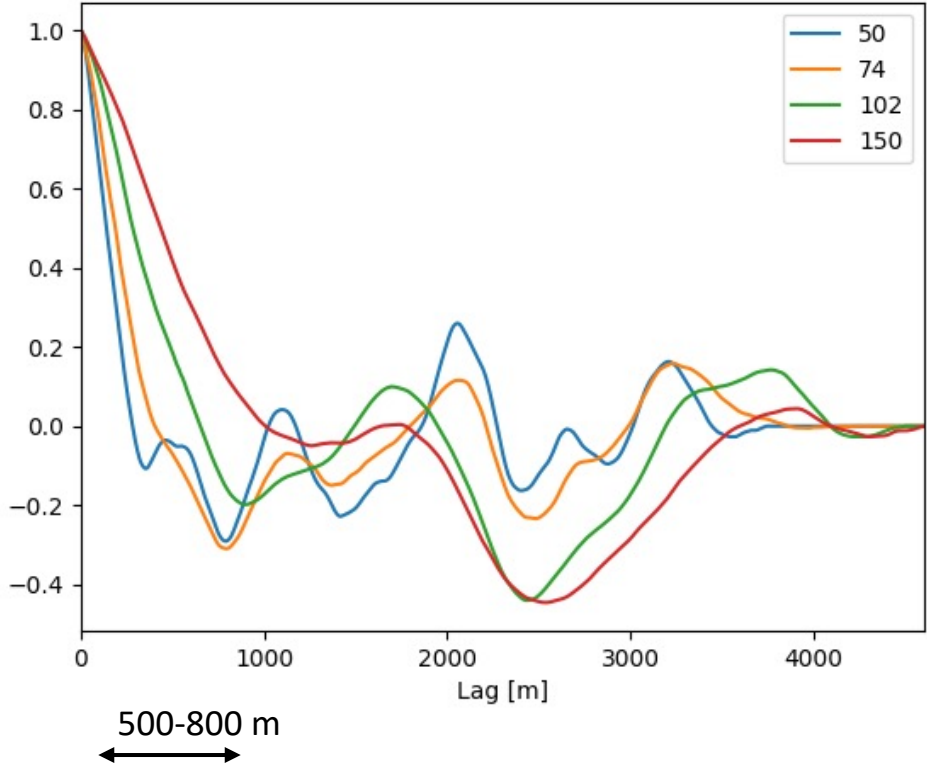
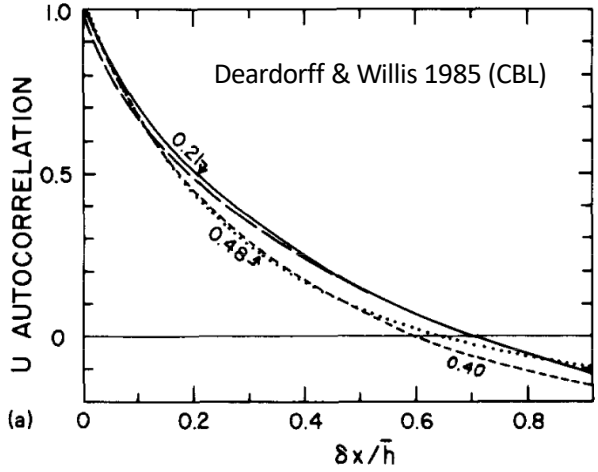
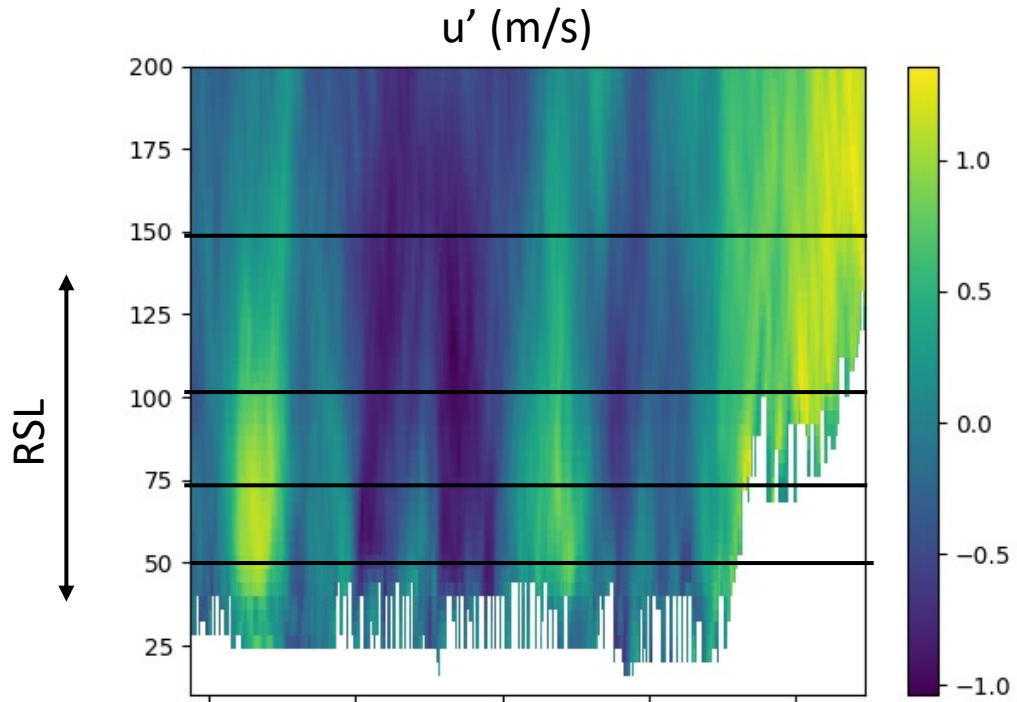


- Calm and clear sky conditions
- $dx = dy = dz = 4m$
- Adaptive time step $\sim 0.5s$
- Nested simulation $64m \rightarrow 32m \rightarrow 4m$. Using results from the innermost domain.
- 30 min averaged. No spatial averaging.

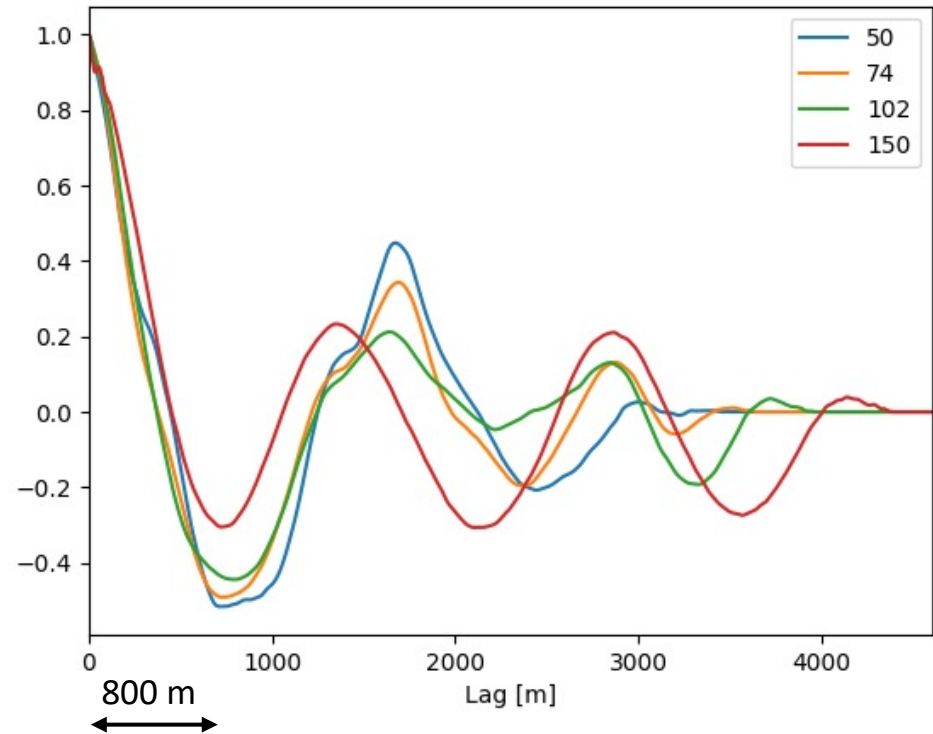
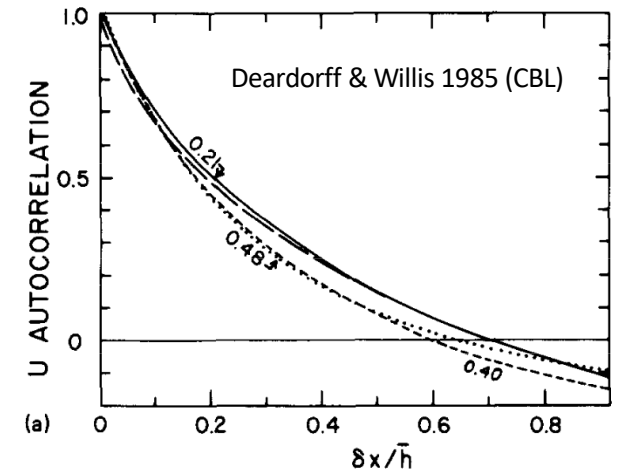
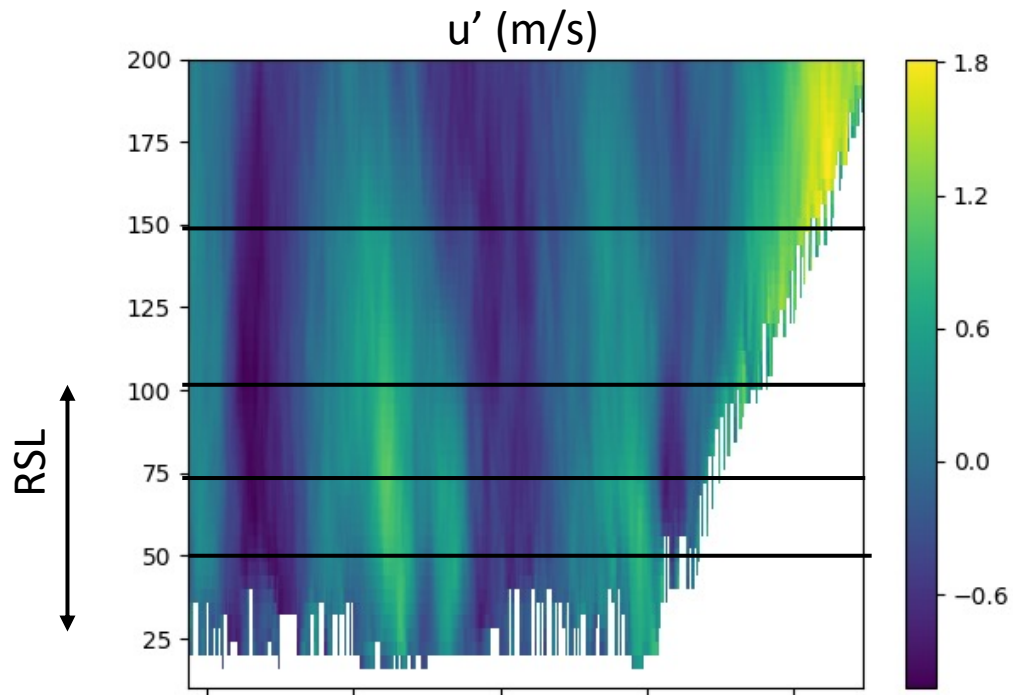
u autocorrelation (south)



u autocorrelation (middle)



u autocorrelation (north)

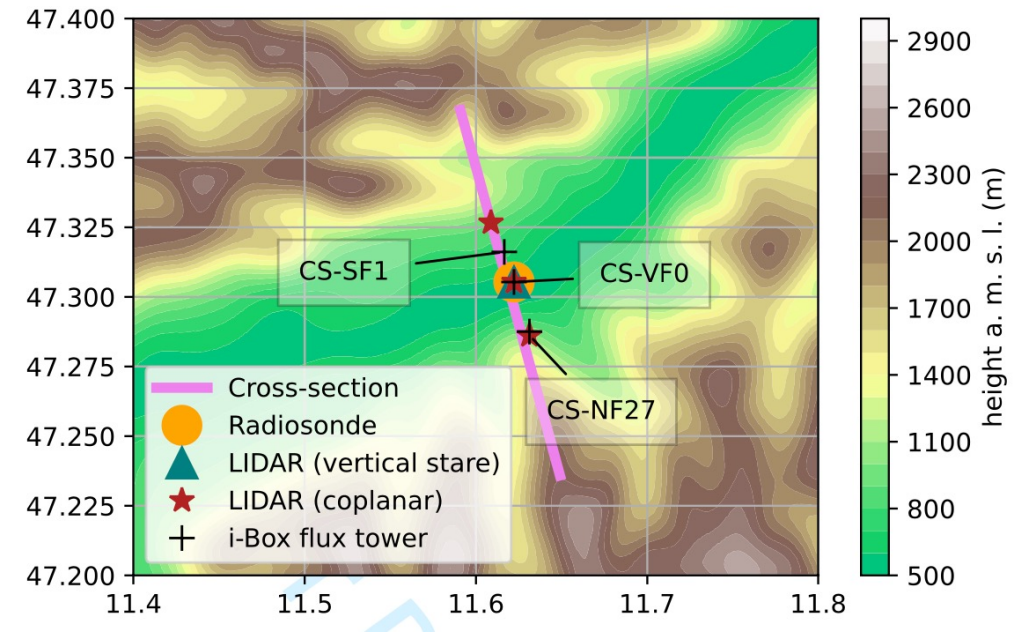


Observations so far...

- $\langle u \rangle$ seem uncorrelated to itself over scales of 500-800 m
- Implies that the subgrid flow can be regarded homogeneous over grid spacings of 500-800 m within the RSL over Zürich city
- Provided that $\langle \rangle = 30$ min averaging
 - It means, at $\Delta x = 500\text{m}$ and $dt = 5\text{s}$ averaging u over 360 time steps. Not reasonable!
- Need to investigate for shorter time averaging windows

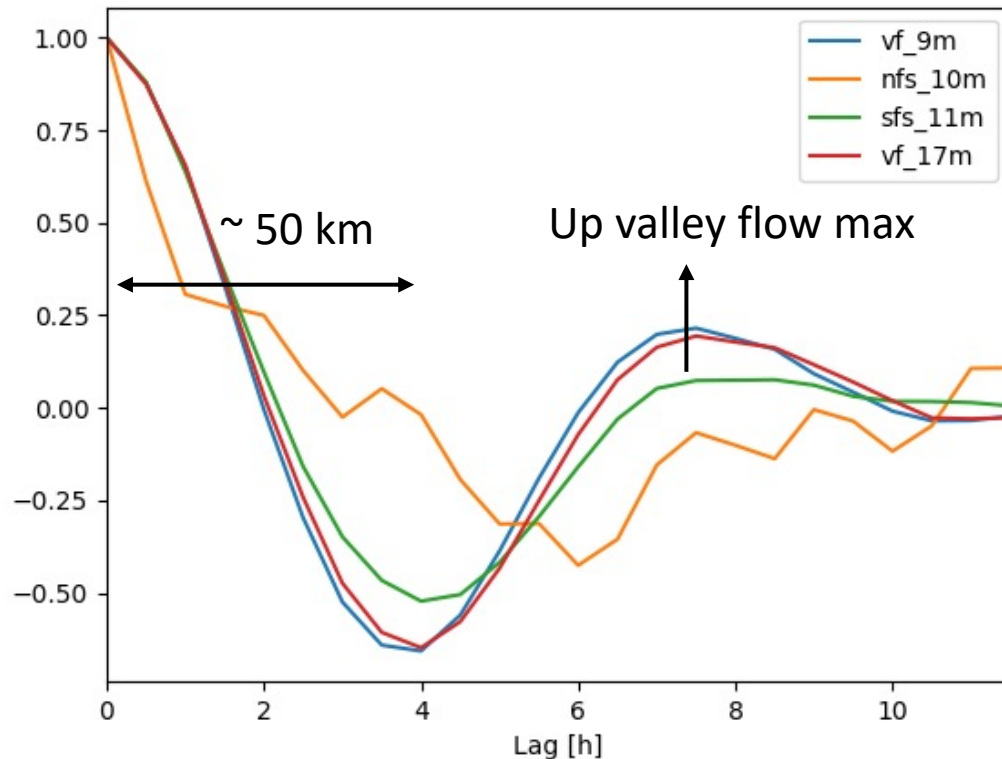
Let's switch the scale

i-Box flux tower (Innsbruck, Austria)



Over the mountains, I always thought that log-law would hold at 100m!

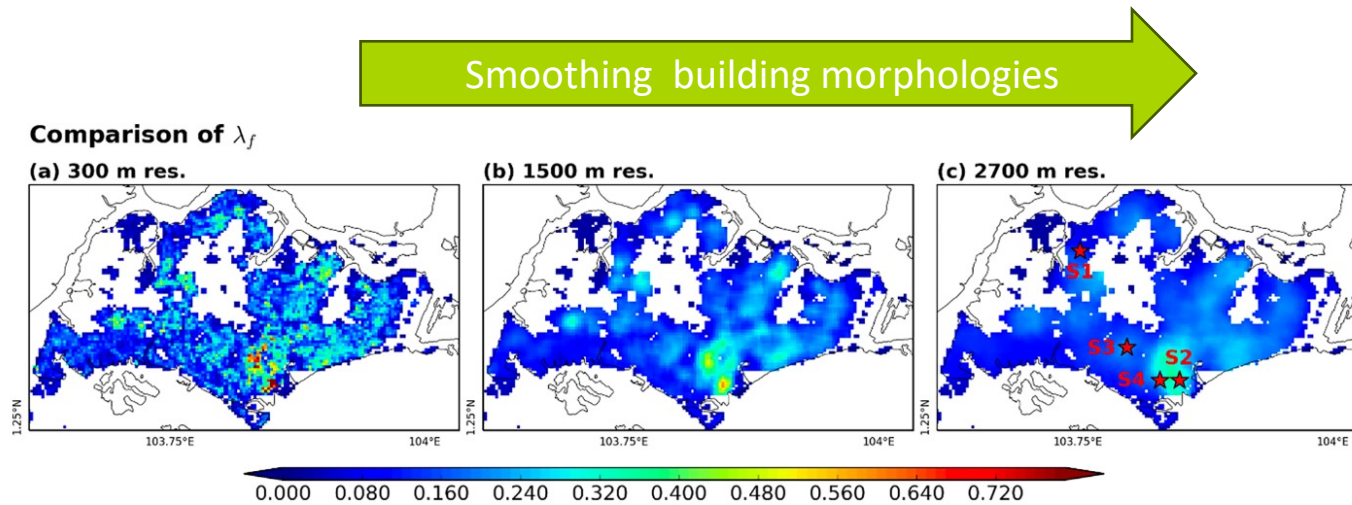
u autocorrelation



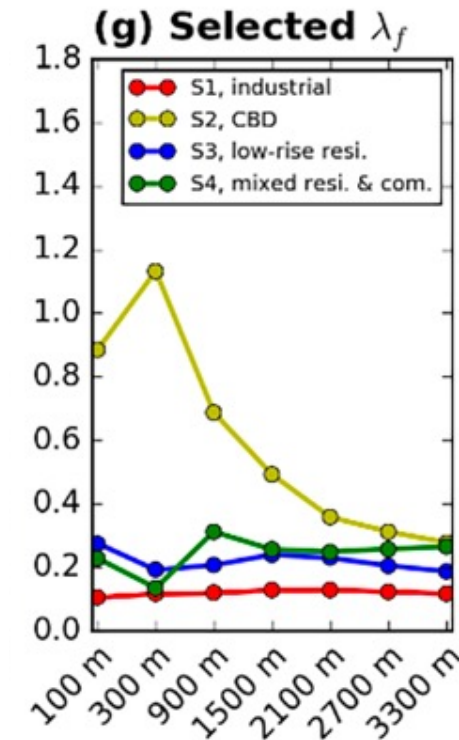
- Time series on 13 sept 2019 from 8-18h
- On 4 locations.
- 30 min averaged samples

-Same observation that local homogeneity seem valid for 30 min averages
- Questionable for higher resolution (dt = 1 s) samples!

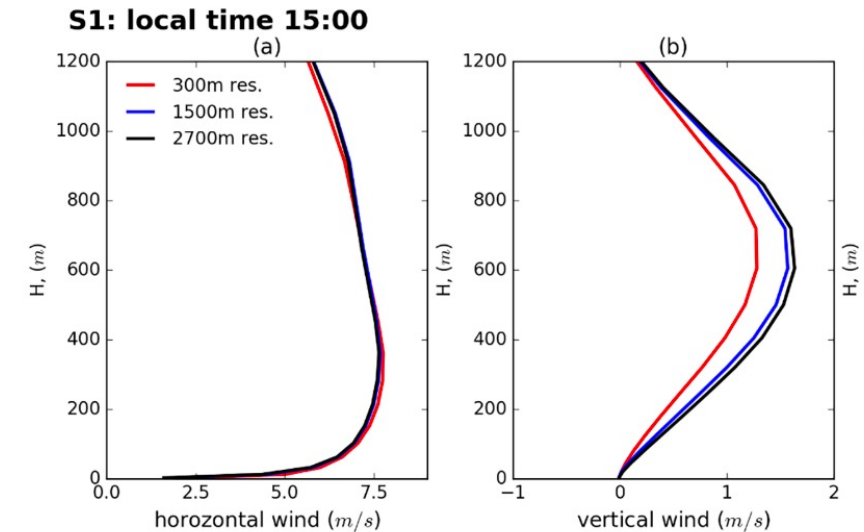
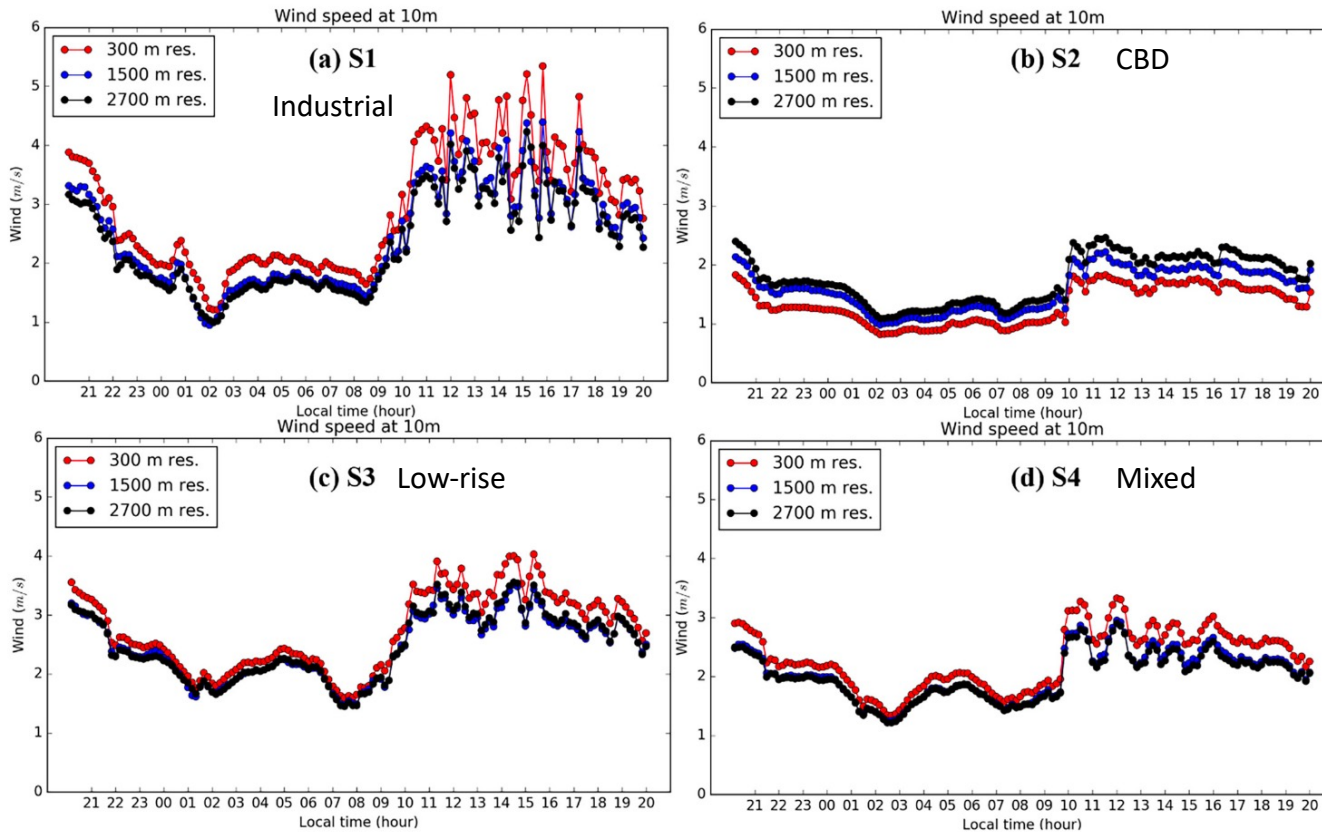
That said, no one stopping us from doing the simulation



heterogeneity disappears for $\Delta x > 2$ km thereby more suitable to assume local homogeneity



so what happens when comparing with the runs where local homogeneity is likely not valid?



- Differences are significant. Gives a motivation to work towards a better surface treatment at O(100m).
- See Jacopo's proposal next

Thank you!

