

# LPI (Lightning Potential Index) derived from COSMO-DE fields

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- Yair et al. (JGR, 2010), Lynn and Yair (Adv. Geosci., 2010)
- Charge separation in thunderstorms is correlated with the simultaneous presence of updrafts, supercooled liquid water, graupel and other frozen hydrometeor types („cloud ice“, „snow“)
- This concept was modeled by the authors within the LPI-Index. In some details **the original literature is unclear. My interpretation is:**

$$\text{LPI} = f_1 f_2 \frac{1}{H_{-20^\circ\text{C}} - H_{0^\circ\text{C}}} \int_{H_{0^\circ\text{C}}}^{H_{-20^\circ\text{C}}} \epsilon w^2 g(w) dz$$

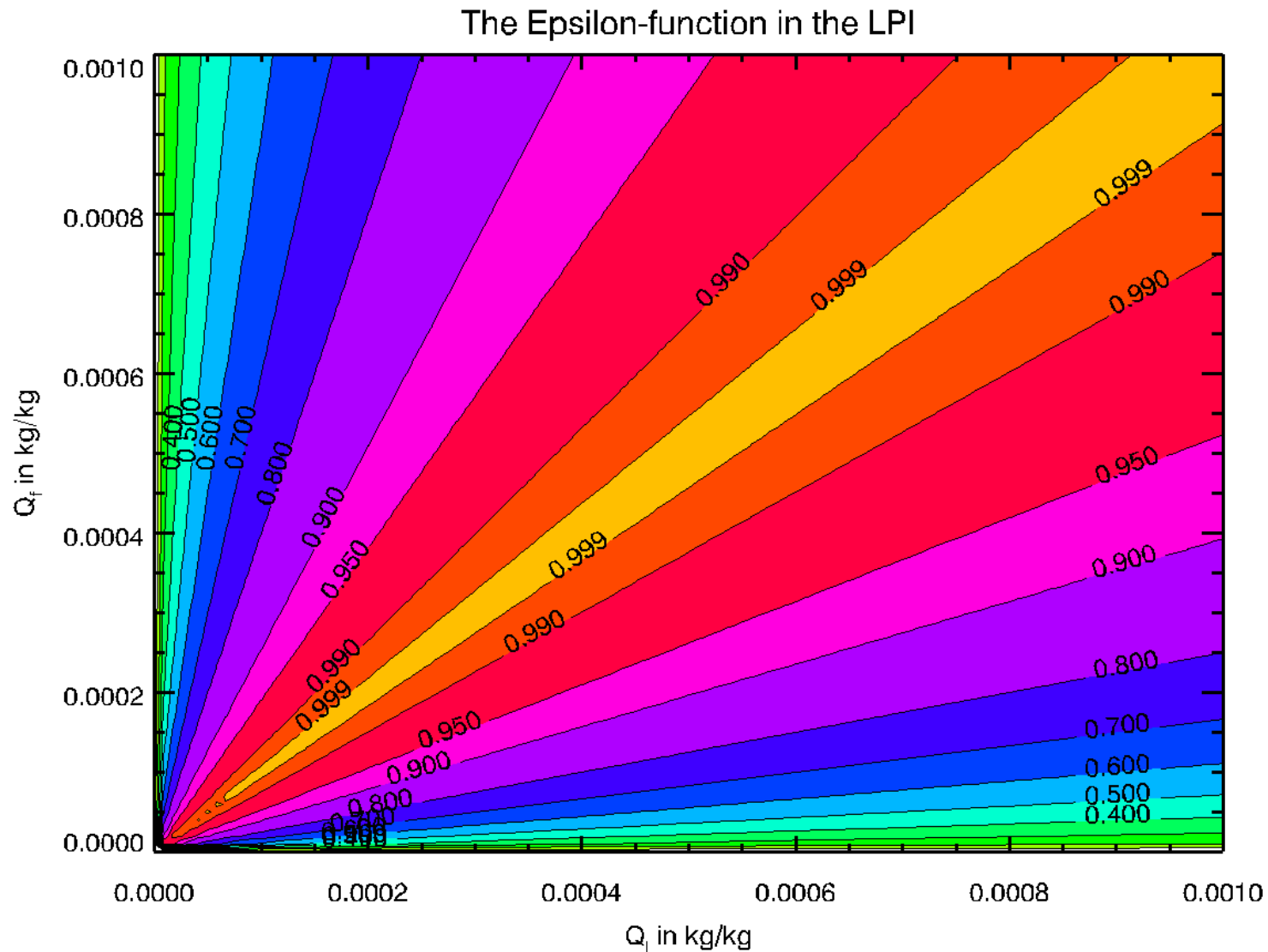
$$\epsilon = \frac{2 \sqrt{q_L q_F}}{q_L + q_F}$$

$$q_L = q_c + q_r$$

$$q_F = \frac{q_g}{2} \left[ \frac{2 \sqrt{q_i q_g}}{q_i + q_g} + \frac{2 \sqrt{q_s q_g}}{q_s + q_g} \right]$$

$f_1$ ,  $f_2$  and  $g(w)$  see  
next-next slide!

## → Function $\varepsilon$ :



# Concept of the LPI: $f_1$ , $f_2$ and $g(w)$

→ Filter functions  $f_1$ ,  $f_2$  and  $g$ :

$$\text{LPI} = f_1 f_2 \frac{1}{H_{-20^\circ\text{C}} - H_{0^\circ\text{C}}} \int_{H_{0^\circ\text{C}}}^{H_{-20^\circ\text{C}}} \epsilon w^2 g(w) dz$$

$$f_1 = \begin{cases} 1 & a \geq 0.5 \\ 0 & \text{sonst} \end{cases}$$

$$a = \frac{\iint \begin{cases} 1 & \max[w(z)] \geq w_{\max,0} \\ 0 & \text{else} \end{cases} dx dy}{\iint dx dy}$$

$$f_2 = \begin{cases} 1 & B_{ML} \geq B_0 \\ 0 & \text{sonst} \end{cases}$$

$$B_{ML} = \frac{\iint \int_{p_s-50\text{hPa}}^{p_s-550\text{hPa}} R_d (T_{v,\text{parcel}} - T_{v,u}) d \ln p dx dy}{\iint dx dy}$$

$$g = \begin{cases} 1 & w \geq 0.5 \text{ m s}^{-1} \\ 0 & \text{else} \end{cases}$$

**Neighbourhood criterion 1, updraft based:** majority of surroundings must have an updraft  $> w_{\max,0}$ .  
„Surroundings“:  $\sim 10 \times 10 \text{ km}^2$

**Neighbourhood criterion 2, stability based:** average of the vert. integrated buoyancy-term must be  $> B_0$ .  
Parcel: similar to mixed-layer CAPE (100 hPa layer)  
„Surroundings“:  $\sim 20 \times 20 \text{ km}^2$

**updraft filter**  
within column

→ Investigated variants:

$$\text{LPI}_1 = \frac{1}{H_{-20^\circ\text{C}} - H_{0^\circ\text{C}}} \int_{H_{0^\circ\text{C}}}^{H_{-20^\circ\text{C}}} \epsilon w^2 dz$$

$$\text{LPI}_2 = \frac{1}{H_{-20^\circ\text{C}} - H_{0^\circ\text{C}}} \int_{H_{0^\circ\text{C}}}^{H_{-20^\circ\text{C}}} \epsilon w^2 g(w) dz$$

$$\text{LPI}_3 = f_1 f_2 \frac{1}{H_{-20^\circ\text{C}} - H_{0^\circ\text{C}}} \int_{H_{0^\circ\text{C}}}^{H_{-20^\circ\text{C}}} \epsilon w^2 dz$$

$$\text{LPI}_4 = f_1 f_2 \frac{1}{H_{-20^\circ\text{C}} - H_{0^\circ\text{C}}} \int_{H_{0^\circ\text{C}}}^{H_{-20^\circ\text{C}}} \epsilon w^2 g(w) dz$$

- Time period: 28.7. – 16.8. 2014
- Hourly computation of the LPI based on COSMO-DE operational forecast data from DWD data base with the help of an IDL test program.
- 00 UTC run up to +11 h and 12 UTC run up to + 11 h combined to a continuous hourly data set.
- Comparison to LINET data (total lightning) in COSMO-DE resolution (data provided by K. Wapler, DWD). Because „it had to go fast“, the data were only available on a smaller domain (KONRAD domain).  
Computation of the **time averaged flash rate  $\pm 15$  min around the date** in the unit  $1 / (\text{km}^2 \text{ min})$ . **NOTE: depends on the grid spacing!**
- **Only  $f_1$**  could be tested, because  $B_{MF}$  is not in data base. For  $f_2$  it is assumed that it has no effect during this period. **The parameter  $w_{\max,0}$  has been varied** to determine the „best“ value **(which is resolution dependent!)**:

$$w_{\max,0} = 1.1 \text{ m/s}$$

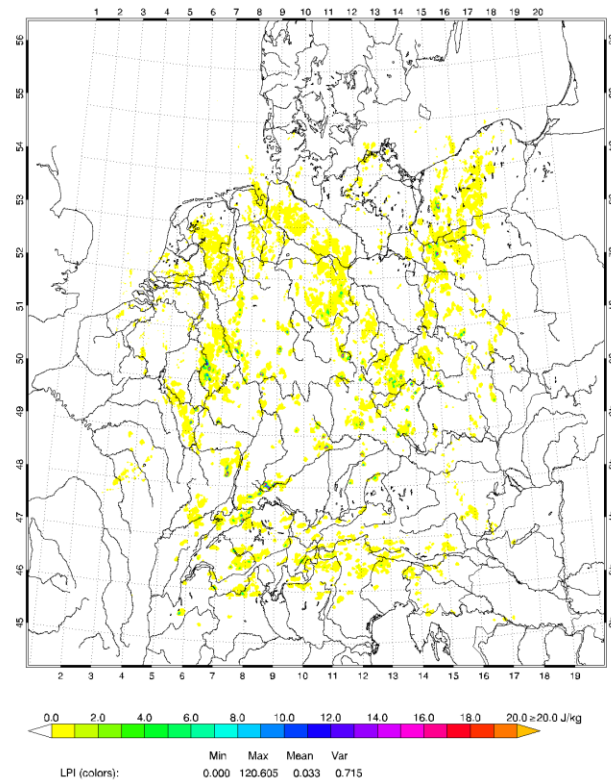
# A first test using COSMO-DE

Deutscher Wetterdienst  
Wetter und Klima aus einer Hand



**CDE-Routi:  $LPI_1$**

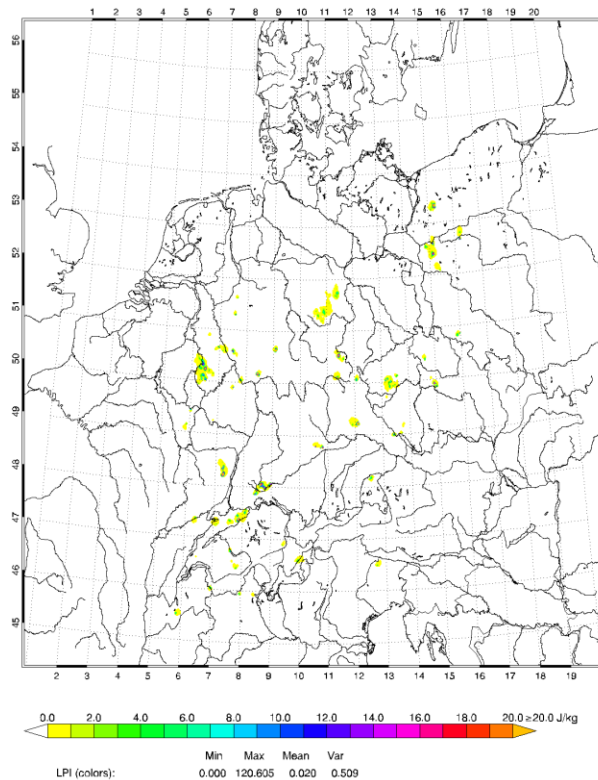
**LPI COSMO-DE no neighbourhood crit.**  
LPI 20140804120000 UTC +00020000



$W_{\text{neighbour}} = \text{NaN}$

**$LPI_3$  (without  $f_2$ )**

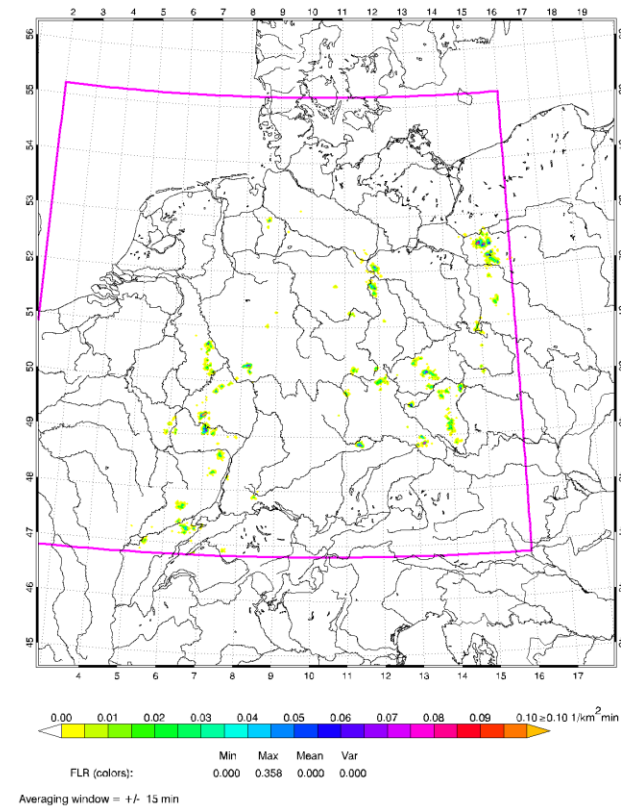
**LPI COSMO-DE neighbourhood crit.**  
LPI 20140804120000 UTC +00020000



$W_{\text{neighbour}} = 1.1$  ms

**Obs LINET t  $\pm$  15 min**

**FLR  $\pm$  15 min LINET**  
FLR [ $1/\text{km}^2$  min] 20140804140000 UTC  $\pm$  15 min





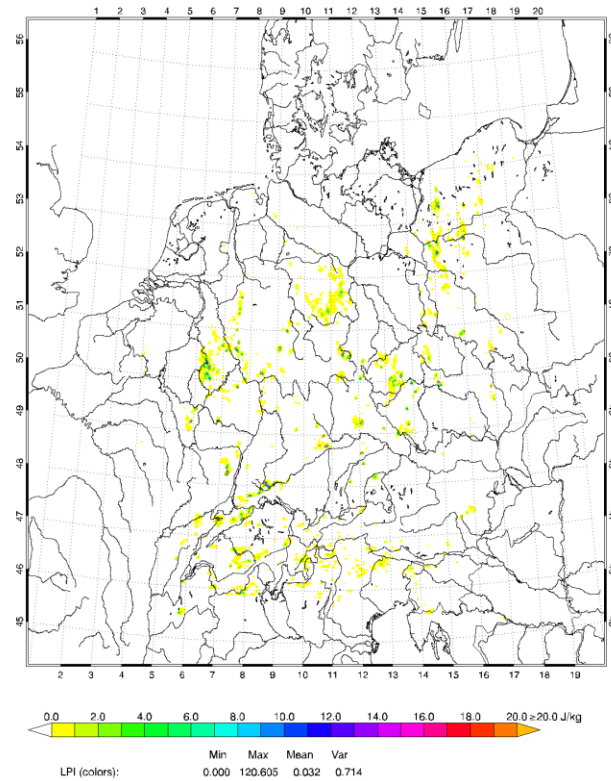
# A first test using COSMO-DE

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**CDE-Routi:  $LPI_2$**

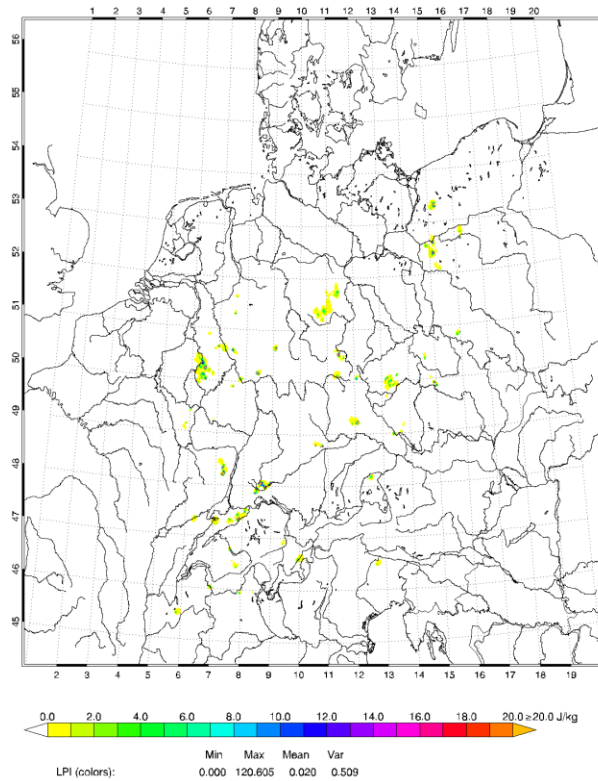
**LPI COSMO-DE no neighbourhood crit.**  
LPI 20140804120000 UTC +00020000



$W_{\text{neighbour}} = \text{NaN}$

**$LPI_4$  (without  $f_2$ )**

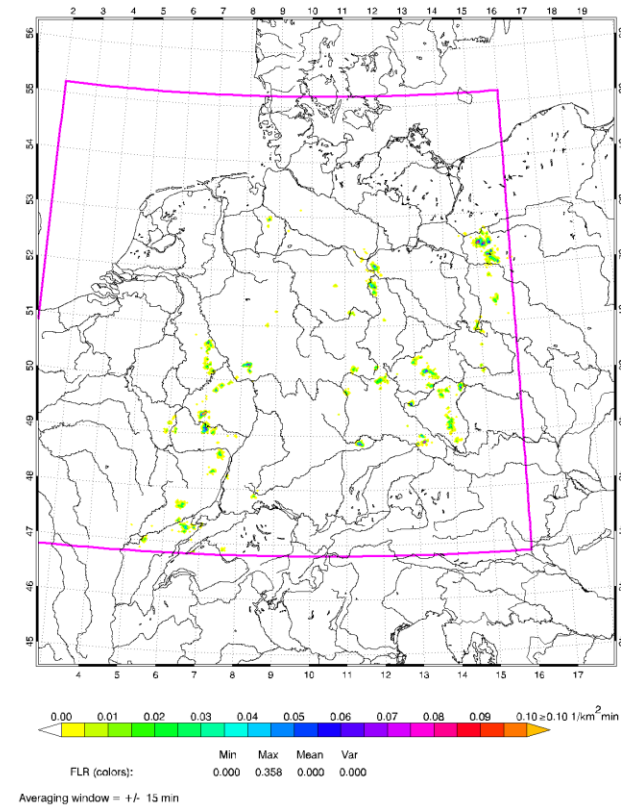
**LPI COSMO-DE neighbourhood crit.**  
LPI 20140804120000 UTC +00020000



$W_{\text{neighbour}} = 1.1$  ms

**Obs LINET t  $\pm$  15 min**

**FLR  $\pm$  15 min LINET**  
FLR [ $1/\text{km}^2$  min] 20140804140000 UTC  $\pm$  15 min





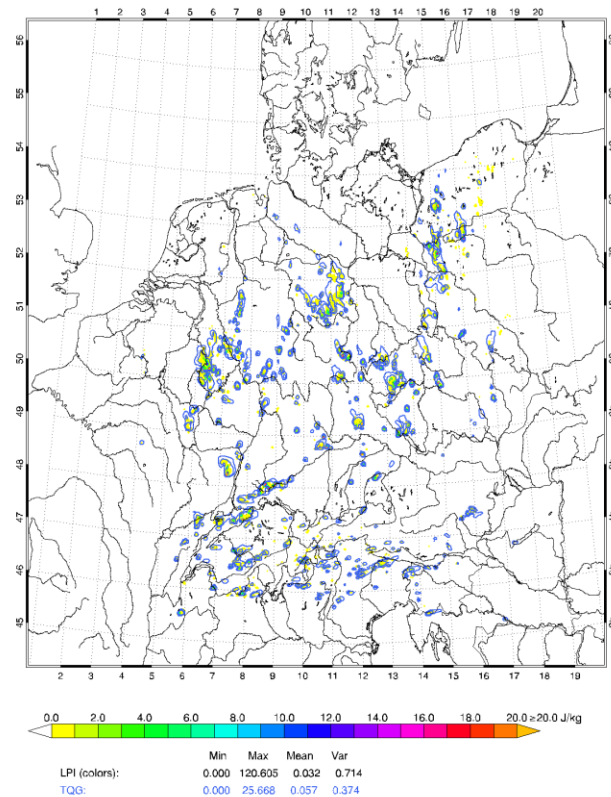
# A first test using COSMO-DE

Deutscher Wetterdienst  
Wetter und Klima aus einer Hand



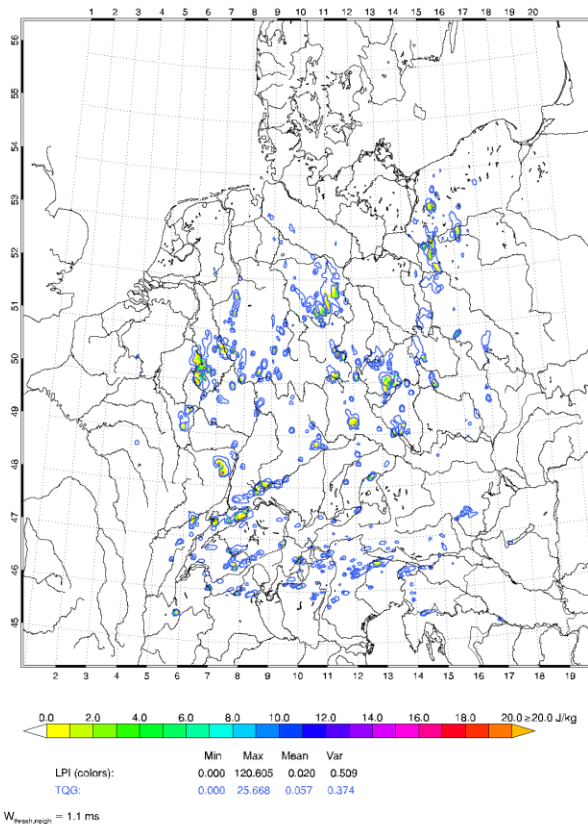
## CDE-Routi: $LPI_2$ + TQG

**LPI COSMO-DE no neighbourhood crit.**  
LPI, TQG, 20140804120000 UTC +00020000



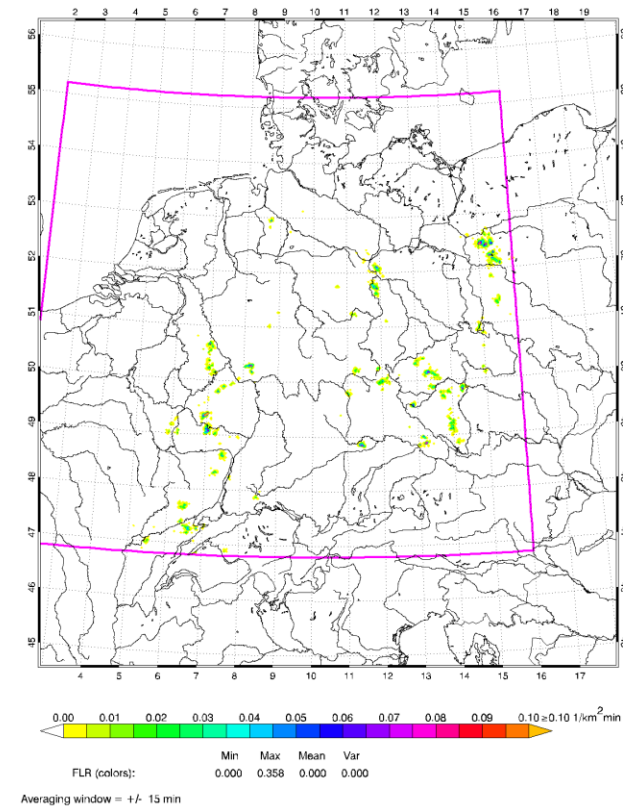
## $LPI_4$ (without $f_2$ ) + TQG

**LPI COSMO-DE neighbourhood crit.**  
LPI, TQG, 20140804120000 UTC +00020000



## Obs LINET t $\pm$ 15 min

**FLR  $\pm$  15 min LINET**  
FLR [ $1/\text{km}^2 \text{ min}$ ] 20140804140000 UTC  $\pm$  15 min

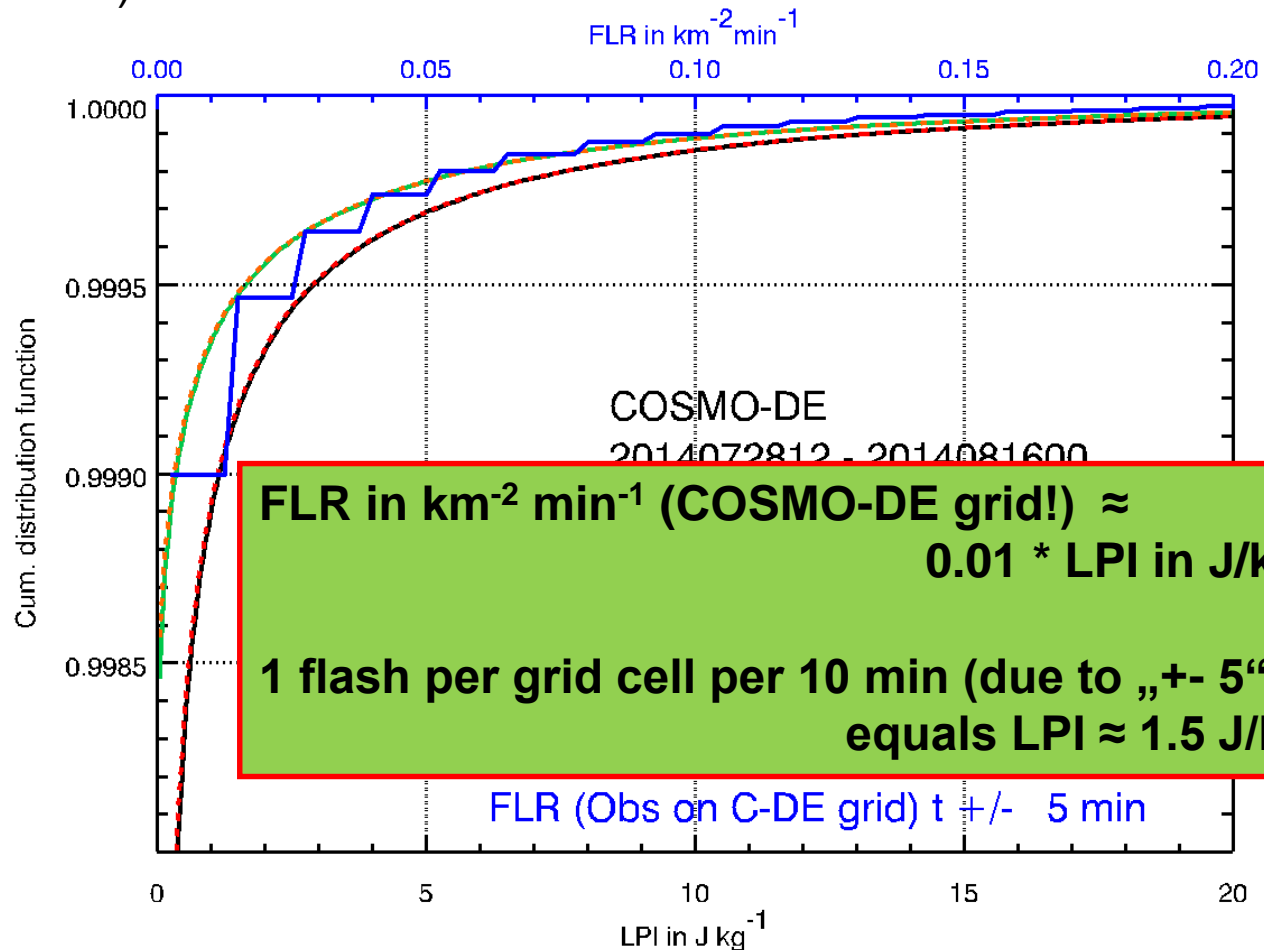


(TQG: Isolines 0.1 and 1.0  $\text{kg}/\text{m}^2$ )



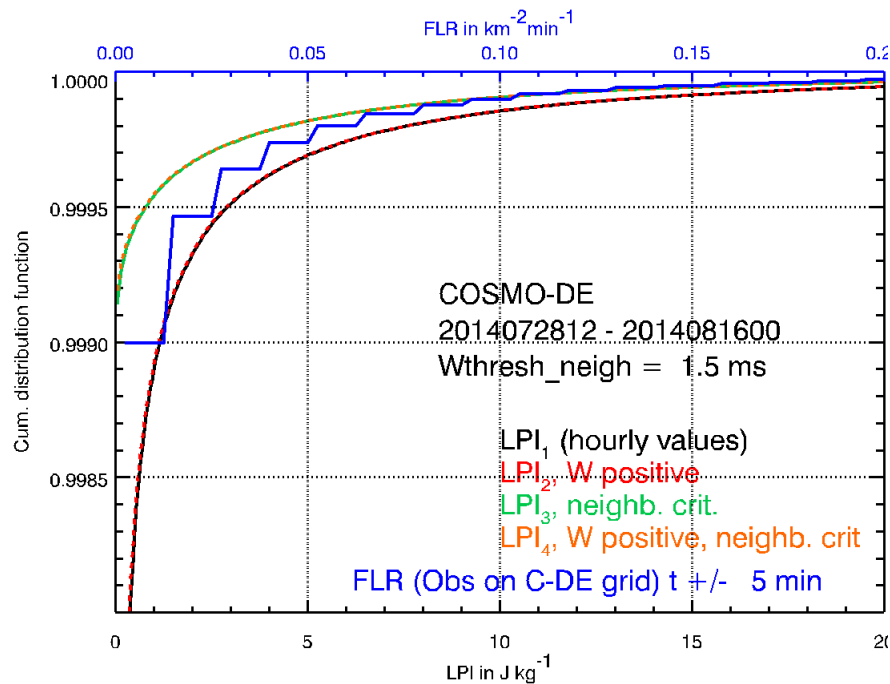
- Cumulated space-time distribution function of the 3-weeks period (only KONRAD-domain):

Relative scale of FLR to LPI „by eye“ in such a way, that it leads approximately to a constant factor.

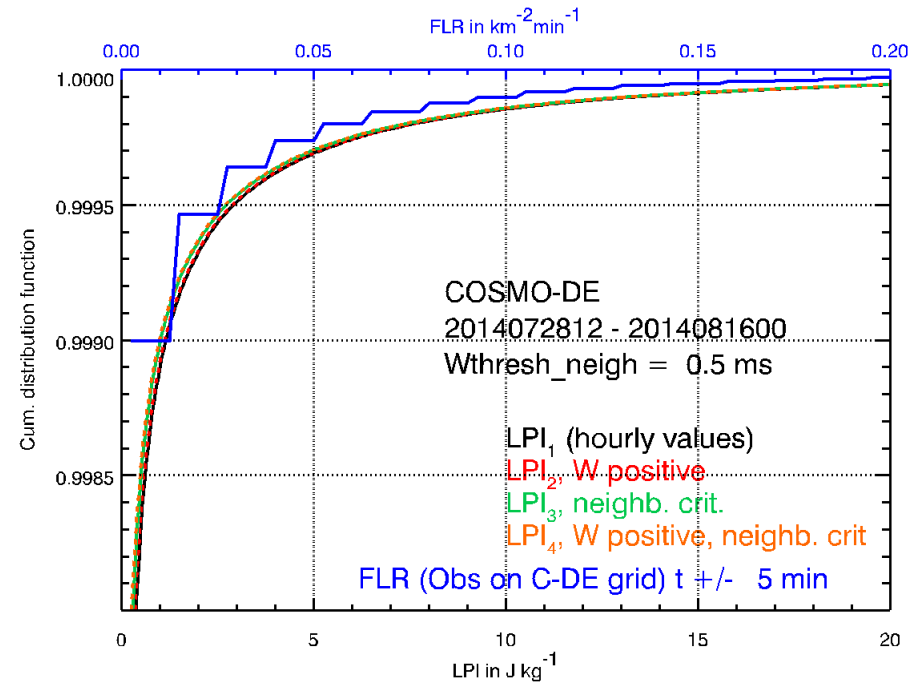


→ Variation des  $w_{\max,0}$ :

1.5 m/s



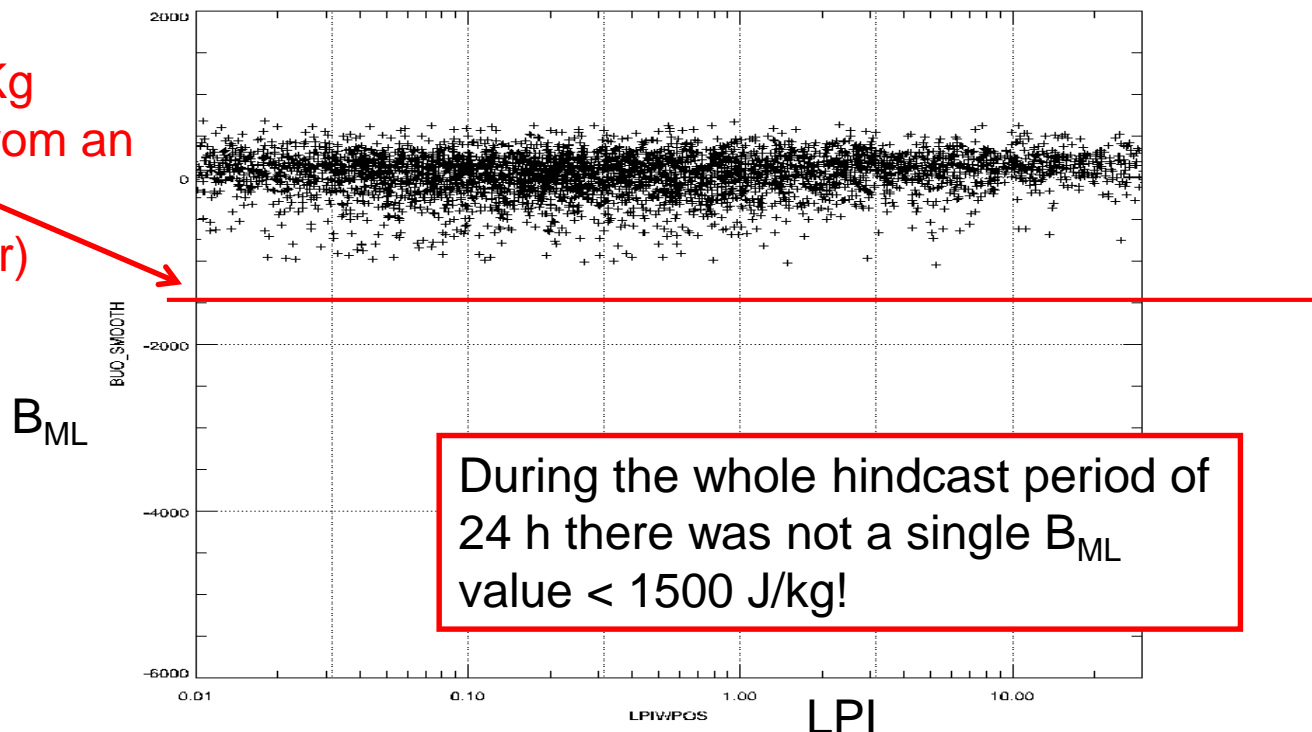
0.5 m/s



- What about the  $B_{ML} > B_0$  criterion?
- It should not be relevant in this time period, because it was a convective period. **Example from a COSMO-DE Hindcast:**

2014080312 UTC + 02 h

$B_0 = -1500 \text{ J/Kg}$   
(determined from an  
October  
case, see later)



- Time period: 6.10. – 23.10. 2014
- Hourly computation of the LPI based on COSMO-DE operational forecast data from DWD data base with the help of an IDL test program.
- 00 UTC run up to +11 h and 12 UTC run up to + 11 h combined to a continuous hourly data set.
- Comparison to LINET data (total lightning) in COSMO-DE resolution (data provided by K. Wapler, DWD). This time, we have data everywhere in the COSMO-DE domain.  
Computation of the **time averaged flash rate  $\pm 15$  min around the date** in the unit  $1 / (\text{km}^2 \text{ min})$ . **NOTE: depends on the grid spacing!**
- At first, still only  $f_1$  filter possible.
- Concerning  $f_2$  the 22.10.2014 was simulated as HINDCAST (newer model version, driven by analyses), and parameters  $w_{\text{max},0}$  and  $B_0$  have been varied to find their „best“ values **(model-, resolution dependent!)**:

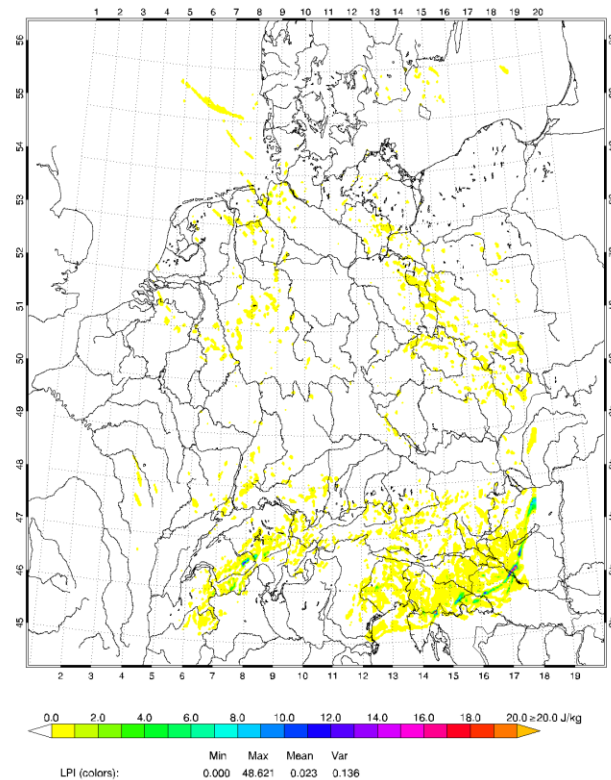
$$w_{\text{max},0} = 1.1 \text{ m/s}$$

$$B_0 = -1500 \text{ J/kg}$$

# A second test using COSMO-DE

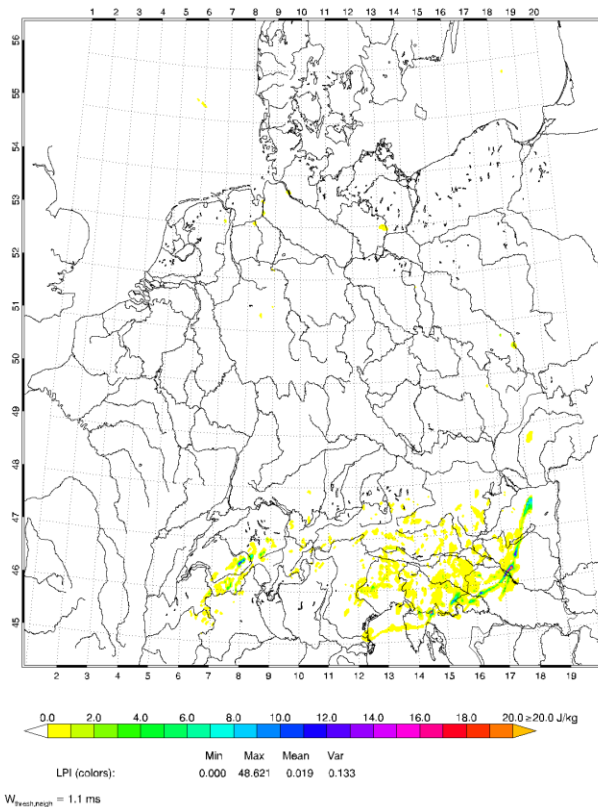
CDE-Routi:  $LPI_2$

LPI COSMO-DE no neighbourhood crit.  
LPI 20141022000000 UTC +00010000

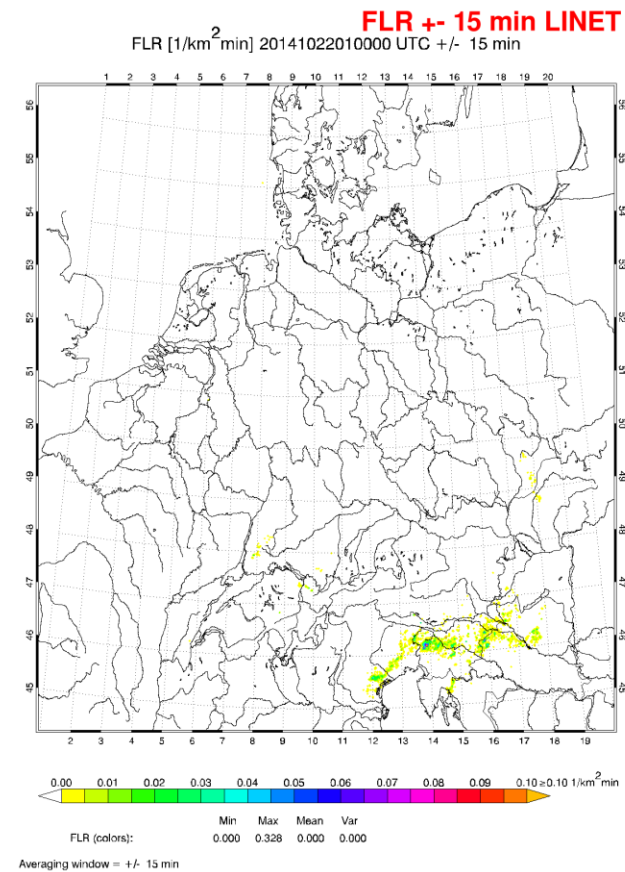


$LPI_4$  (without  $f_2$ )

LPI COSMO-DE neighbourhood crit.  
LPI 20141022000000 UTC +00010000



Obs LINET t +/- 15 min



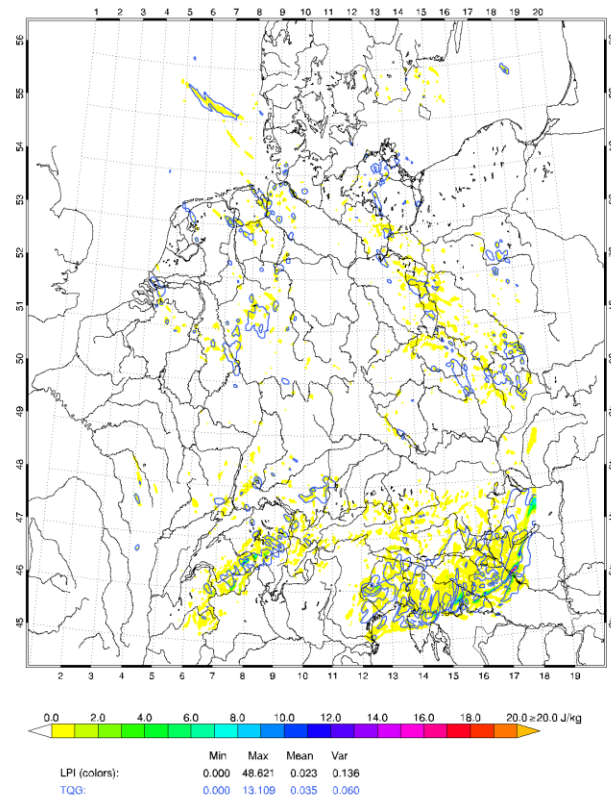
**Graupel formation in orogr. wave clouds gives  $LPI > 0$ !**  
**Therefore additional filter necessary:  $B_{MF} > B_0$**



# A second test using COSMO-DE

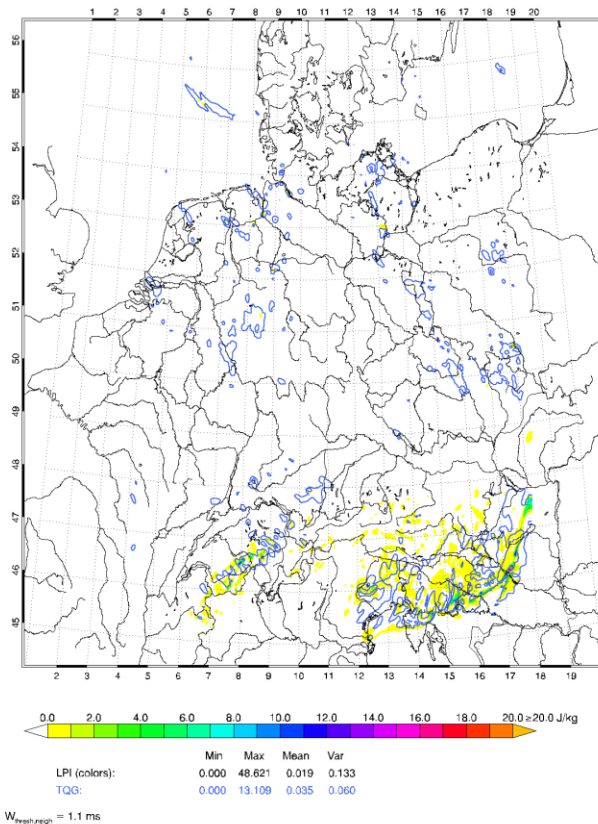
**CDE-Routi:**  $LPI_2$

**LPI COSMO-DE no neighbourhood crit.**  
LPI, TQG, 20141022000000 UTC +00010000

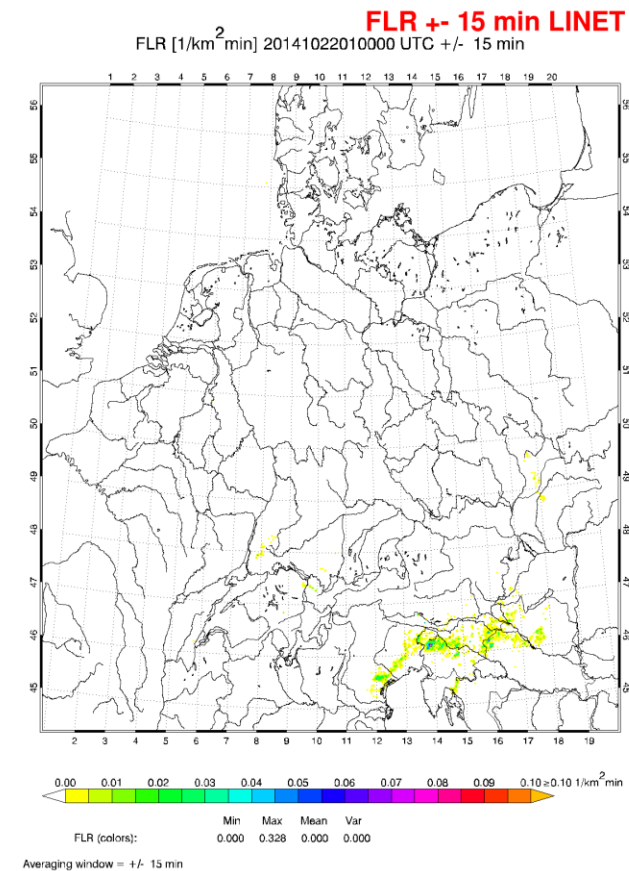


**$LPI_4$  (without  $f_2$ )**

**LPI COSMO-DE neighbourhood crit.**  
LPI, TQG, 20141022000000 UTC +00010000



**Obs LINET t +/- 15 min**



**Graupel formation in orogr. wave clouds gives  $LPI > 0$ !**  
**Therefore additional filter necessary:  $B_{MF} > B_0$**

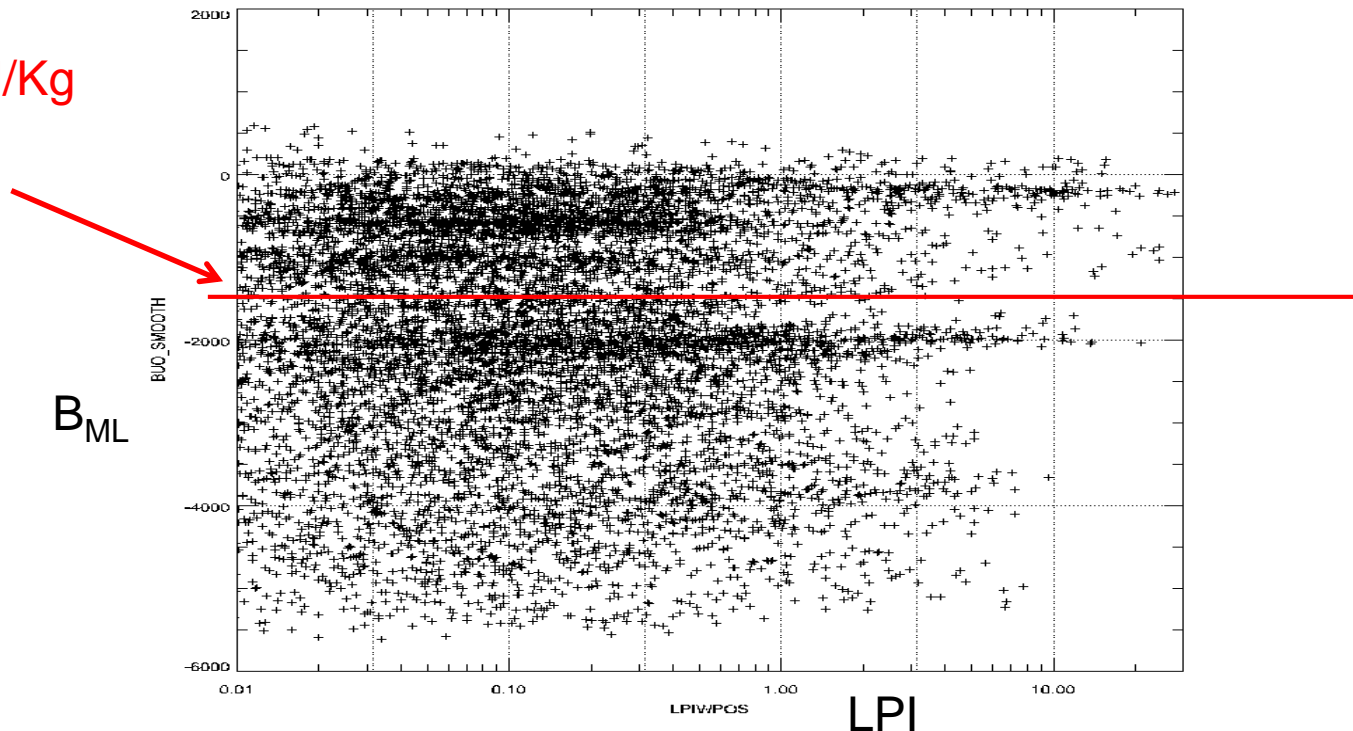


# A second test using COSMO-DE

- $B_{ML} > B_0$  criterion:
- From COSMO-DE hindcast, not routine data base!

2014102200 UTC + 01 h

$B_0 = -1500 \text{ J/Kg}$



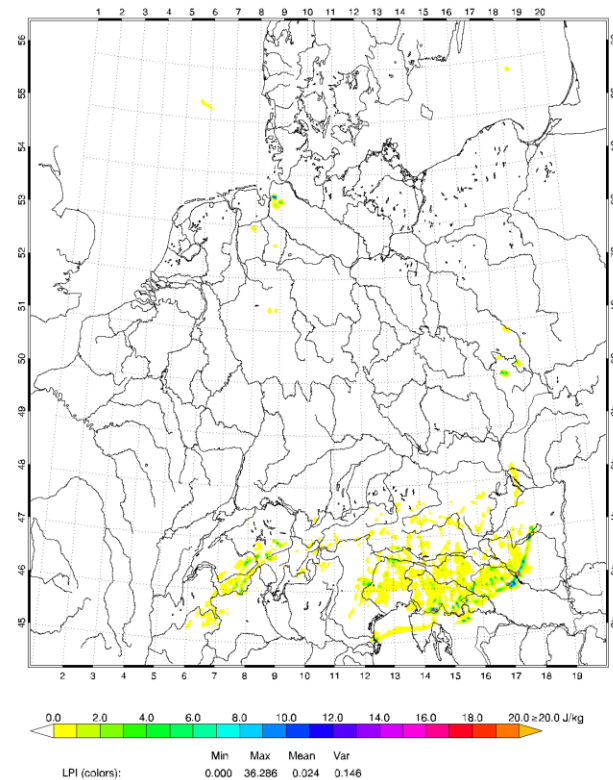
# A second test using COSMO-DE

Deutscher Wetterdienst  
Wetter und Klima aus einer Hand



Hindcast:  $LPI_2$

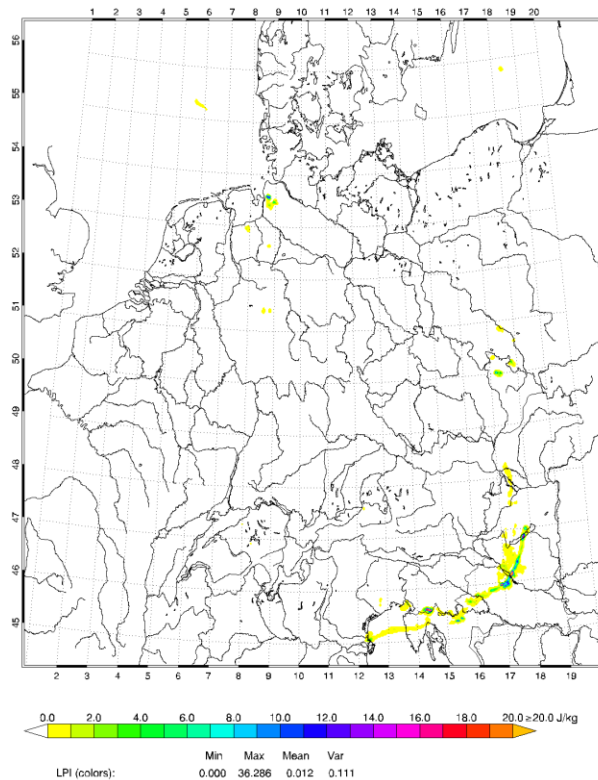
**LPI COSMO-DE no buoyancy filter**  
LPI 20141022000000 UTC +00010000



$W_{\text{feature}} = 1.1 \text{ m/s}$

$LPI_4$  (with  $f_2$ )

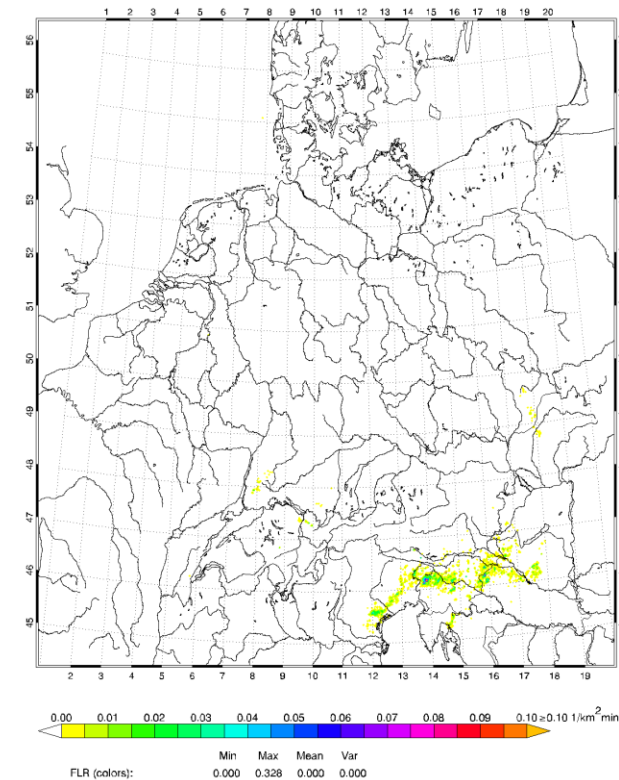
**LPI COSMO-DE buoyancy filter**  
LPI (BUO\_SMOOTH-filtered) 20141022000000 UTC +00010000



$W_{\text{feature}} = 1.1 \text{ m/s}$ , BUO\_SMOOTH > -1500 J/kg

Obs LINET t +/- 15 min

**FLR +/- 15 min LINET**  
FLR [ $1/\text{km}^2 \text{ min}$ ] 20141022010000 UTC +/- 15 min



Averaging window = +/- 15 min

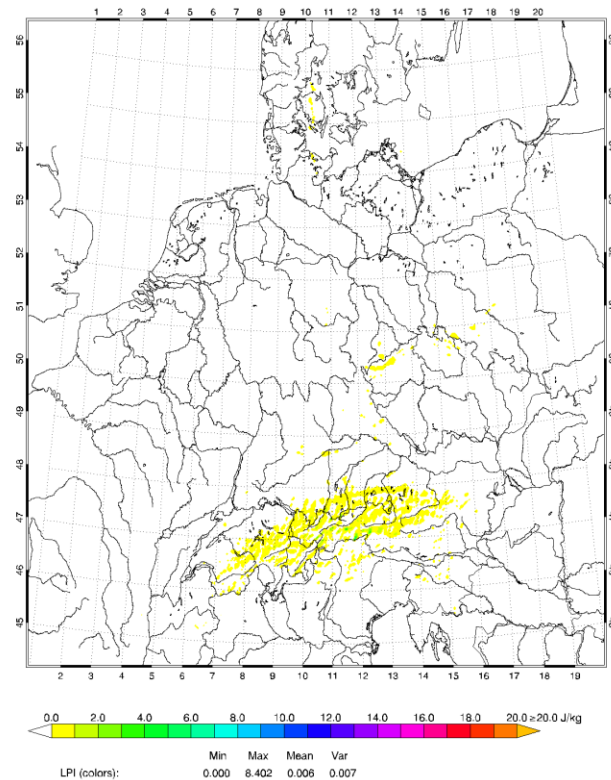
**Graupel formation in orogr. wave clouds gives  $LPI > 0$ !**  
**Filter  $B_{MF} > B_0$  works well!**



# A second test using COSMO-DE

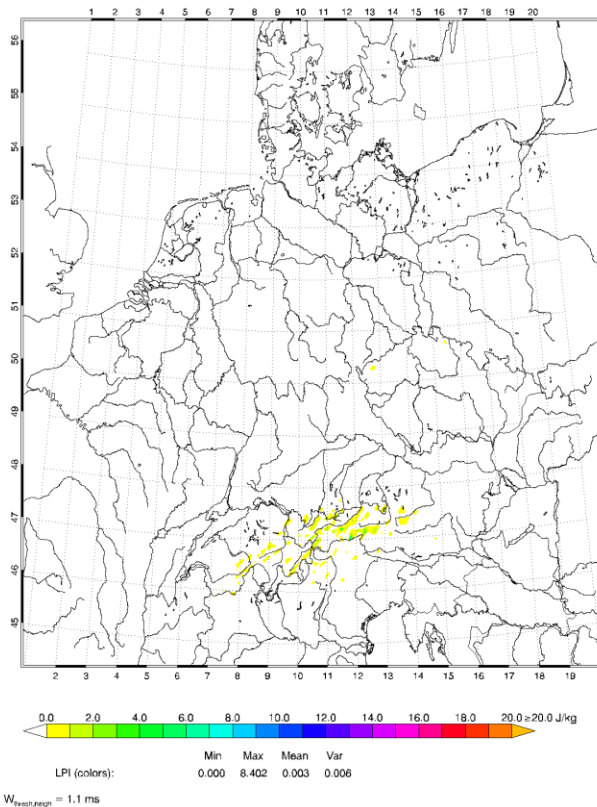
**CDE-Routi:  $LPI_2$**

**LPI COSMO-DE no neighbourhood crit.**  
LPI 20141022120000 UTC +00110000



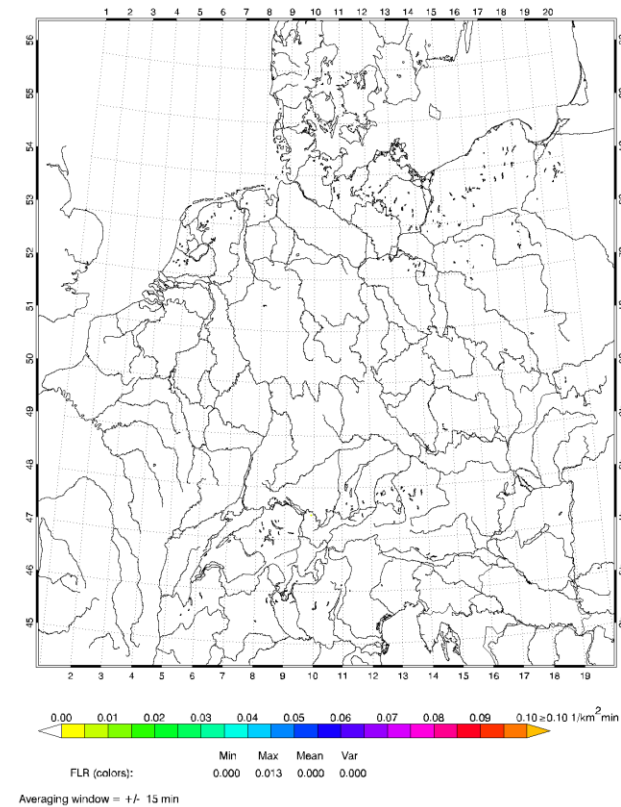
**$LPI_4$  (without  $f_2$ )**

**LPI COSMO-DE neighbourhood crit.**  
LPI 20141022120000 UTC +00110000



**Obs LINET t +/- 15 min**

**FLR +/- 15 min LINET**  
FLR [ $1/\text{km}^2 \text{ min}$ ] 2014102230000 UTC +/- 15 min



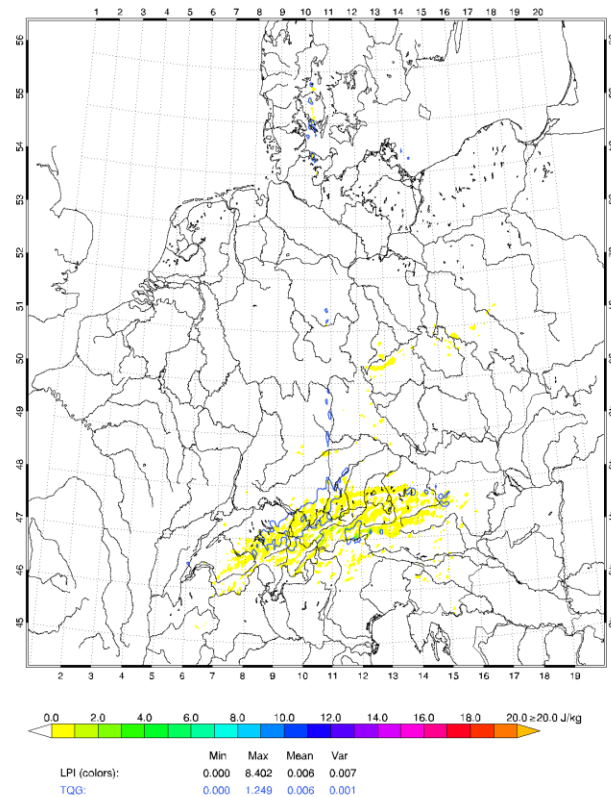
**Graupel formation in orogr. wave clouds gives  $LPI > 0$ !**  
**Therefore additional filter necessary:  $B_{MF} > B_0$**



# A second test using COSMO-DE

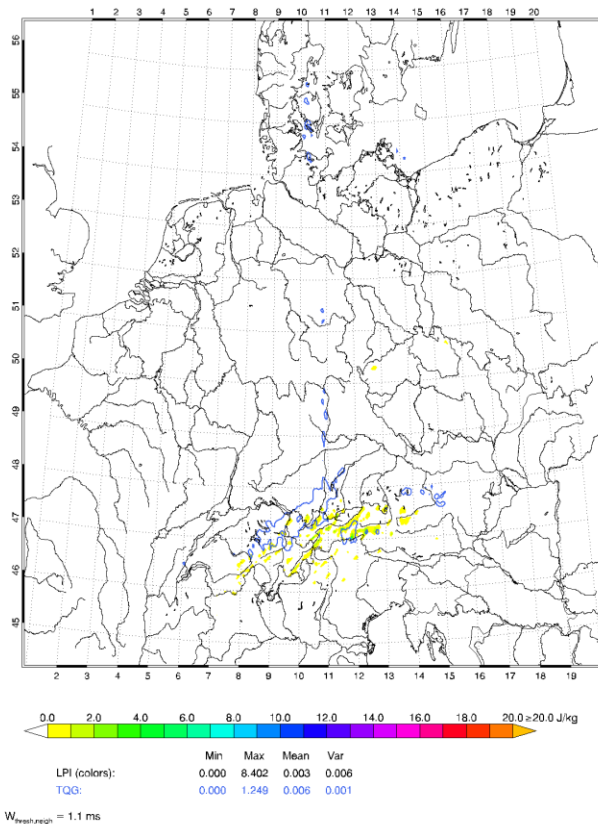
**CDE-Routi:**  $LPI_2$

**LPI COSMO-DE no neighbourhood crit.**  
LPI, TQG, 20141022120000 UTC +00110000

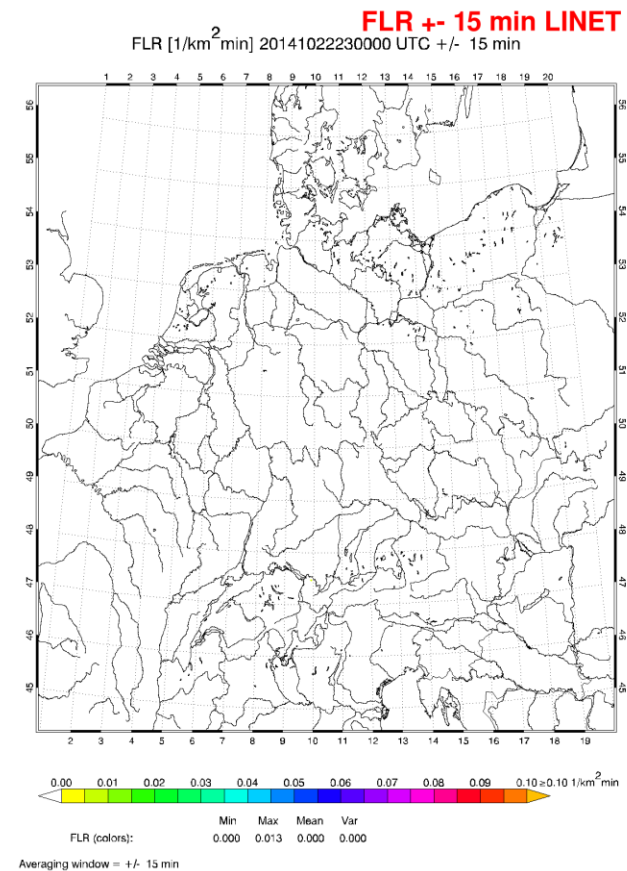


$LPI_4$  (without  $f_2$ )

**LPI COSMO-DE neighbourhood crit.**  
LPI, TQG, 20141022120000 UTC +00110000



**Obs LINET t +/- 15 min**

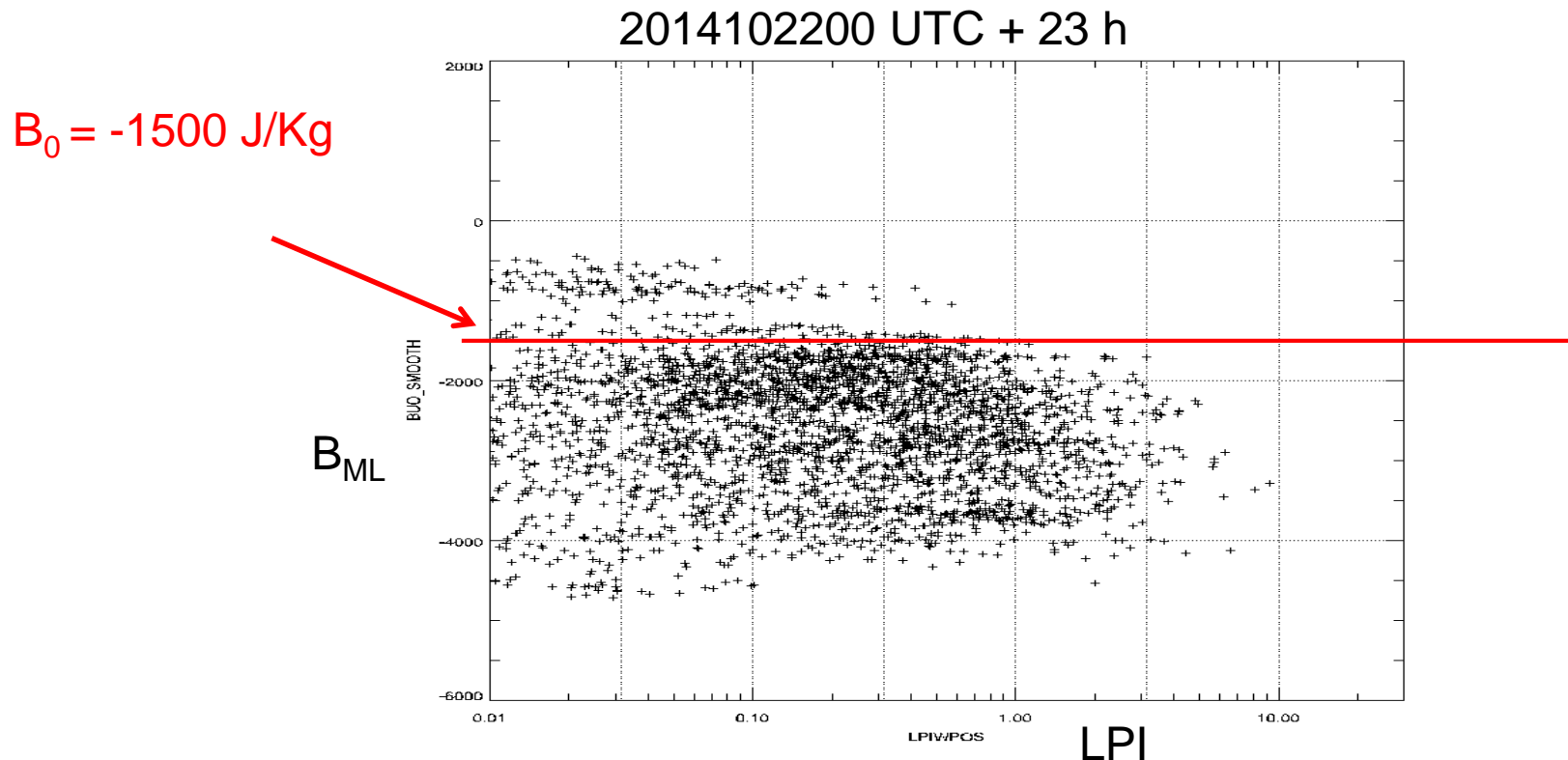


**Graupel formation in orogr. wave clouds gives  $LPI > 0$ !**  
**Therefore additional filter necessary:  $B_{MF} > B_0$**

# A second test using COSMO-DE

→  $B_{ML} > B_0$  criterion:

→ From COSMO-DE hindcast, not routine data base!



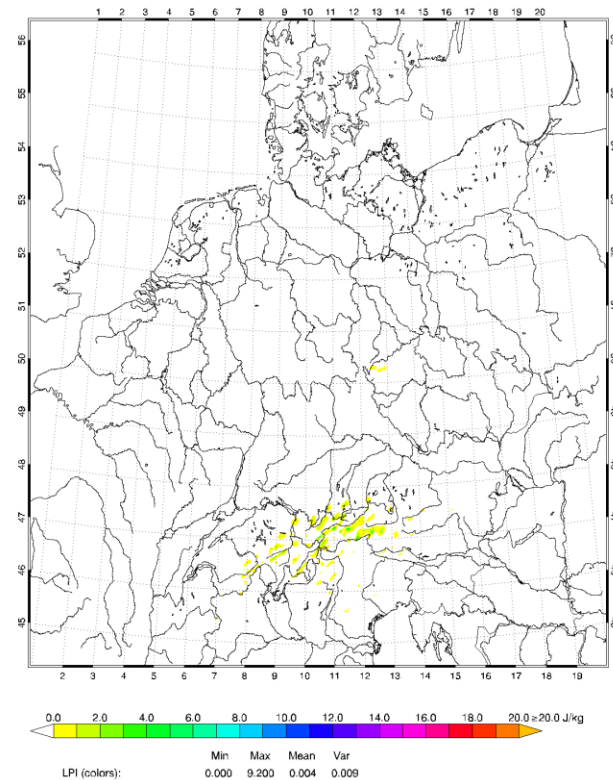
# A second test using COSMO-DE

Deutscher Wetterdienst  
Wetter und Klima aus einer Hand



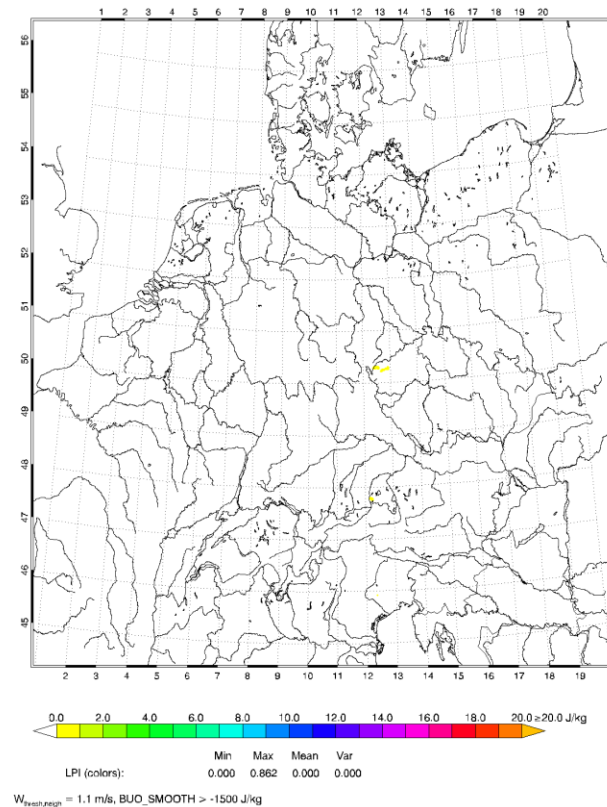
Hindcast:  $LPI_2$

**LPI COSMO-DE no buoyancy filter**  
LPI 20141022000000 UTC +00230000



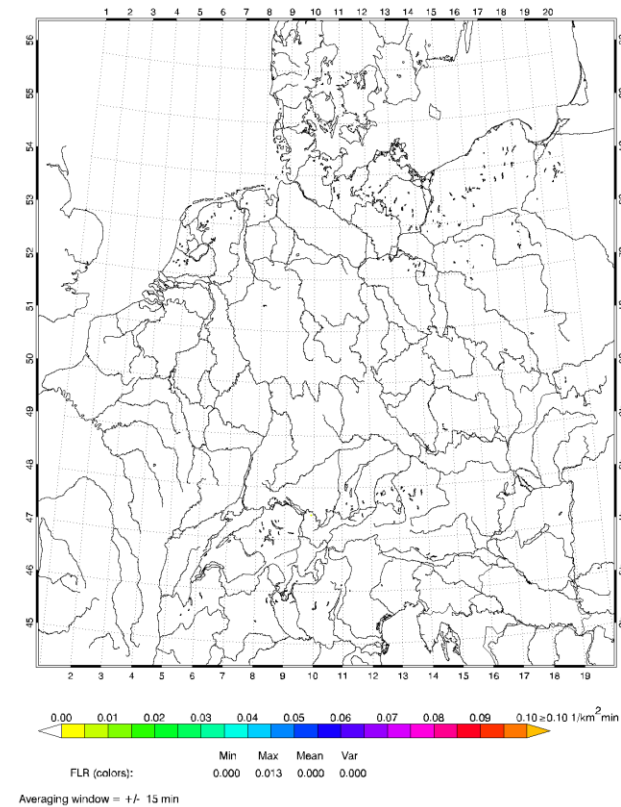
$LPI_4$  (mit  $f_2$ )

**LPI COSMO-DE buoyancy filter**  
LPI (BUO\_SMOOTH-filtered) 20141022000000 UTC +00230000



Obs LINET t  $\pm$  15 min

**FLR  $\pm$  15 min LINET**  
FLR [ $1/\text{km}^2 \text{ min}$ ] 20141022230000 UTC  $\pm$  15 min



**Graupel formation in orogr. wave clouds gives  $LPI > 0$ !**  
**Filter  $B_{MF} > B_0$  works well!**



## The comparison with lightning data (flash rates) „by eye“ shows:

- ➔ Statistics of the space-time distribution of the LPI values  $> 0$  corresponds well with that of the observed flash rates.
- ➔ LPI intimately tied to the explicit simulation of convective cells in the model and its ice microphysics (updraft strength, supercooled liquid, graupel, cloud ice, snow). **Ensemble prediction like COSMO-DE-EPS!**
- ➔ LPI leads to different flash signals compared to, e.g., TQG or TOT\_PREC alone. Not every convective Cell, which has a high TQG, leads to an LPI signal.
- ➔ Spatial filtering by the  $W_{\max}$  – majority criterion ( $f_1$ ) and the smoothed buoyancy-criterion ( $f_2$ ) in a horizontal neighbourhood seems to successfully eliminate spurious and false weak signals.
- ➔ Time aggregation between output timesteps? Seems not necessary for a 15-minute output interval like in COSMO-DE. And would be expensive, because spatial filtering requires a `gather_field(...)` for a global 2D field, and one wants to avoid this for every time step.



- Diagnose the LPI directly in the COSMO-Model at output time steps, or in fieldextra.
- Application in COSMO-DE-EPS:
  - Either directly (probability of exceeding some threshold etc.),
  - or as an additional predictor in a currently developed statistical method (FE 15), which derives flash rates directly from a variety of different ensemble fields.
- Application as forward operator in data assimilation
- Status:
  - Subroutines in Fortran90
  - grib numbers in next DWD grib\_api version (until then no LPI in grib2!)
  - Implem. in COSMO src\_output.f90 + performance tuning (gather\_field())
  - Timings: 24 h COSMO\_DE, LPI-output every 15 minutes, (20x10 PEs):
    - without LPI: total: 1755 s comp\_O: 23 s
    - with LPI: total: 1770 s (+ ~1 %) comp\_O: 30 s (+ ~30 %)
    - crayftn: Gfast -Ktrap=divz,inv,ovf -O2 -hflex\_mp=conservative -K trap=fp