

# High resolution numerical modelling of moist convection in statistical equilibrium: buoyancy and velocity scales

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Earth, Atmospheric and Planetary Sciences

# The radiative convective equilibrium problem: buoyancy and velocity scales (1)

One of the most important issues in the study of dry and moist convection in statistical equilibrium is the determination of buoyancy and velocity scales. These are relevant to such issues as:

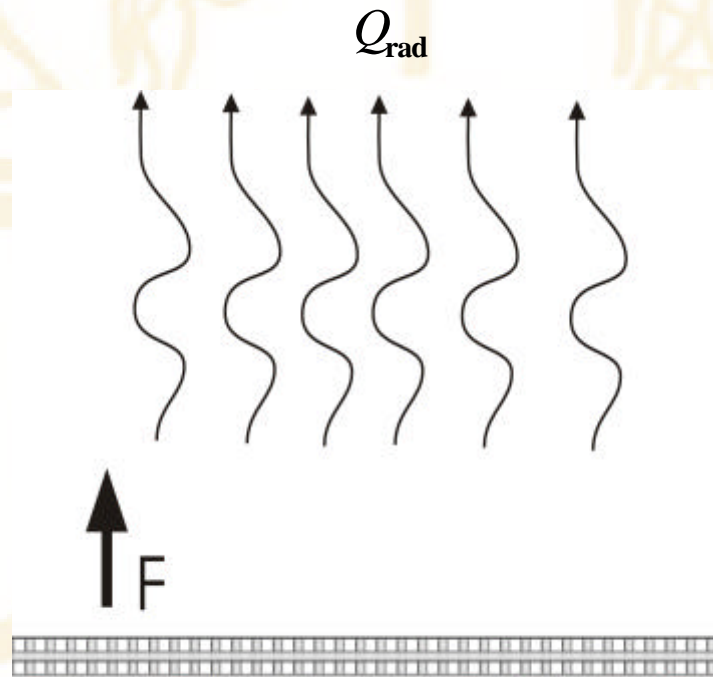
- the phase transition of random convective states to organized tropical cyclone-dominated convection
- study of the interaction between moist convective plumes and boundary layer convection
- the absence of a scaling theory for moist convection limits our understanding of the feedbacks of changes in large-scale forcing on convective ensembles and then the development of comprehensive representations of convection in large scale models

# The radiative convective equilibrium problem: buoyancy and velocity scales (2)

In the absence of large-scale circulations, the tropical atmosphere would assume a state of *radiative-moist convective equilibrium*, in which the divergence of the net vertical radiative flux (shortwave and longwave) would be compensated by the convergence of the vertical flux of enthalpy in convective clouds, except for in a thin boundary layer next to the surface, in which ordinary drag turbulence would carry the flux.

# The radiative convective equilibrium problem: buoyancy and velocity scales (3)

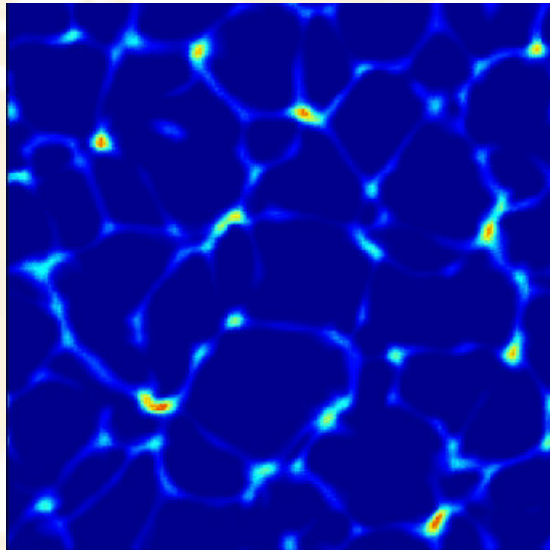
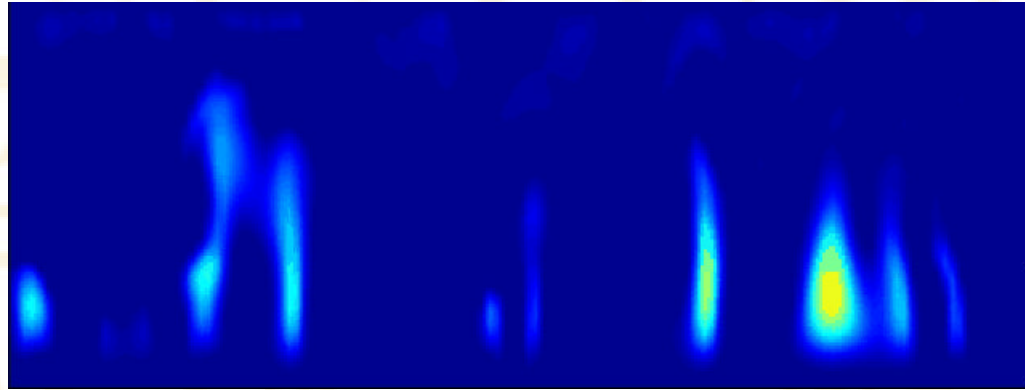
The canonical problem of radiative-dry convective equilibrium was first developed by Prandtl (1910, 1942). This problem is *the simplest model that captures some of the essential aspects of atmospheric convection.*



# The radiative convective equilibrium problem: buoyancy and velocity scales (4)

## Dry Prandtl Problem

W field



from Parodi, Emanuel and  
Provenzale, New Journal of  
Physics (2003)

# The radiative convective equilibrium problem: buoyancy and velocity scales

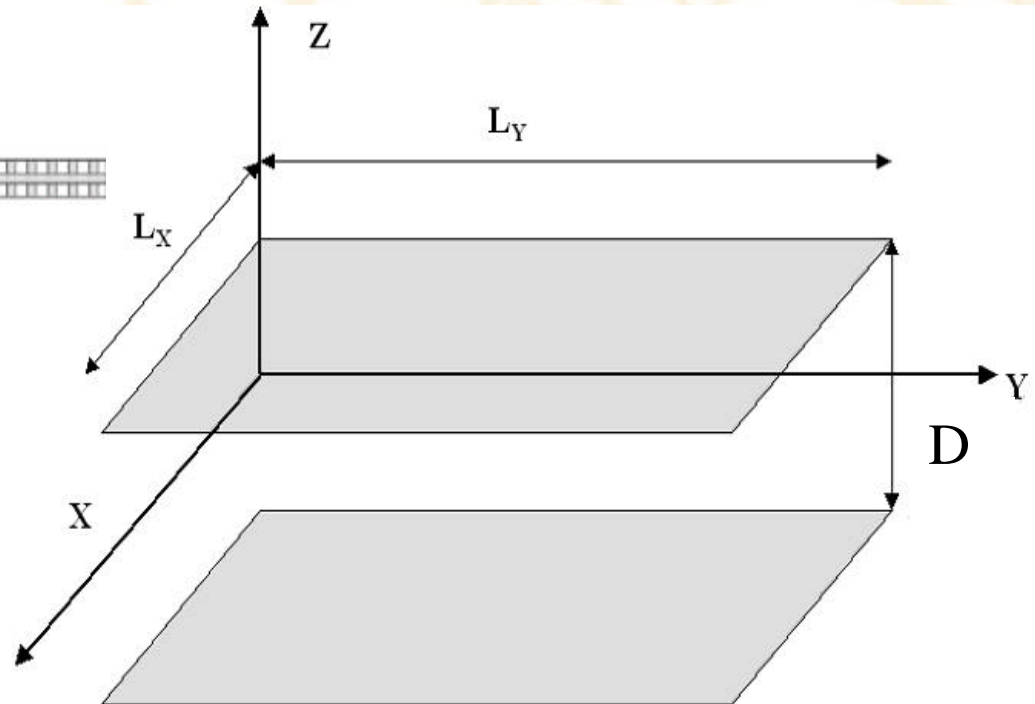
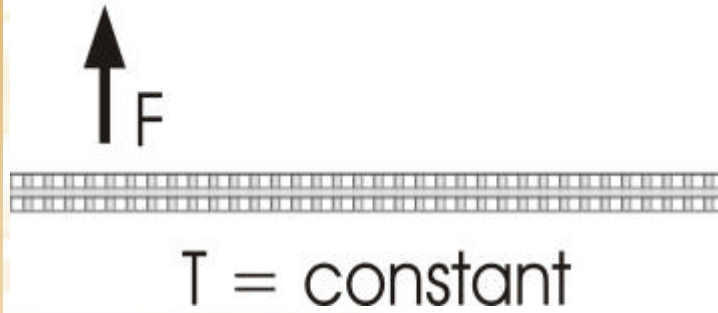
- Buoyancy and velocity scales for dry convection in statistical equilibrium were derived long ago by Prandtl (1910, 1925):  
for this problem the turbulence kinetic energy scales as  $(Fz)^{2/3}$ , where  $z$  is the altitude above the surface, while the unstable stratification decreases as  $z^{-4/3}$
- But the question of convective velocity and buoyancy scales, as well as the topic of fractional area coverage of convective clouds, are unresolved in moist convection (in radiative convective equilibrium) (Emanuel and Bister, 1996; Grabowski, 2003; Robe and Emanuel, 1996, 2001; Xu and Randall, 1998; Wu, 2001)

# Computational domain

$Q_{\text{rad}}$



- Doubly periodic domain
- Constant cooling rate  $Q_{\text{rad}}$  over the full height of the troposphere



# The radiative convective equilibrium problem: buoyancy and velocity scales

- High resolution (meso- $\gamma$  scale) simulations of an atmosphere in radiative convective equilibrium are performed using the Lokal Model;
- Prescribing different constant cooling rates,  $Q_{\text{rad}}$ , we try to characterize the velocity and buoyancy scales for moist convection in statistical equilibrium;
- The dependence of spatio-temporal properties of the convective flow field on numerical and physical details such as domain size and microphysics, is investigated

# The radiative convective equilibrium problem: buoyancy and velocity scales

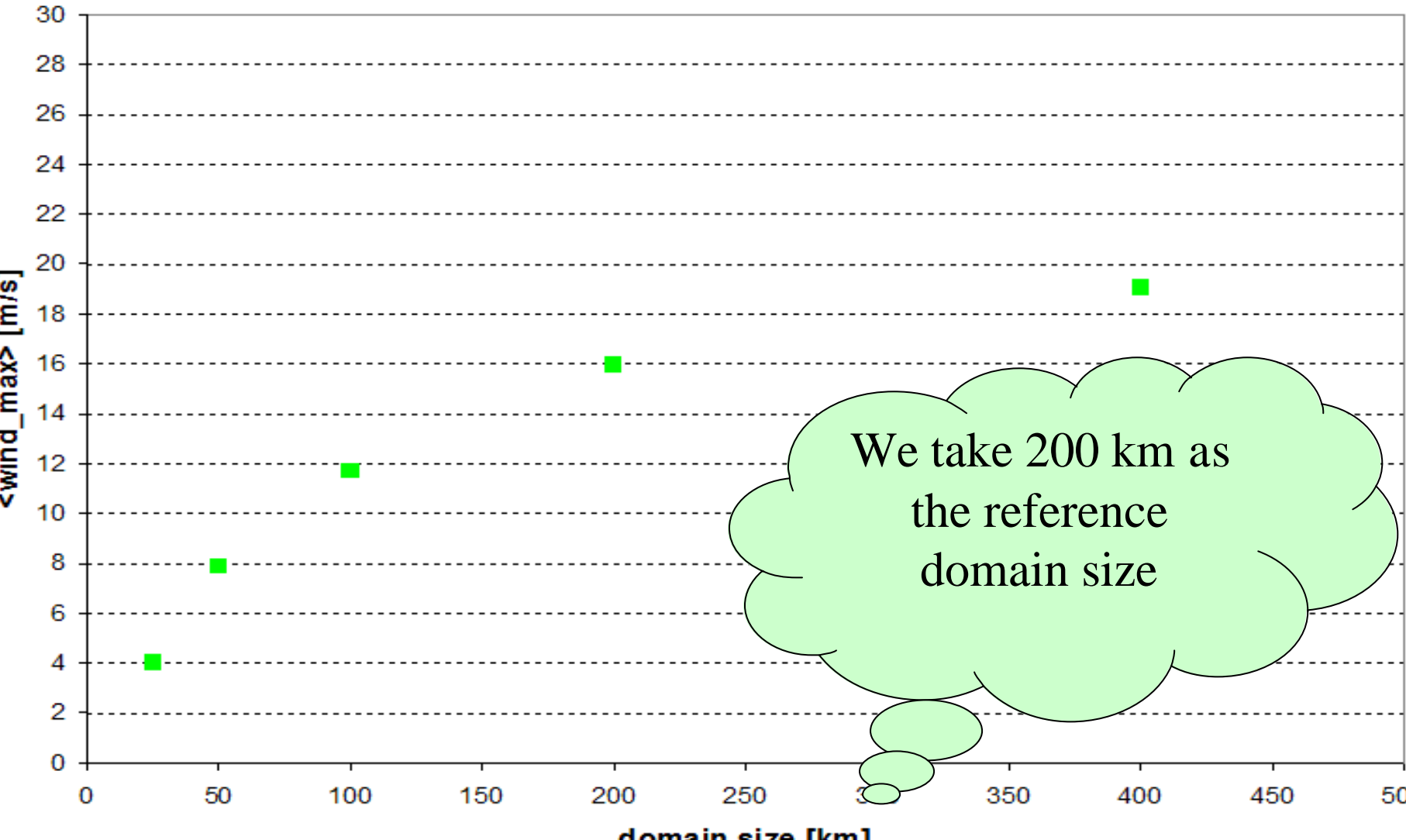
- The main hypothesis of the work is that convective updraft velocities and rainfall intensity scale with the terminal velocity of raindrops;
- For prescribed cooling rate  $Q_{\text{rad}}$ , a set of simulations with different raindrop terminal velocities (range: 2-50 m/s) is performed and the results are compared

# Model settings

- Domain sizes: 25x25x20 km, 50x50x20 km, 100x100x20 km, 200x200x20 km and 400x400x20 km
- Horizontal resolution: 2 km (in the future 500 m is planned)
- No orography
- Doubly periodic boundary conditions
- Kessler microphysics
- Constant cooling rate  $Q_{\text{rad}}$ : -2 K/day, -4 K/day and -6 K/day
- Leapfrog HE-VI time integration scheme
- Rayleigh damping layer in upper layers ( $15 < z < 20$  km)
- The lower boundary is a passive ocean with constant temperature  $T_{\text{s}}=300$  K

# Radiative convective equilibrium statistics: role of the domain size

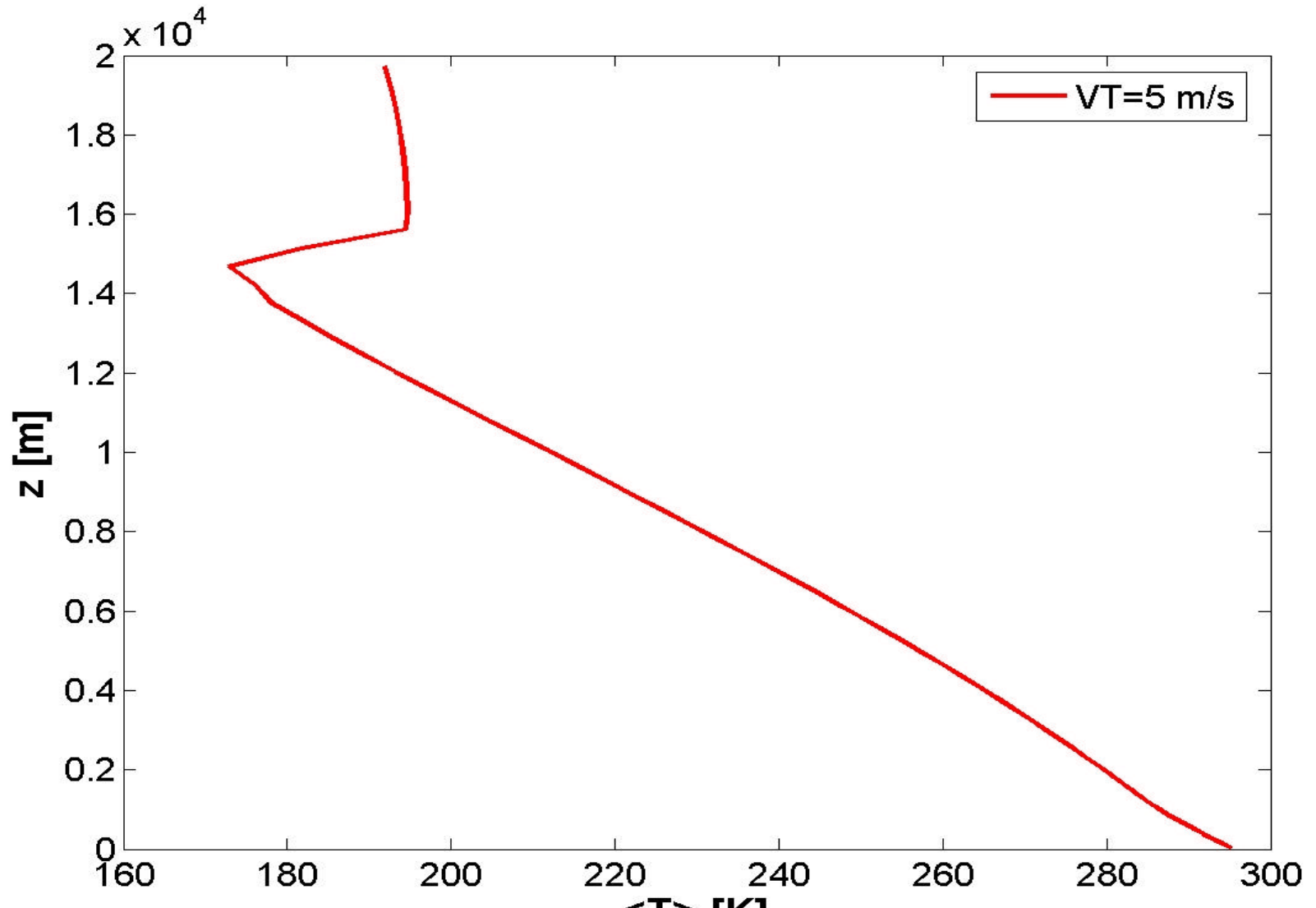
$Q_{\text{rad}} = -4$  K/day, raindrop terminal velocity  $V_T = 5$  m/s



# Radiative convective equilibrium statistics:

## Horizontally averaged thermodynamic profiles

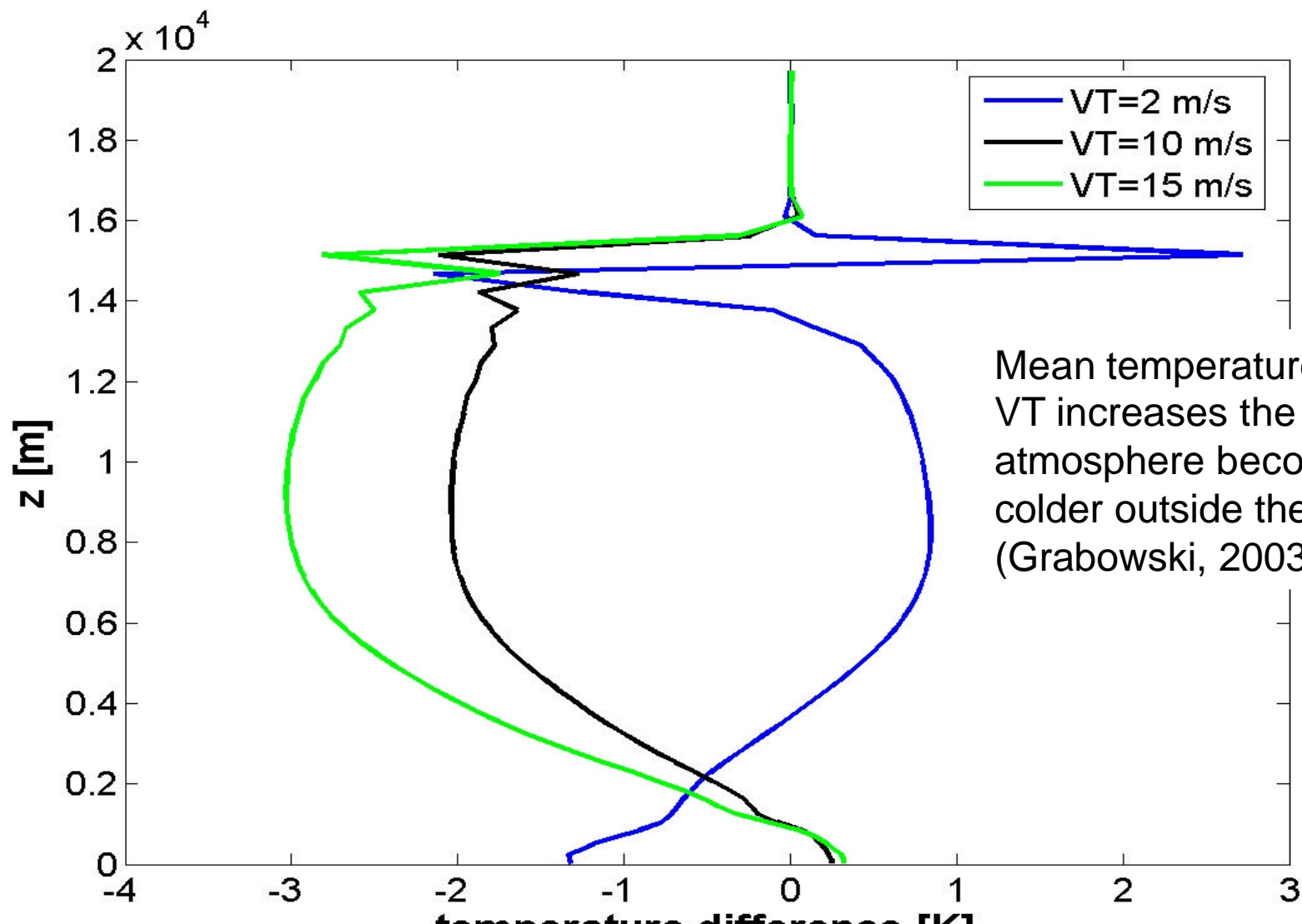
$Q_{\text{rad}} = -4$  K/day,  $V_T = 5$  m/s: control run



# Radiative convective equilibrium statistics:

## Horizontally averaged thermodynamic profiles

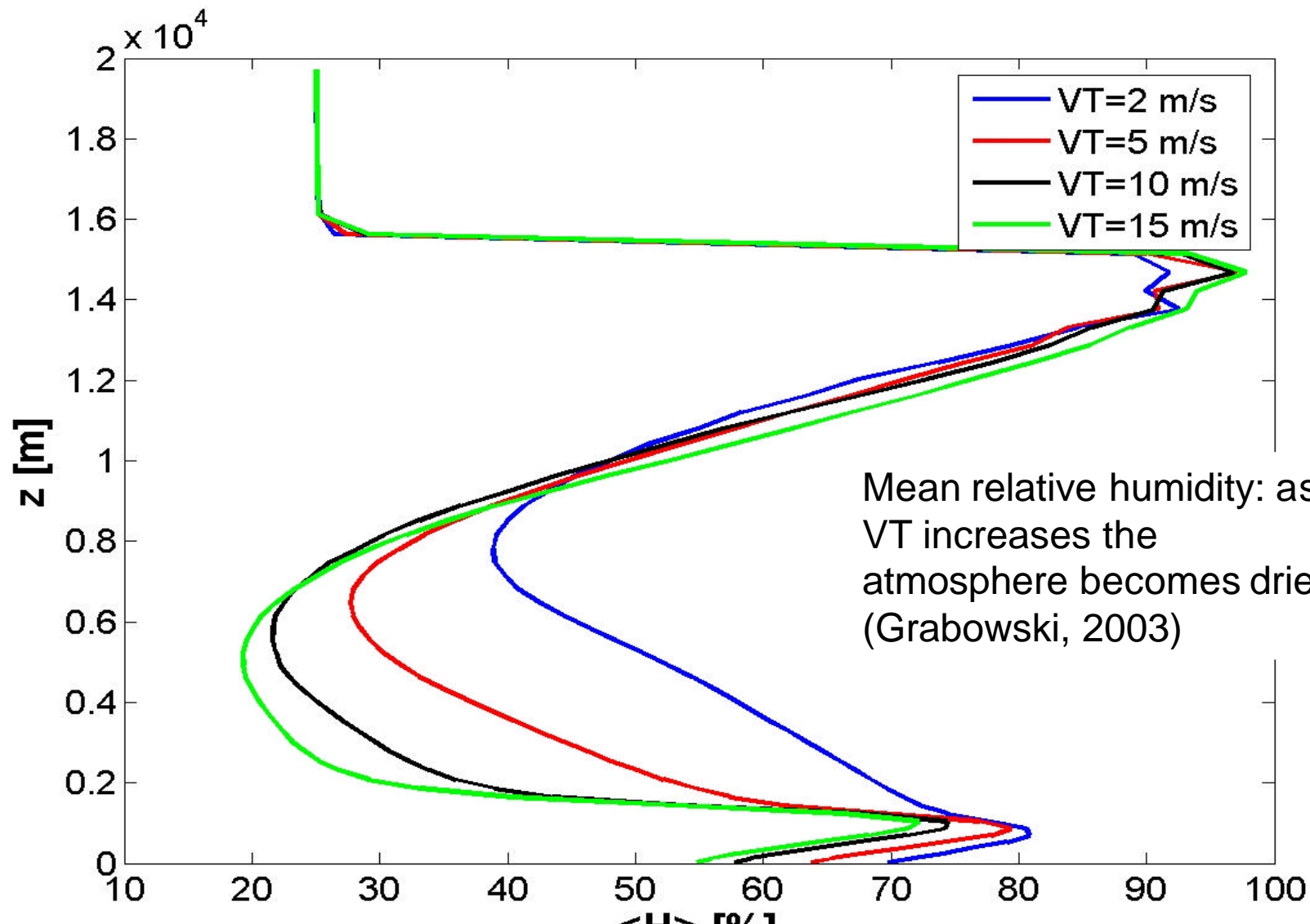
$$Q_{\text{rad}} = -4 \text{ K/day}: \langle T_{\text{VT}} \rangle - \langle T_{\text{VT}=5 \text{ m/s}} \rangle$$



# Radiative convective equilibrium statistics:

## Horizontally averaged thermodynamic profiles

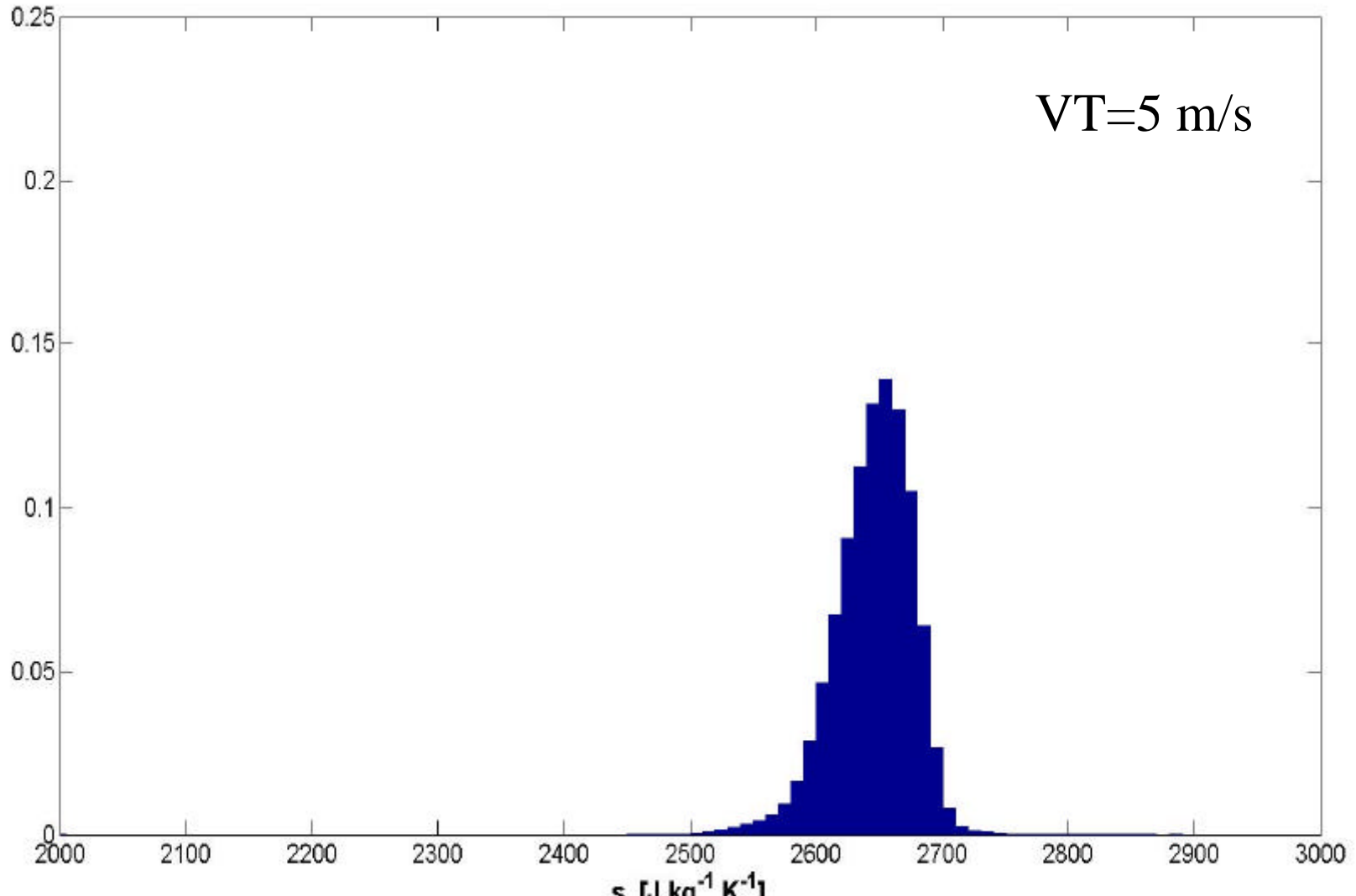
$$Q_{\text{rad}} = -4 \text{ K/day}$$



# Radiative convective equilibrium statistics:

## Moist static energy

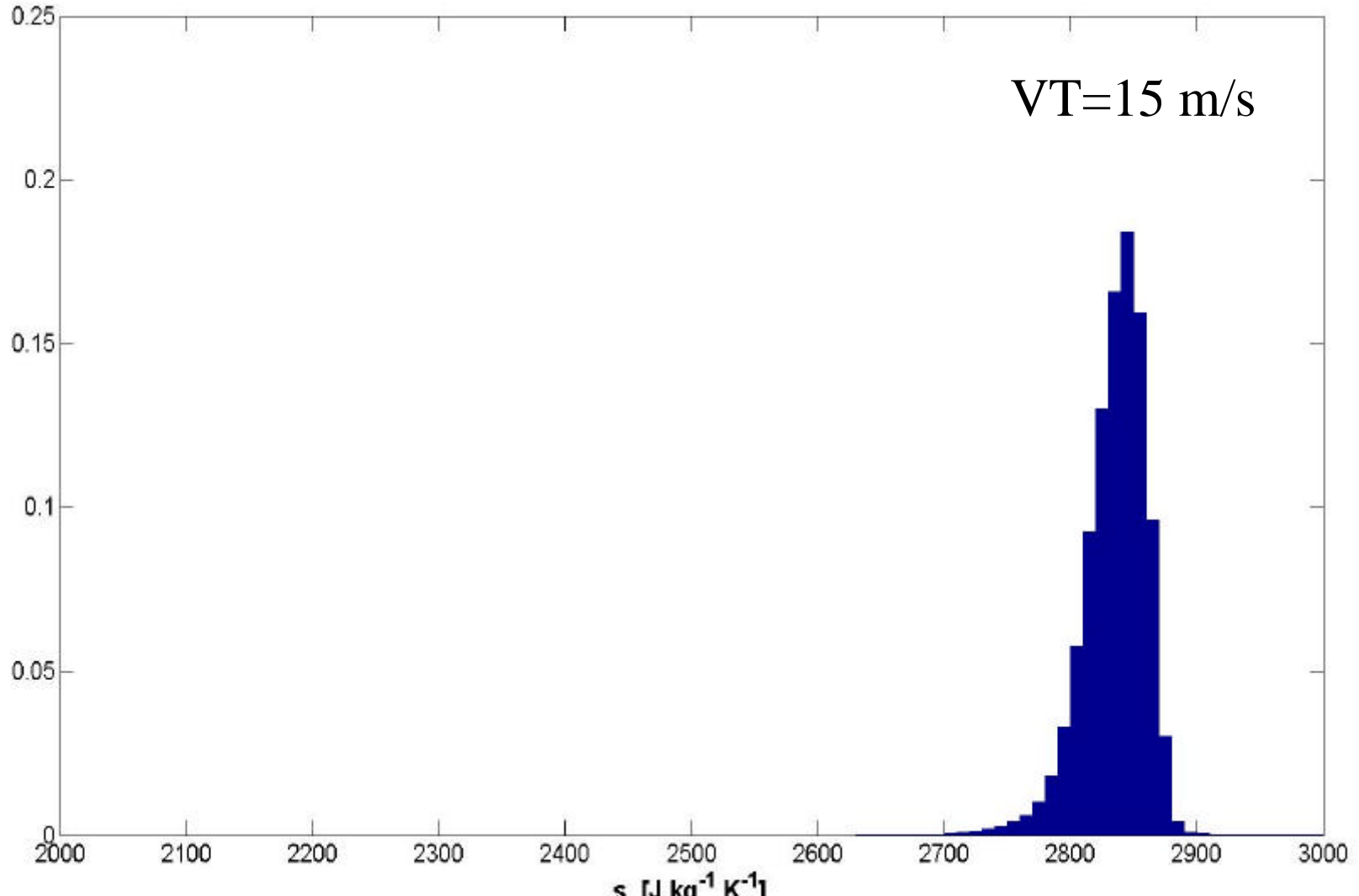
$$Q_{\text{rad}} = -4 \text{ K/day}$$



# Radiative convective equilibrium statistics:

## Moist static energy

$$Q_{\text{rad}} = -4 \text{ K/day}$$



# Radiative convective equilibrium statistics:

## Buoyancy and velocity scales

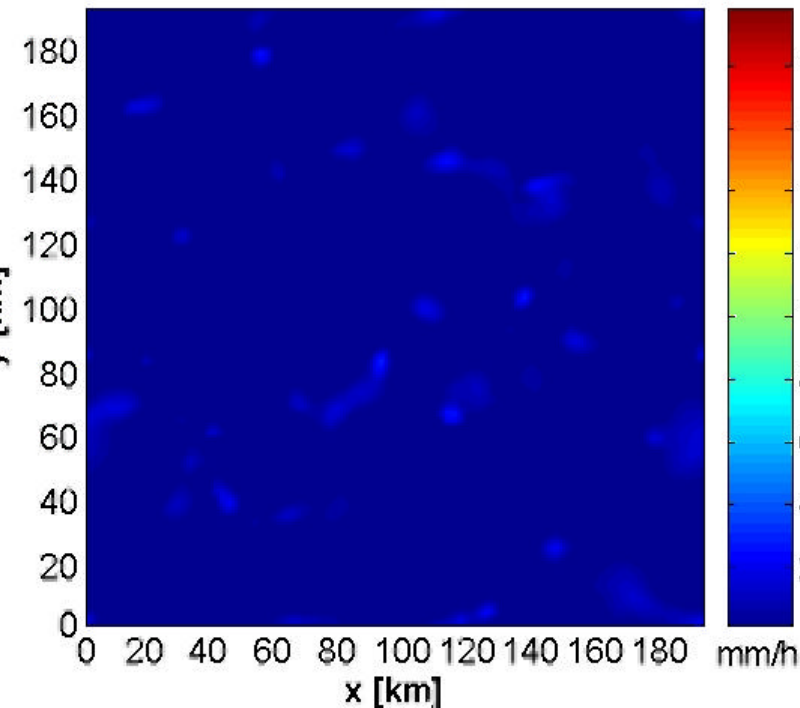
- Convective rain cell identification: first we detect local maxima of the rainfall intensity field  $R$ . We retain only those maxima in  $R$  that exceed the threshold of 30 mm/h. The horizontal extent of each rain cell is then determined by identifying the connected region around the maximum that has  $R$  larger than 0.5 mm/h;
- For each cell we use this connected region (determined in the  $R$  field) as a mask to determine the mean and standard deviation of  $w$  field in the cell at  $z=5000$  m;
- We evaluate the dependence of some statistical cell properties (mean vertical velocity, mean rainfall intensity and number of cells) on the raindrop terminal velocity

# Radiative convective equilibrium statistics:

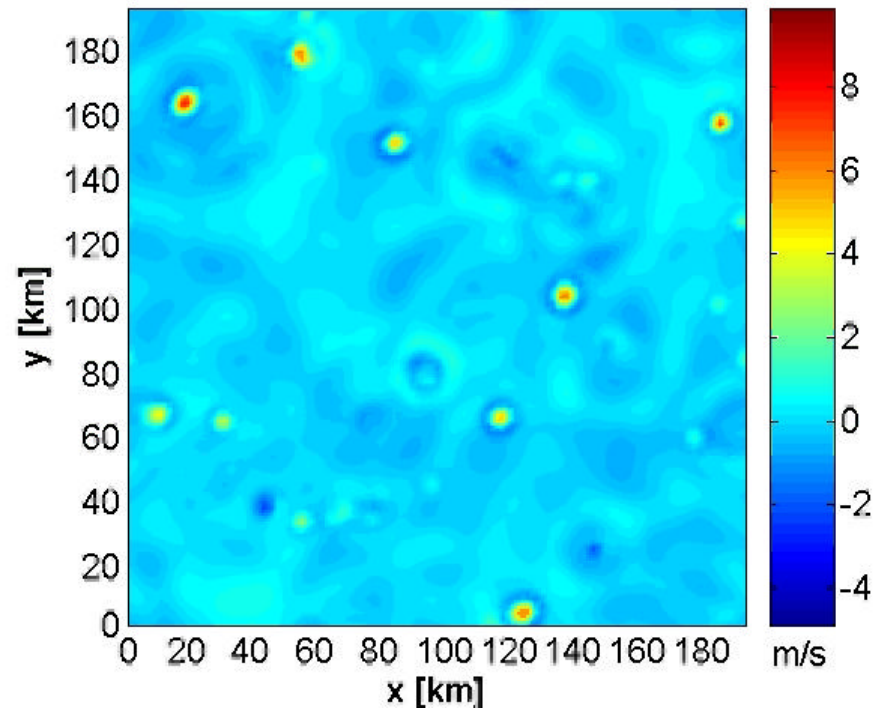
## Buoyancy and velocity scales

$Q_{\text{rad}} = -4 \text{ K/day}$ , raindrop terminal velocity  $V_T = 2 \text{ m/s}$ , domain size = 200 km

t=0



t=0



Rainfall intensity field

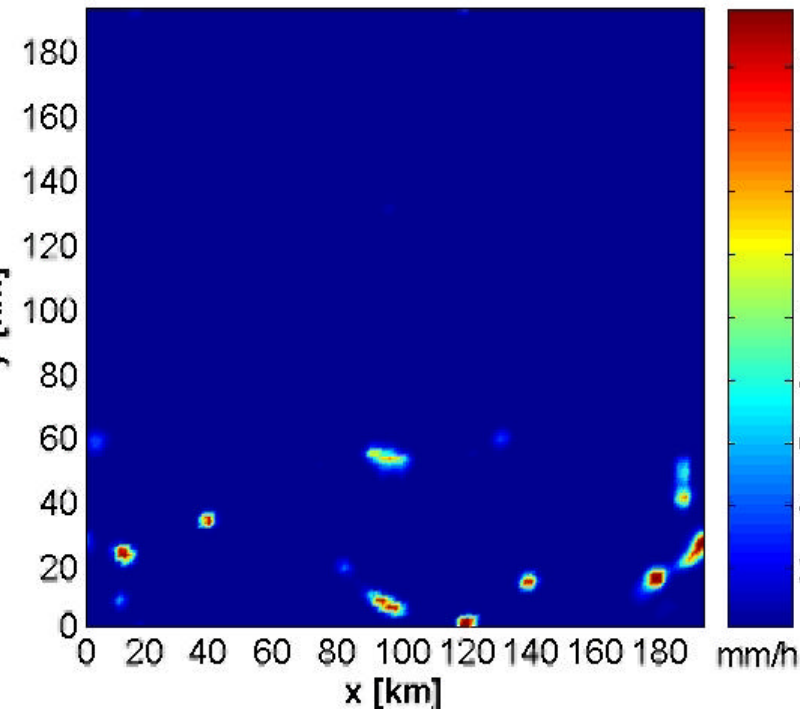
Vertical velocity field:  $z = 5000 \text{ m}$

# Radiative convective equilibrium statistics:

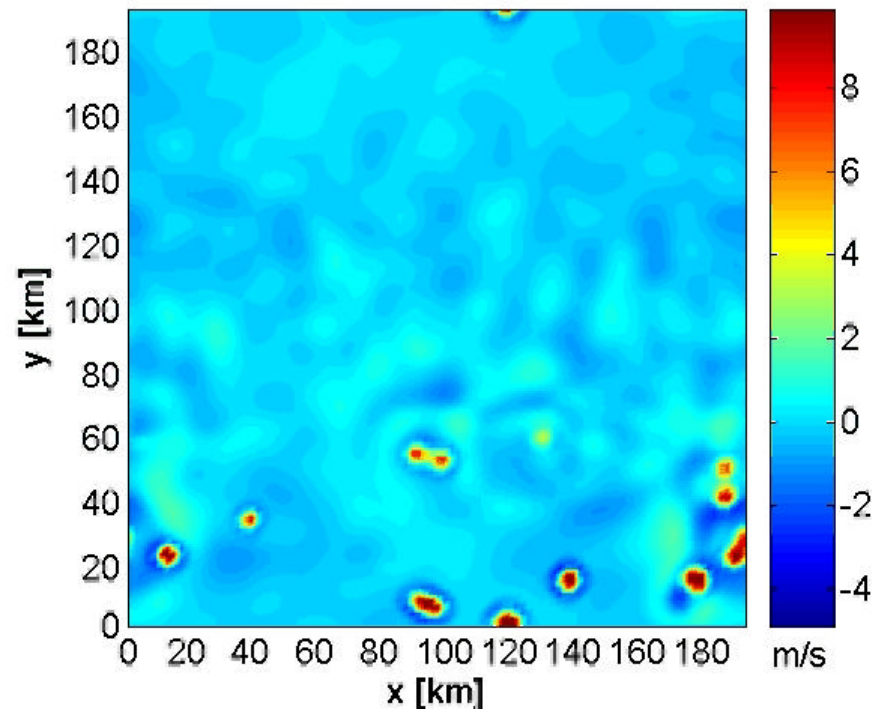
## Buoyancy and velocity scales

$Q_{\text{rad}} = -4$  K/day, raindrop terminal velocity  $V_T = 15$  m/s, domain size = 200 km

t=0



t=0



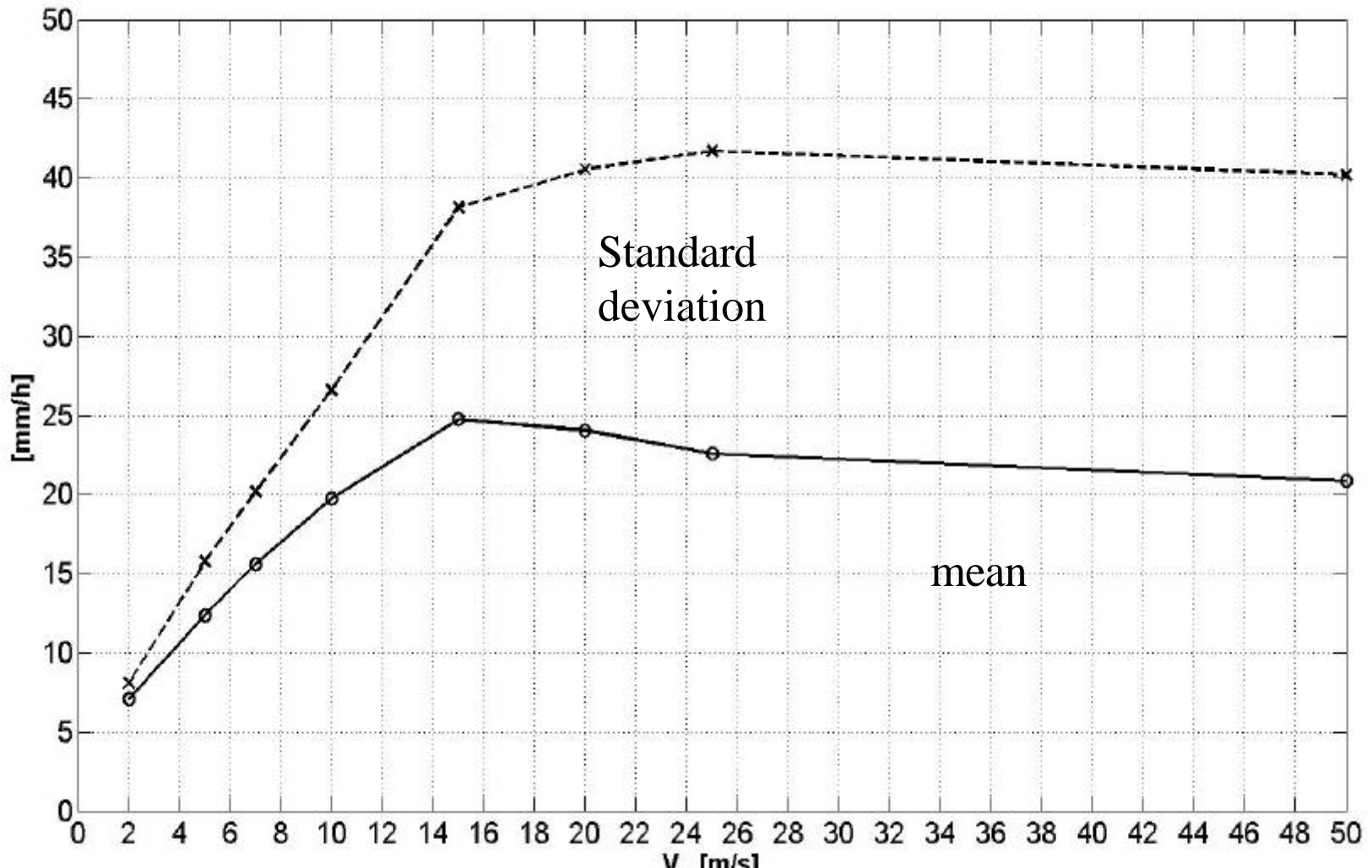
Rainfall intensity field

Vertical velocity field:  $z=5000$  m

# Radiative convective equilibrium statistics.

## Buoyancy and velocity scales

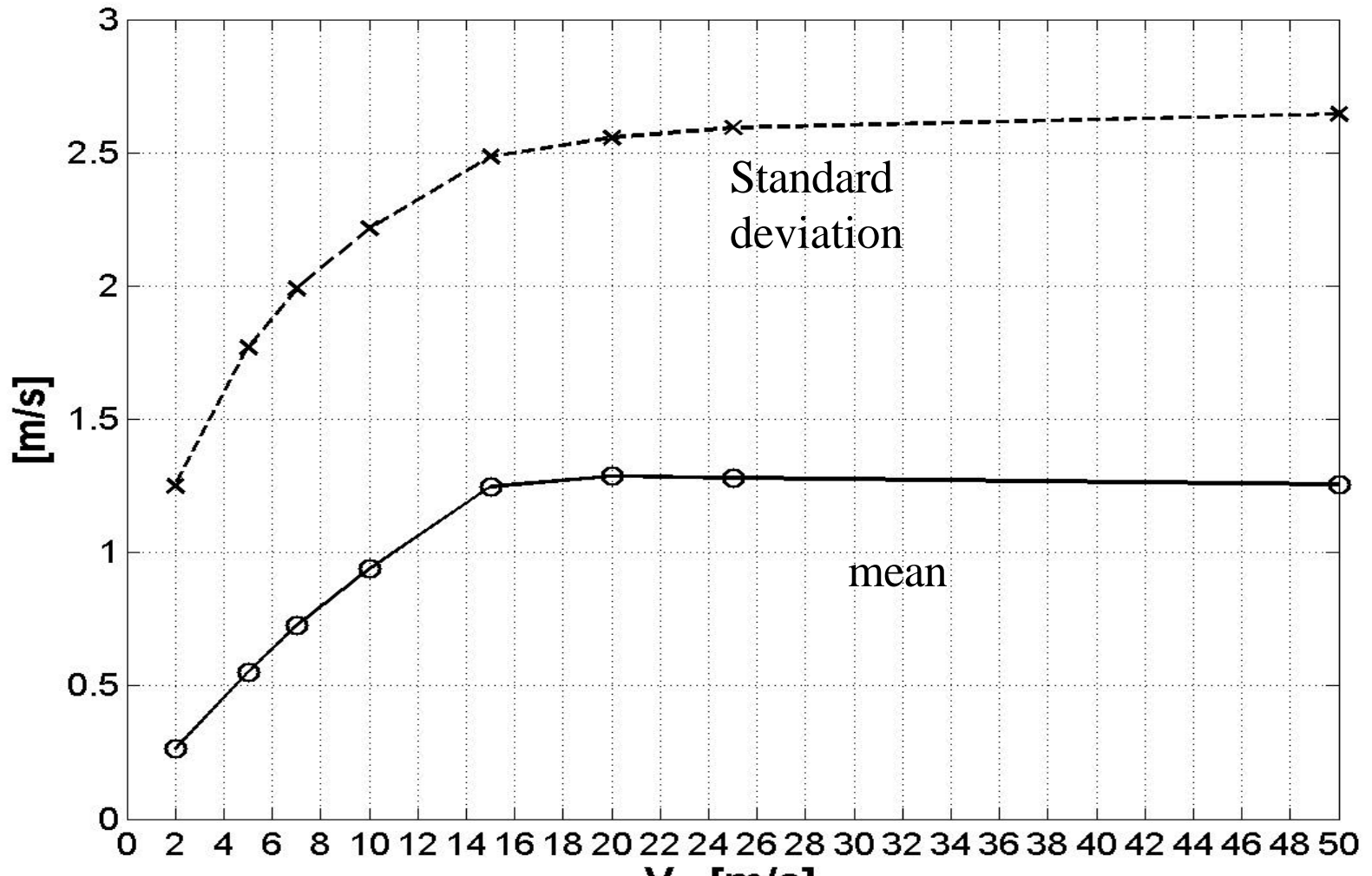
rainfall intensity scaling (over a period of 4 days in radiative convective equilibrium:  
30 frames, time resolution = 12 min)



# Radiative convective equilibrium statistics:

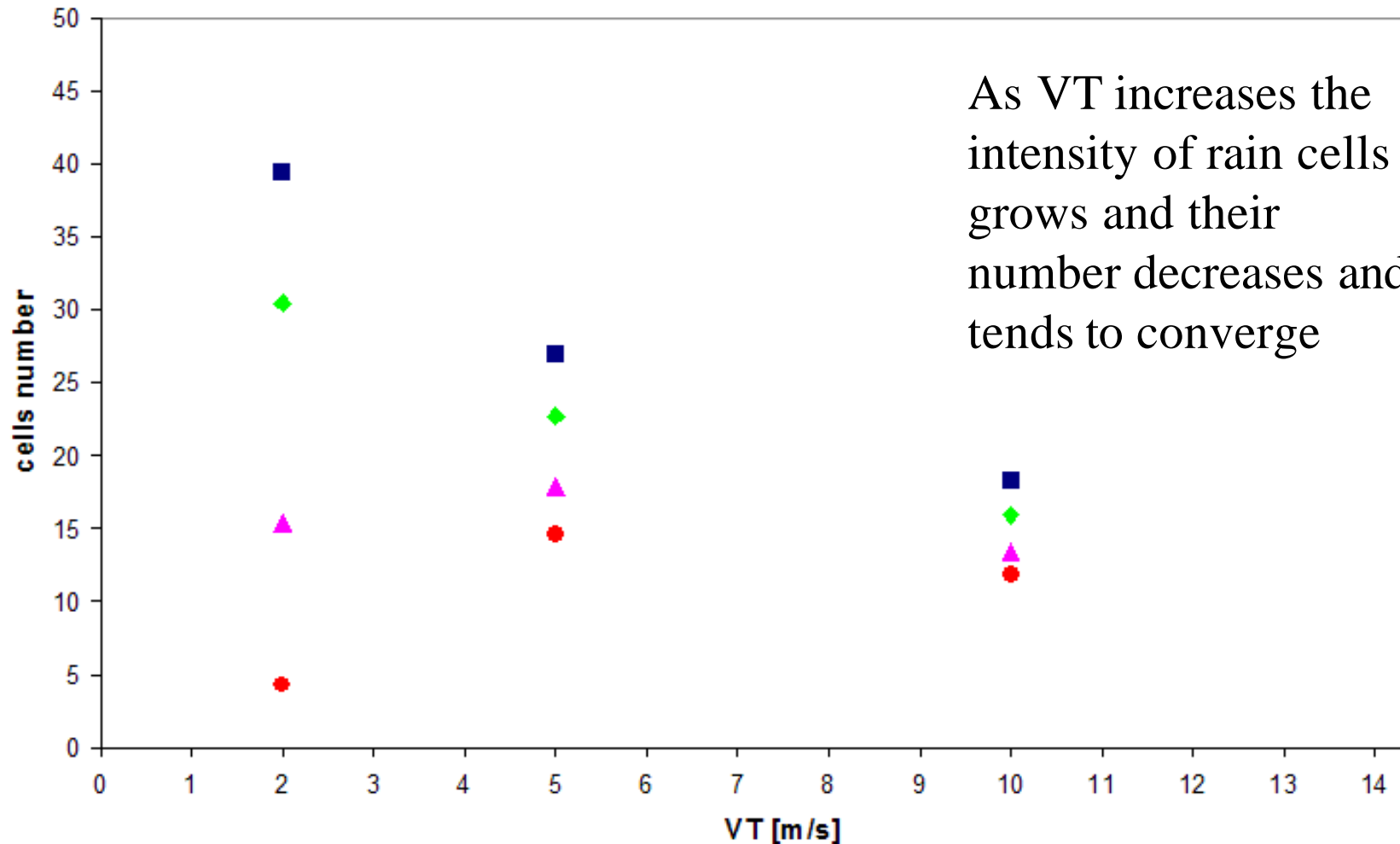
## Buoyancy and velocity scales

Vertical velocity scaling (over a period of 4 days in radiative convective equilibrium  
30 frames, time resolution= 12 min)



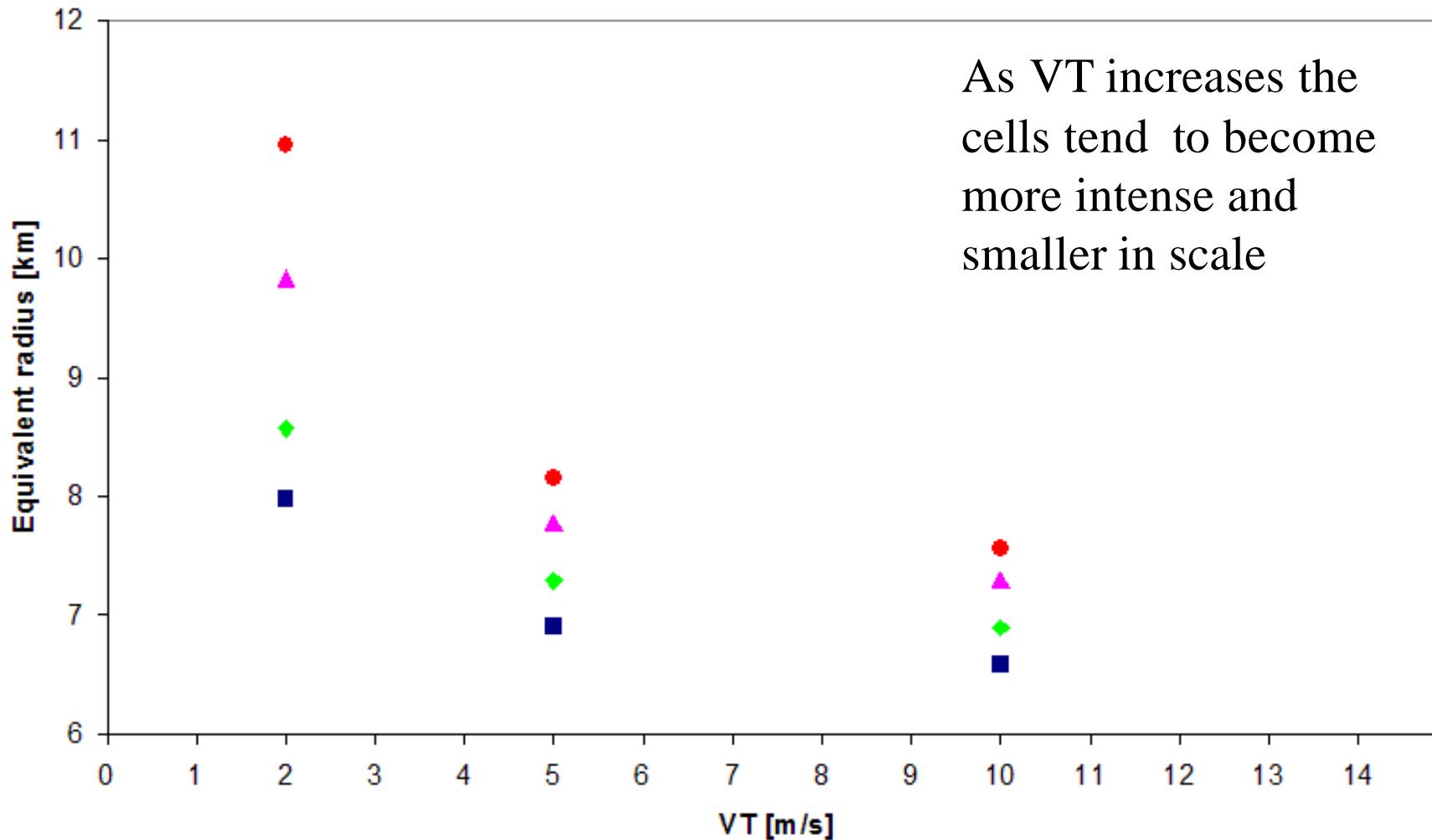
# Radiative convective equilibrium statistics: Buoyancy and velocity scales

Number of detected cells depends on the adopted threshold



# Radiative convective equilibrium statistics: Buoyancy and velocity scales

Rain cell equivalent radius depends on the adopted threshold



# Conclusions

- Buoyancy and velocity scales for moist convection in statistical equilibrium are studied;
- We find that convective updraft velocity and rainfall intensity scale with the raindrop terminal velocity;
- A minimum domain size (around  $200 \times 200 \text{ km}^2$ ) to achieve a significant convergence in the statistical properties of the moist convection is identified;
- In agreement with Grabowski (2003) and others, we find that as  $V_T$  increases the atmosphere becomes more convective and drier

# Future work

This work is in progress and the results deserve further investigation:

- It is planned to repeat the same analysis with the WRF model in order to further assess the reliability of the results and of the proposed scalings
- Evaluation of the role of other parameters: especially higher cooling rates ( e.g  $Q_{\text{rad}} = -6 \text{ K/day}$  and  $-8 \text{ K/day}$ ) and lower horizontal resolution (1 km and 500 m);
- Developing and testing a theory for this scaling.
- Use of the moist radiative convective problem to compare behaviour of different (1D and 3D) turbulence parameterizations in LM

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