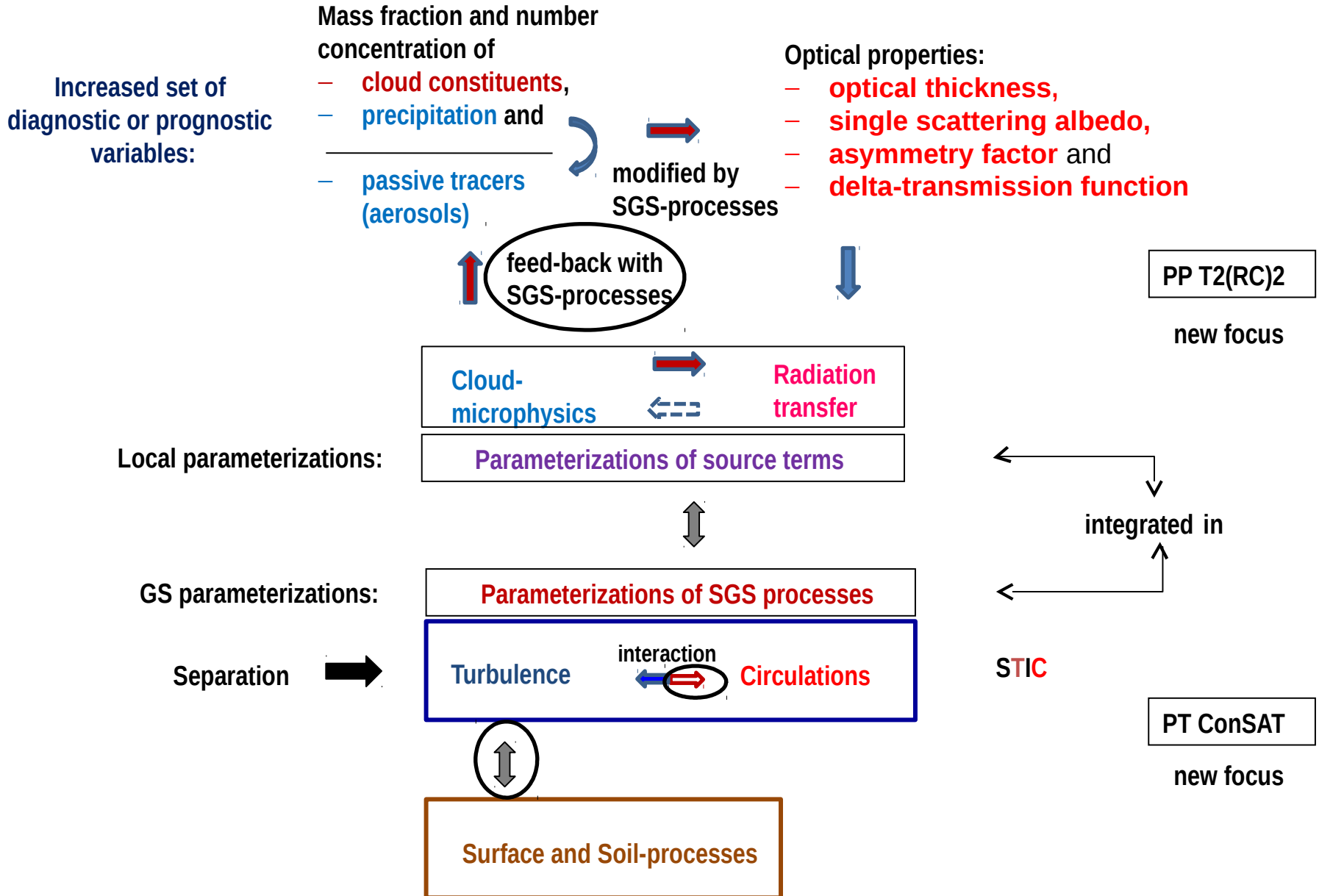


Along the aim of COSMO-SP to consider missing interactions:



Scale Interaction (STIC) and its essential effect on Surface-to-Atmosphere Transfer (SAT)

Matthias Raschendorfer, DWD

Outline:

- A lesson from previous ConSAT tasks:

- **Background-diffusion (BD)**, introduced, e.g., by **minimal diff.-coeff.**, is a substitute of missing **STIC terms** (acting due to non-turbulent heterogeneity).
- If **BD** of **non-adaptive STIC terms** are applied in the BL even above a homogeneous surface, this partly destroys the **stability reduction** of SAT-velocity.
 - too large heat-fluxes in those situations



one branch of ConSAT

- ❖ more complete **STIC-terms** being better adapted to external parameters and to the local model state
 - ❖ adapted relaxation of **hidden numerical security measures**
 - ❖ activation of **prepared extensions**
 - ❖ transfer of related ICON-development into COSMO?
- I'm explaining the idea of **STIC** and the status of current development



The filtered model equations:

$$\partial_t(\bar{\rho}\hat{\phi}_i) + \nabla \cdot \left(\overbrace{\bar{\rho}\hat{\phi}_i\hat{\mathbf{v}}}^{\text{GS flux density}} + \underbrace{\overline{\rho\phi_i\mathbf{v}} - k^{\phi_i}\nabla\hat{\phi}_i}_{\text{SGS flux density}} \right) + \nabla \cdot \left(\overbrace{\rho\phi_i\mathbf{v} - k^{\phi_i}\nabla\phi_i}_{\text{roughness layer modification of transport}} \right) = \overbrace{Q_{\lambda}^{\phi_i}(\hat{\phi}, \bar{p})}^{\text{non-linear function}} + \underbrace{\overline{Q_{\lambda}^{\phi_i}(\phi, p)}}_{\text{SGS source term including roughness layer effects (form drag)}}$$

$$\overline{Q_{\lambda}^{v_i}(\phi, p)} = -\overline{\partial_i p'}$$

form drag non-commutability of filter and spatial differentiation → contribution by SGS slopes of model layers or non-atmospheric intersections

$$\overline{Q_{\lambda}^{q_k}(\phi, p)}$$

SGS contribution by cloud microphysics

$$\overline{Q_{\lambda}^T(\phi, p)}$$

SGS contribution by cloud microphysics and radiation

functions in various **covariance terms of scalar variables**

$\underline{\phi}$: vector of all 1st-order prognostic model variables

$$\bar{p} = \bar{\rho} R_d \mathbf{1} + \left(\frac{R_v}{R_d} - \mathbf{1} \right) \overline{q_v} - \overline{q_c} \bar{T} + R_d \mathbf{1} + \left(\frac{R_v}{R_d} - \mathbf{1} \right) \overline{\rho q_v T} - \overline{\rho q_c T}$$

$\bar{\zeta}$: grid-scale filtered (mean) variable with fluctuation $\zeta' = \zeta - \bar{\zeta}$

$\hat{\zeta} = \frac{\bar{\rho}\zeta}{\bar{\rho}}$: corresponding density weighted mean with fluctuation $\zeta' = \zeta - \hat{\zeta}$

2nd-order (SO) budgets:

$\phi, \psi \dots \in \{ \phi_1, \phi_2, \dots \}$ prognostic model variables

influenced by pressure force,
microphysics and radiation



$$\partial_t (\overline{\rho \phi \psi}) = - \nabla \cdot (\overline{\rho \phi \psi} \hat{\mathbf{v}} + \overline{\rho \phi \psi} \mathbf{v}) - (\overline{\rho \psi} \mathbf{v} \cdot \nabla \hat{\phi} + \overline{\rho \phi} \mathbf{v} \cdot \nabla \hat{\psi}) + (\overline{\mathbf{e}^\psi} \cdot \nabla \phi + \overline{\mathbf{e}^\phi} \cdot \nabla \psi) + \boxed{\overline{\phi Q^\psi} + \overline{\psi Q^\phi}}$$

GS flux density

SGS flux density

shear production

dissipation sink

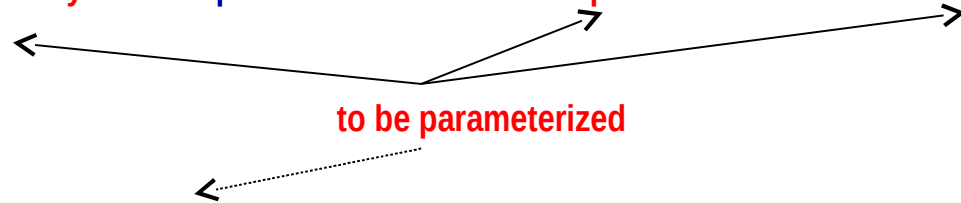
source term correlation

+ . . .

to be parameterized

laminar
transport

roughness layer
modification of
transport



Parameterizations in terms of grid scale (GS) variables :

- Further information (**assumptions**) about these **additional covariance terms** has to be introduced:

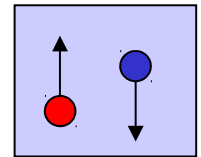
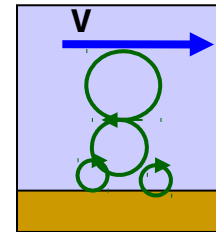
functions in all GS model variables $\bar{\rho}, \hat{\phi}, \bar{p}$ } **GS parameterizations due to**
 dependent on a list of additional **parameters** $\underline{\beta}$ } **- SGS variability**

- Closure assumptions are **additional constraints** that can't be general valid

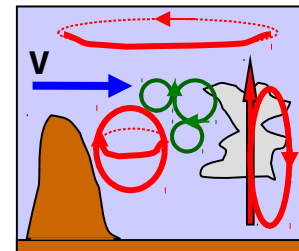
➤ distinguish **different SGS flow structures** more or less according to the **length scales of their motions**

➤ each with **specific parameterization assumptions**

Turbulence: isotropic, normal distributed, only one characteristic **length scale** at each grid point, forced by **shear and buoyancy**



SGS Circulation: non isotropic, arbitrarily skewed and coherent structures of several length scales, supplied by **various pressure forces**



Convection large vertical scales of coherence, full microphysics, forced by buoyancy feed back

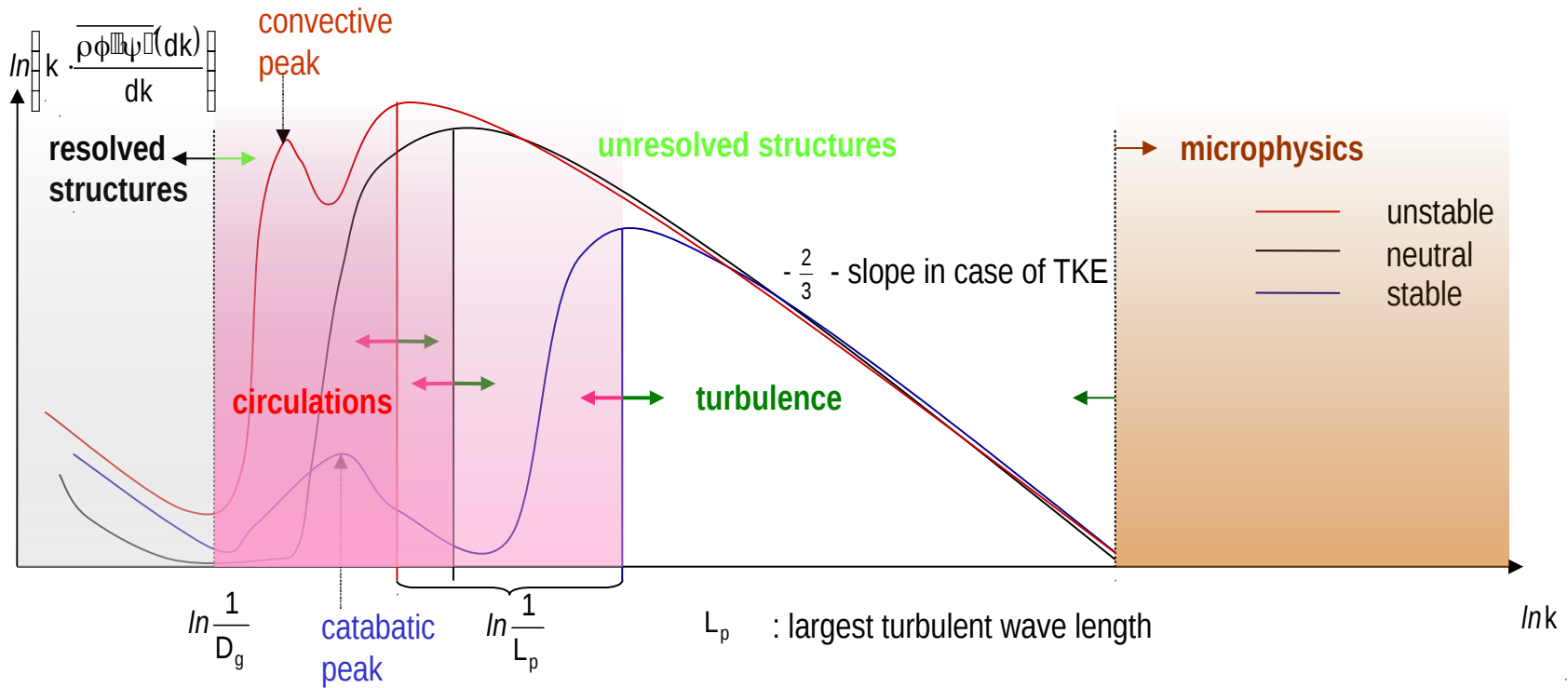
Kata- and anabatic density circulations: direct thermal circulation forced by lateral cooling or heating by sloped surfaces of the earth; dominated by SGS surface structures like SSO

Horizontal shear eddies: produced by strong horizontal shear e.g. at frontal zones; dominated by horizontal grid scale

Wake eddies: produced by blocking at SGS surface structures (form drag forces)

Breaking gravity wave eddies: belong to wave length of instable gravity waves of arbitrary scales

Spectral characteristics of turbulence and circulations:



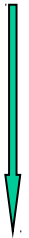
- **circulations** generally are related with **additional spectral peaks**

- or they cause **different peak wavelengths** in **vertical** direction compared to the **horizontal** directions:

- **larger** peak wavelength in **vertical** direction in case of **unstable** stratification
- **smaller** peak wavelength in **vertical** direction in case of **stable** stratification

anisotropic peak wave length

- at least a **two-scale-problem**
- **different closure assumptions** for turbulence and circulations



The TKE-scheme including empirical parameterization extensions:

Matthias Raschendorfer

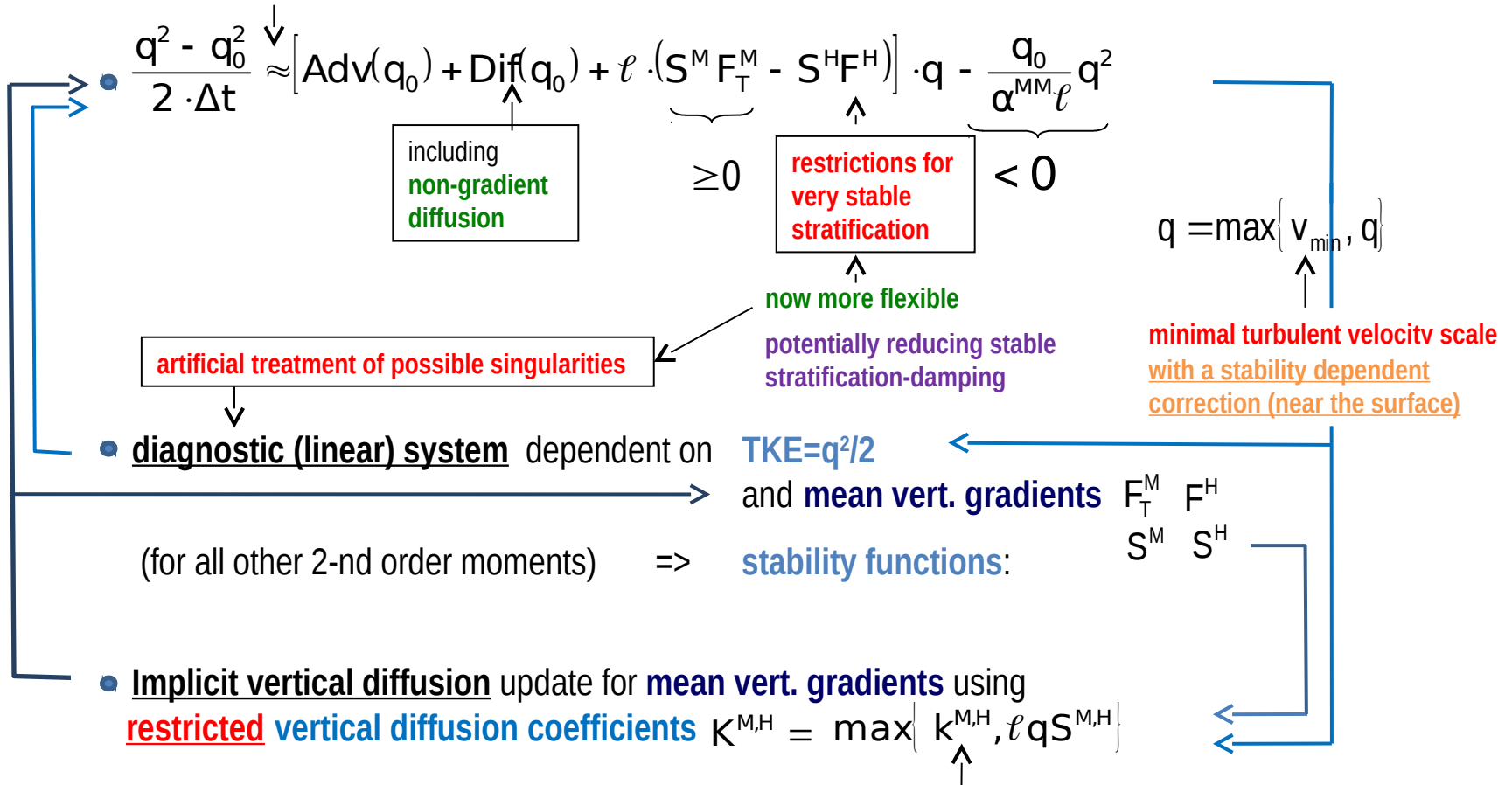
Günther Zängl (DWD)

o TKE vanishes at stable stratification and vanishing vertical shear

- Unrealistic decouple of surface and boundary layer
- Missing stratospheric turbulence

❖ artificial limitations and empirical extensions are necessary

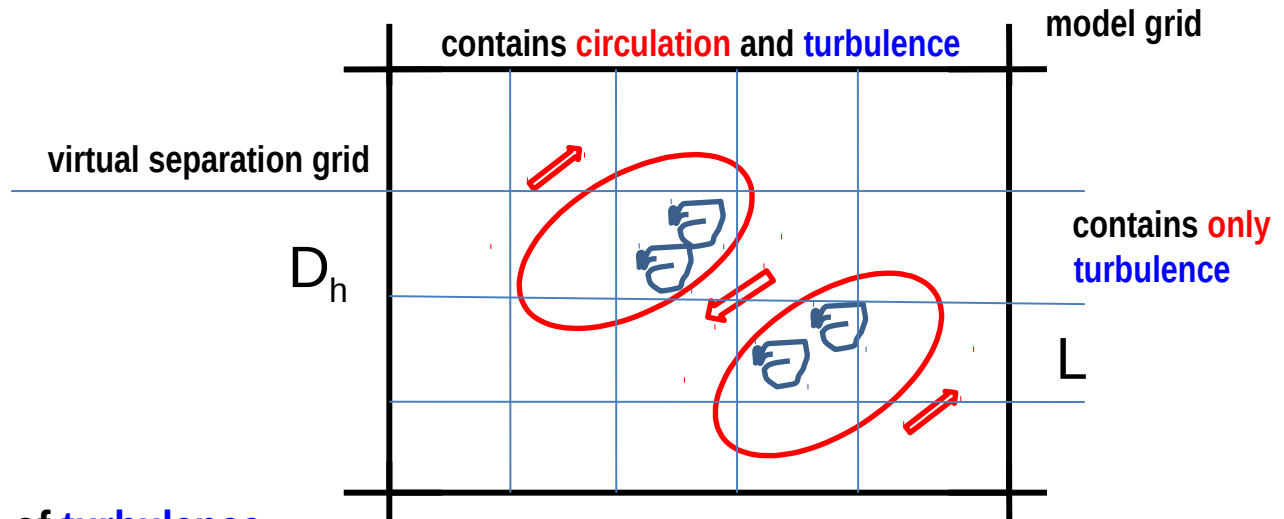
with optional positive definite solution of prognostic TKE-equation and optional vertical smoothing of F_T^M F^H



Current realization:

- We usually apply parameterizations of effects on 1-st order budgets due to different processes (turbulence, convection, SSO wakes) without using a clear separation procedure
 - Each scheme for a specific SGS process would only be valid, if all the other sub grid scale processes were in accordance with the specific closure assumptions, what is in CONTRADICTION to the need of DIFFERENT SGS models!!
- This missing separation causes serious problems:
 - **Non-realizability** due to the application of not valid assumptions
 - **Double-counting** of effects from different scale regimes
 - **Missing feedback** between different scale regimes
 - **No amplification of turbulence due to the action of circulations**
 - **No decrease of Circulation Kinetic Energy (CKE) by turbulent friction**
 - **No trigger of convective circulations by turbulent eddies**
 -

Separated Turbulence Interacting with non-turbulent Circulations (STIC):



➤ 3D-shear production of turbulence

- From the grid-scale flow
- From non-turbulent sub-grid flow patterns (**circulations**)
 - Connected with **coherent structures** being not in accordance with turbulence closure
 - Will be expressed by grid-scale 3D shear, if the patterns are resolved by a **smaller grid**
 - Extracts kinetic energy from the **circulation** flow and feeds **turbulence**

The procedure of STIC:

- Assume that **turbulence approximations** can be assigned to all horizontal scales not smaller than a maximal turbulent length scale L_p (mainly dependent on the distance from the surface)
- **Spectral separation** by
 - considering **budgets** with respect to the **separation scale** $L = \min\{L_p, D_g\}$
 - **averaging** these budgets along the **whole control volume** (double averaging)

- **1-st order budgets with SGS contributions from turbulence and circulations**

$$\overline{\rho\phi\psi} = \overline{\rho\hat{\phi}\hat{\psi}} + \overline{\rho\phi\psi}|_L + \overline{\rho\phi\psi}|_L \quad |_L$$

: with respect to the separation scale L

- Two sets of 2-nd order equations containing additional **scale interaction terms**:
one set for **pure turbulence** and another for **pure circulations**



Mass flux equations describing initial conditions and lateral mixing of cells using properties of turbulence

Separated TKE equation contains additional shear term:

- Semi-parameterized (neglecting laminar transport and roughness layer modification of transport)

$$2 \cdot \text{TKE} := q^2 := \frac{\overline{\rho_{|L} q_{|L}^2}}{\bar{\rho}}$$

$$q_C^2 := q_{|L}^2 := \frac{1}{\bar{\rho}_{|L}} \sum_{i=1}^3 \overline{\rho v_i^2} \Big|_L$$

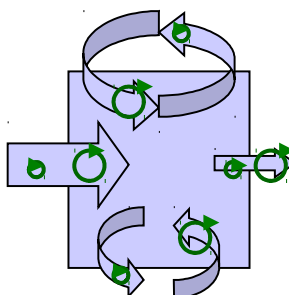
$|_L$: with respect to the separation scale L

not yet considered

$$\partial_t \left[\frac{1}{2} \bar{\rho} \cdot q^2 \right] = \frac{1}{2} \nabla \cdot \left[\bar{\rho} q^2 \hat{v} + \hat{\rho}_{|L} q_{|L}^2 \hat{v}_{|L} + \sum_{i=1}^3 \overline{\rho v_i^2 v_i} \Big|_L \right] + \frac{g}{\hat{\theta}_v} \overline{\rho \theta \Psi w} \Big|_L + \left[- \sum_{i=1}^3 \overline{\rho v_i v_i v_i} \Big|_L \cdot \nabla \hat{v}_i \right] + \left[- \sum_{i=1}^3 \overline{\rho v_i v_i v_i} \Big|_L \cdot (\nabla \hat{v}_i) \Big|_L \right] + \left[- \bar{\rho} \frac{q^3}{\alpha^{MM} \ell} \right]$$

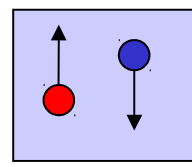
time tendency

transport:
(advection
+ circ. diffusion
+ turb. diffusion)



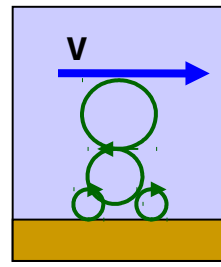
buoyancy production

labil: > 0
neutral: = 0
stabil: < 0



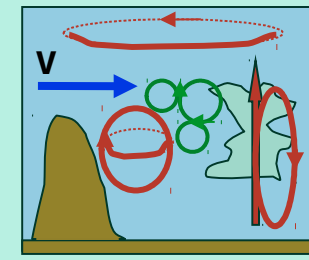
shear production by the mean flow

≥ 0



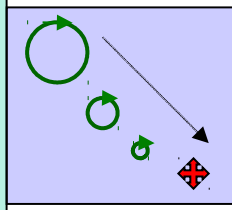
shear production by sub grid scale circulations

≥ 0

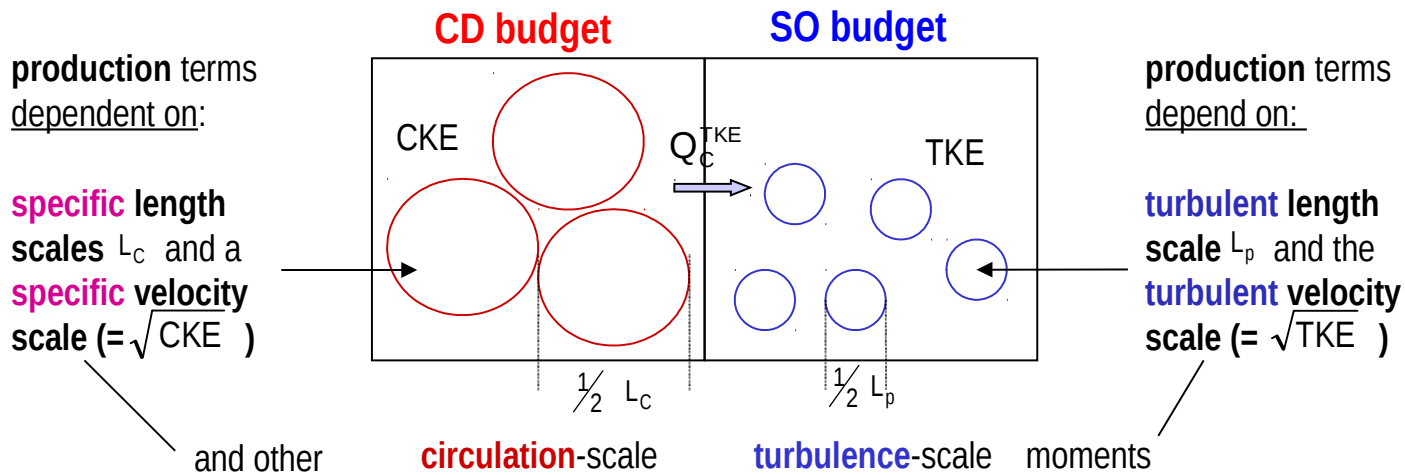


eddy-dissipation rate (EDR)

< 0



Towards a description of TKE-production by sub-grid circulations (SI-term):



- **Simplified CD budget: Equilibrium of production and scale transfer towards turbulence:**

$$Q_C^{TKE}(q_C) \propto \frac{q_C^3}{L_C}$$

L_C **length scale** of the circulation

α_C **effective** scaling parameter

kinetic energy production of the circulation

→ **solving for** q_C **velocity scale** of the circulation

Current work on STIC:

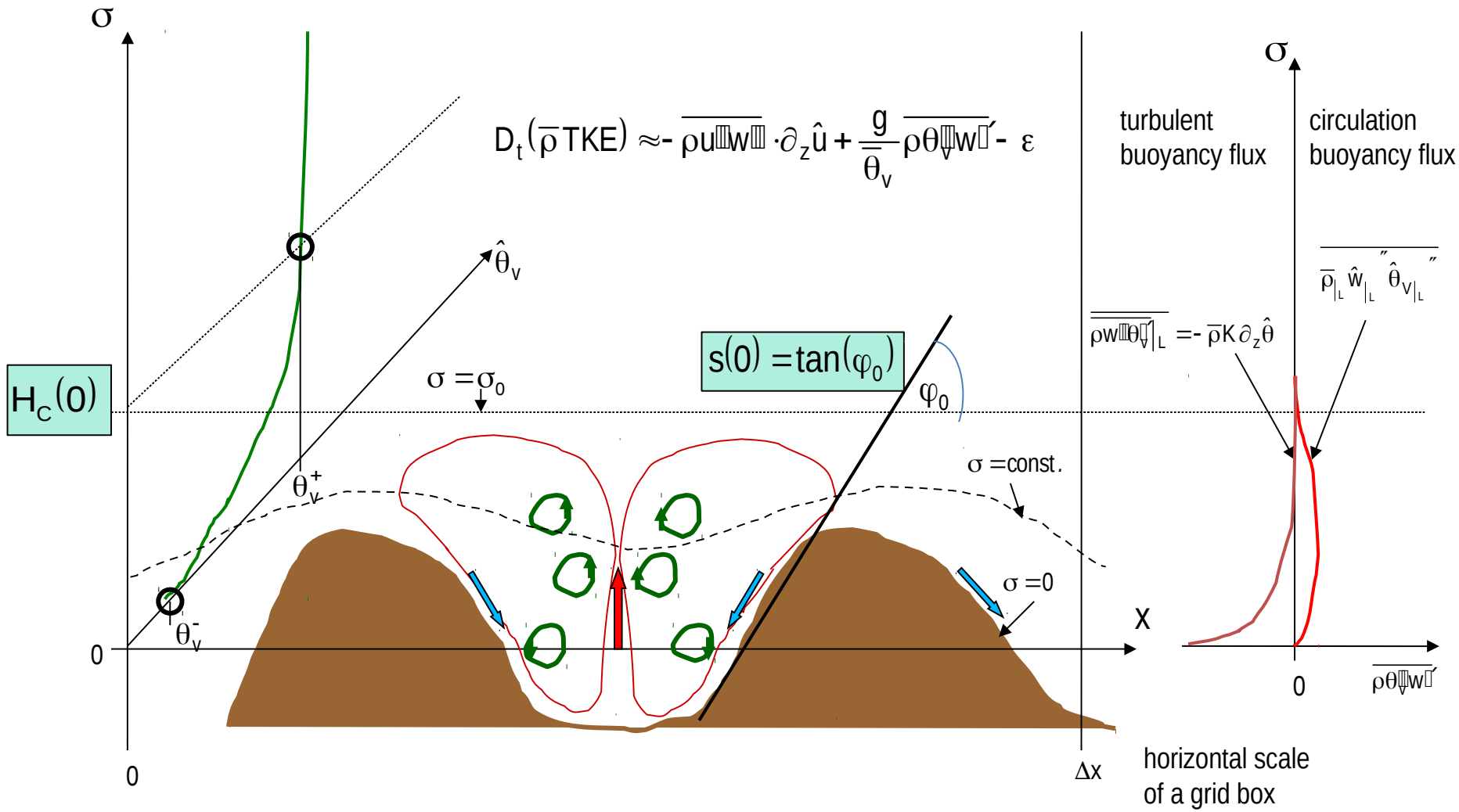
- dTKeshs □ “more realistic generalization”
 - ✓ SI dependent on thermal stability and height above ground
 - formulation SI-sink in CKE-budget of SHS-circulation also dependent on turbulent velocity scale.
 - ✓ new formulation in preparation

- dTKEncv □ “to be used not only for EDP-post-processing”
 - Operational use in prognostic TKE-equation
 - removing sources of **detrimental jumps in space and time**
 - Introduction of turbulence-feedback into **convection-scheme**
 - formulation of **detrainment/entrainment** also dependent on turbulent velocity scale
 - **trigger of SGS convective plumes by turbulent vertical velocity**
 - ✓ publications about EDP running
 - derivation and validation

- dTKEss0 □ “empirical modifications”
 - ✓ SI with correction factor dependent on thermal stability
 - ✓ Introduced by Günther Z.

- dTKEcrc □ “thermal SSO-term”
 - nocturnal katabatic down-valley circulation
 - daytime convective up-valley circulation
 - ✓ dependent on SSO-parameters (vanishing for a flat surface)
 - **Thermal surface inhomogeneity** □ **surface-forcing of SGS convection**
 - ✓ new formulation being tested
 - substituting the current “circulation-term”

Effect of a sub-grid katabatic circulation for stable stratification:



• Even for **vanishing mean wind** and **negative turbulent buoyancy** there remains a **positive definite source term**

- ➡ TKE will **not** vanish
- ➡ Solution even for **strong stability**

TKE-production by sub-grid circulations:

- Equilibrium of **production** and **spectral transfer towards turbulence**:

$$g \frac{\Delta \bar{\theta}_v}{\bar{\theta}_v} \sin(\varphi) \cdot q_c \approx Q_C^{\text{TKE}} \propto \frac{q_c^3}{L_c}$$

$$H_c(\sigma) \approx \max\{0, H_c(0) - \sigma\}$$

mean height-amplitude of a σ -surface

$$\tan[\varphi(\sigma)] = s(\sigma) \approx s(0) \cdot \frac{H_c(\sigma)}{H_c(0)}$$

mean slope of a σ -surface

$$L_c = \frac{H_c}{\sin(\varphi)}$$

coherence-length along the σ -slope

$$\Delta \bar{\theta}_v \approx \left| \partial_z \bar{\theta}_v \right| \cdot H_c$$

effective temperature difference

q_c may trigger convection

$$F^H = \frac{g}{\bar{\theta}_v} \partial_z \bar{\theta}_v \left\{ \begin{array}{l} <0: \text{anabatic} \\ >0: \text{katabatic} \end{array} \right.$$

q_c ventilates the SBL

$$Q_C^{\text{TKE}} \approx \alpha_c \frac{(s \cdot H_c)^2}{1 + s^2} \left| F^H \right|^{\frac{3}{2}}$$

resulting TKE-production

$H_c(0)$
 $s(0)$ } external 2D SSO-parameter

α_c } effective scaling parameter

Direct STIC-impact on SAT:

In TURBTRAN, the SAT-resistance has two contributions:

- Roughness-layer resistance with a laminar and a turbulent part (only for scalars):

$$r_{S0}^H = \frac{1}{\kappa S_0} \left[\lambda^H + \ln \frac{\kappa Z_0 u_0^H}{k^H} \right] = \frac{1}{\kappa u_0^H} \ln \frac{Z_0}{Z_0^H}$$

- Turbulent Prandtl-layer resistance with an unstable and a stable branch:

$$y_s^\phi := \frac{z_0}{h_p} \left[\frac{u_p^\phi}{u_0^\phi} \right]^s - 1 \quad s = \begin{cases} 1 & \text{unstable} \\ -1 & \text{stable} \end{cases} \quad \phi \in \{H, M\} \quad u_x^\phi := \frac{\kappa x}{\ell} \quad \text{turbulent velocity}$$

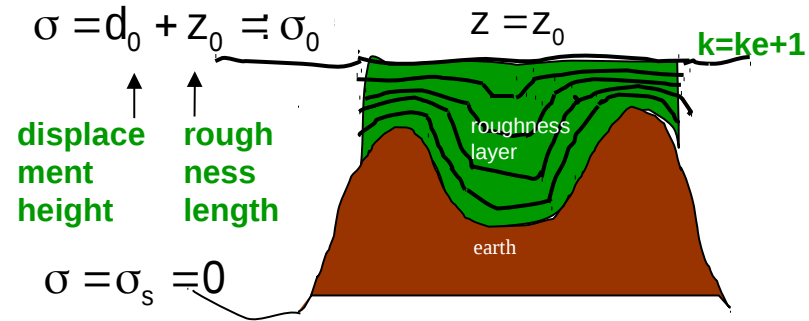
$$r_{0A}^\phi = \frac{1}{\kappa} \int_{\ell_0}^{\ell_A} \frac{d\ell}{\ell \cdot u^H} = \frac{1}{\kappa u_0^\phi} \left[\frac{1}{1 - \gamma_1^\phi} \ln \frac{Z_A}{Z_0 + \gamma_1^\phi \cdot h_A} - \frac{\gamma_1^\phi \rightarrow 0 \text{ (neutral)}}{\gamma_1^\phi} \ln \frac{Z_A}{Z_0} \right] \begin{cases} u_p^\phi \geq u_0^\phi & \text{(unstable)} \\ u_p^\phi < u_0^\phi & \text{(stable)} \end{cases}$$

operationally deactivated

$$u_{SA}^\phi := \frac{1}{r_{S0}^\phi + r_{0A}^\phi} \quad \text{transfer velocity}$$

$$SHF_S = \bar{\rho}_S u_{SA}^H \cdot c_{p,d} (\hat{\theta}_A - \hat{T}_S)$$

$$LHF_S = \bar{\rho}_S u_{SA}^H \cdot L_{ev} (\hat{q}_{vA} - \hat{q}_{vS})$$



k=ke-1

Z = Z_p

k=ke

Z = Z_A

k=ke+1

Z = Z₀

$$\sigma = d_0 + z_0 = \sigma_0$$

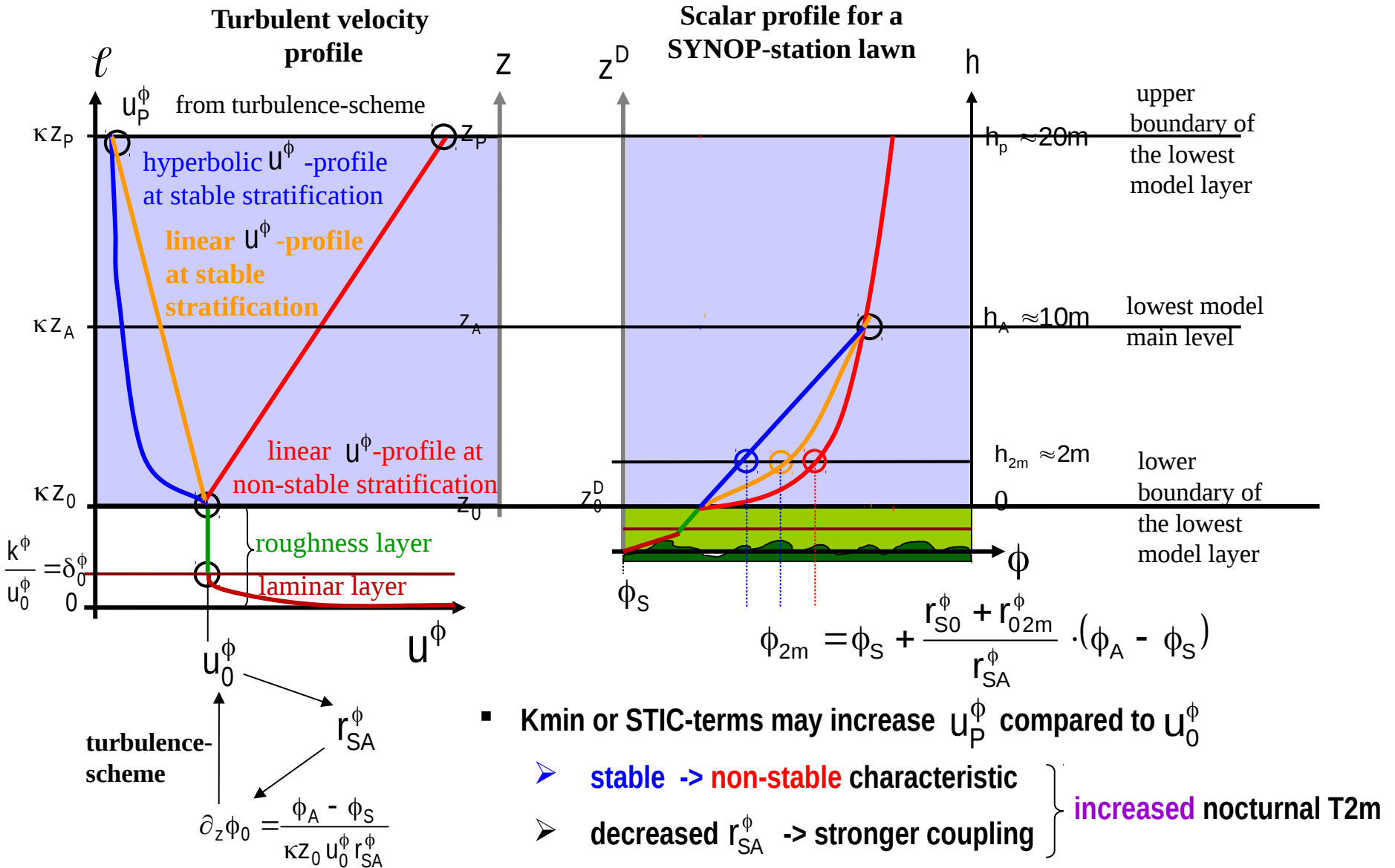
displacement height
roughness length

roughness layer

earth

$$\sigma = \sigma_s = 0$$

STIC-effect of the Profile-Function on near-surface values:



General STIC-Impact on SAT:

- Increased shear lowers Ri-number at stable stratification within the ABL and enters the calculation of stability functions
 - Avoids singularities of the solution
 - Substitutes the introduction of artificial “long-tale” stability functions

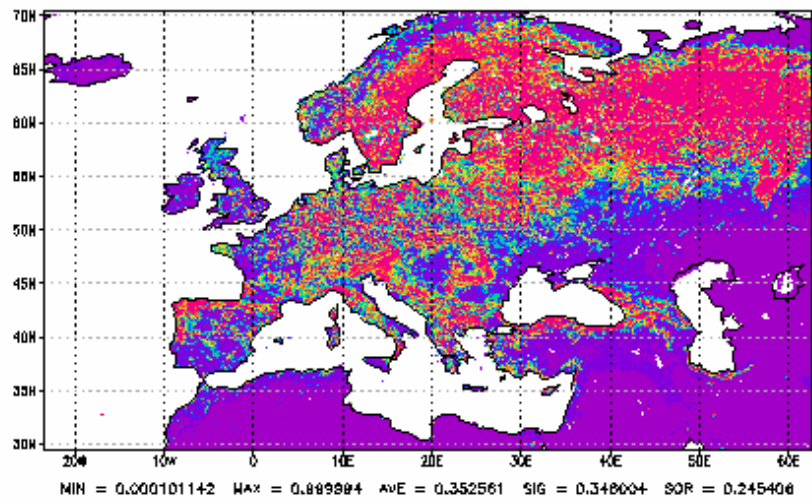
- Has a direct impact on transfer-velocities
 - Due to the adapted construction of the transfer scheme
 - solving TKE-equations at the roughness-layer top and the next higher half-level, where at least the latter can receive an impact by STIC-terms

- Generates additional physically based turbulent mixing
 - avoids unrealistic decoupling of a heterogeneous surface from the atmosphere
 - Substitutes (at least partly) the introduction of artificial minimal diffusion coefficients

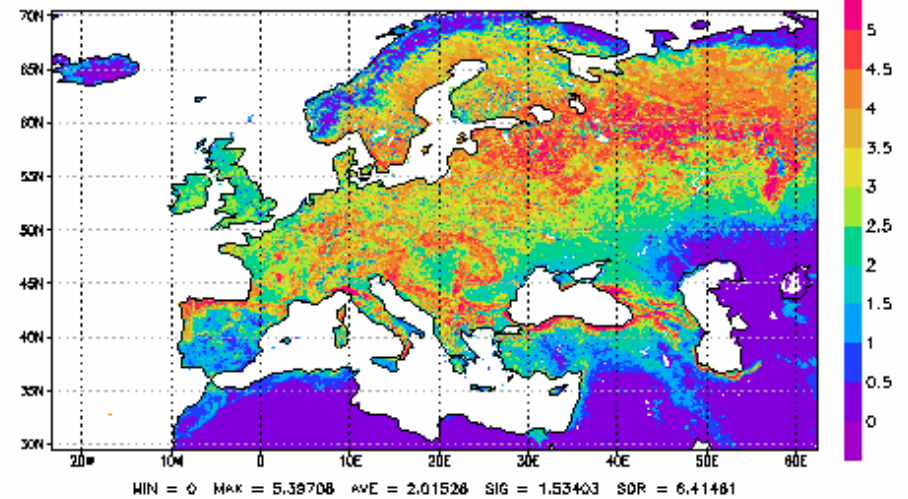
A case-study:

- **An almost clear-sky mid-summer night with ICON-EU**

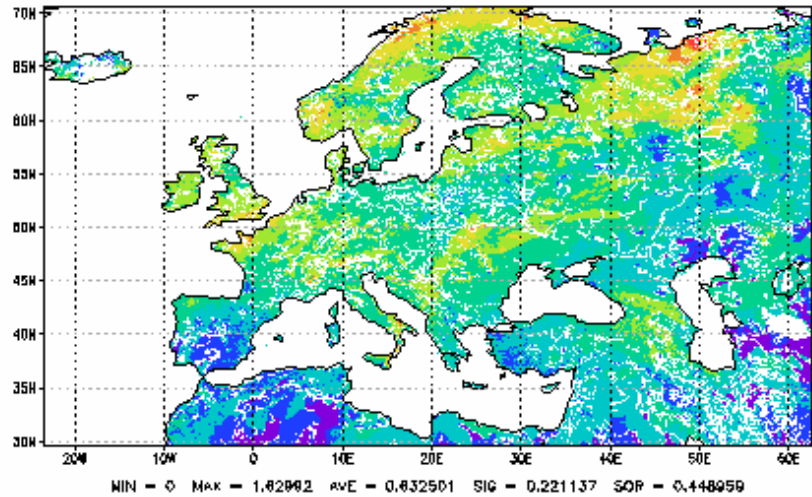
surface roughness [m] (over land) (out_ic02-imp1-new_srf_cpl-tkmin=0.0)



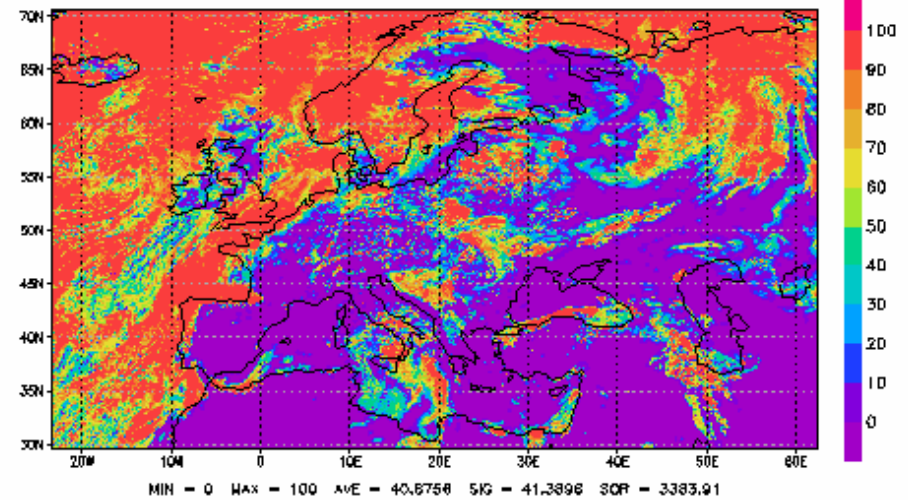
transpiration area index (over land) (out_ic02-imp1-new_srf_cpl-tkmin=0.0)



soil water fraction of field capacity [FCF] Lev.005 (out_ic02-imp1-new_srf_cpl-tkmin=0.0)



low- and mid level cloud cover in % (out_ic02-imp1-new_srf_cpl-tkmin=0.0)



or time=03Z23JUN2016 or hour=3hr

Effect of thermal SSO term:

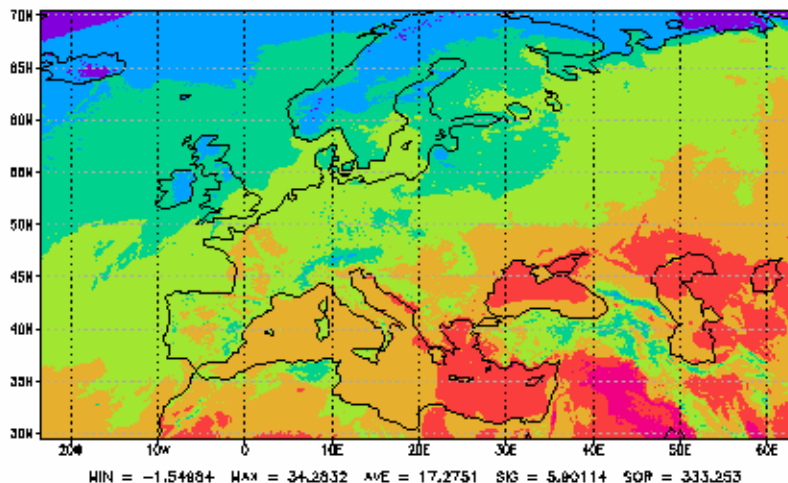
- **Right correction for hilly surfaces**
 - **reduces negative nocturnal T2m-bias**

- **No effect at flat terrain**
 - where only an decreased Kmin can lower the already **present positive nocturnal T2m-bias**

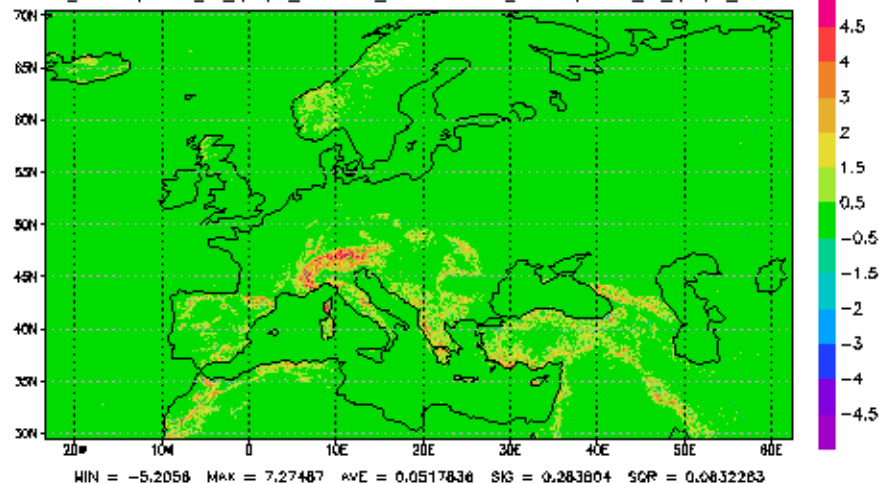
2m-temperature [C]

Nocturnal effect of new SI-term from thermal SSO

ana_ice rout

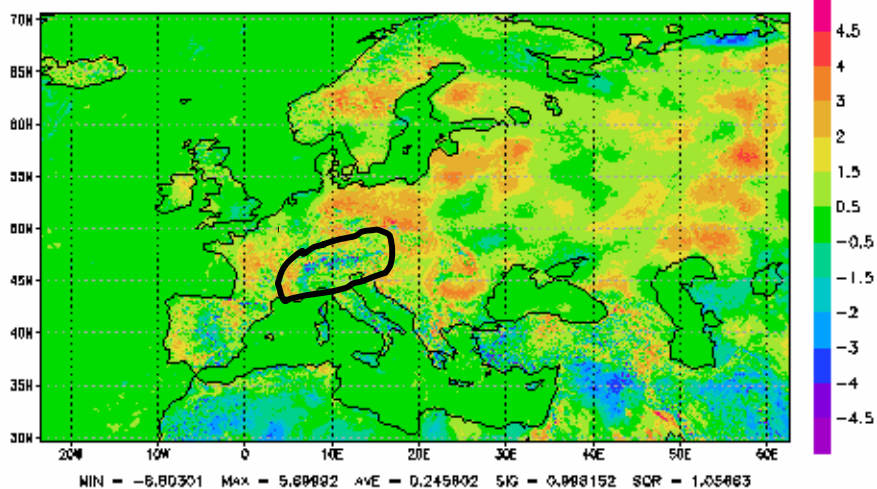


out_ic02-imp1-new_srf_cpl-pat_len=0.0-a_hssso=1.0 - out_ic02-imp1-new_srf_cpl-pat_len=0.0



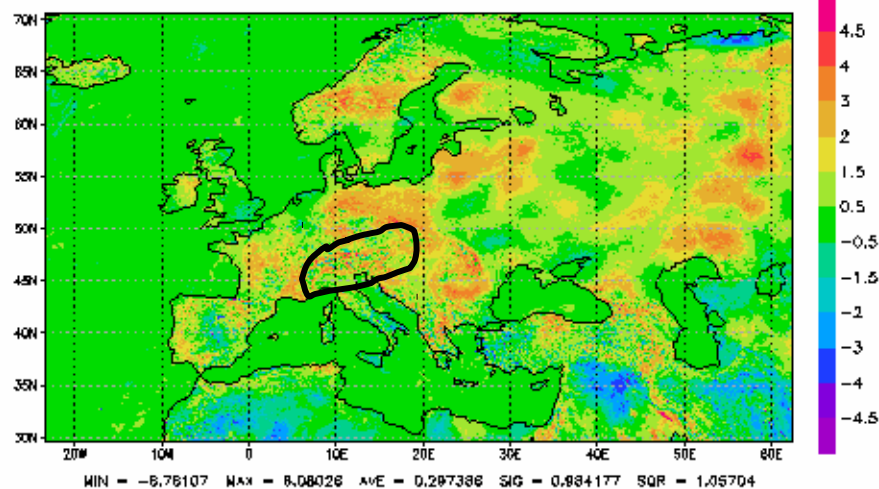
no thermal circulation term at all

out_ic02-imp1-new_srf_cpl-pat_len=0.0 - ana_ice rout



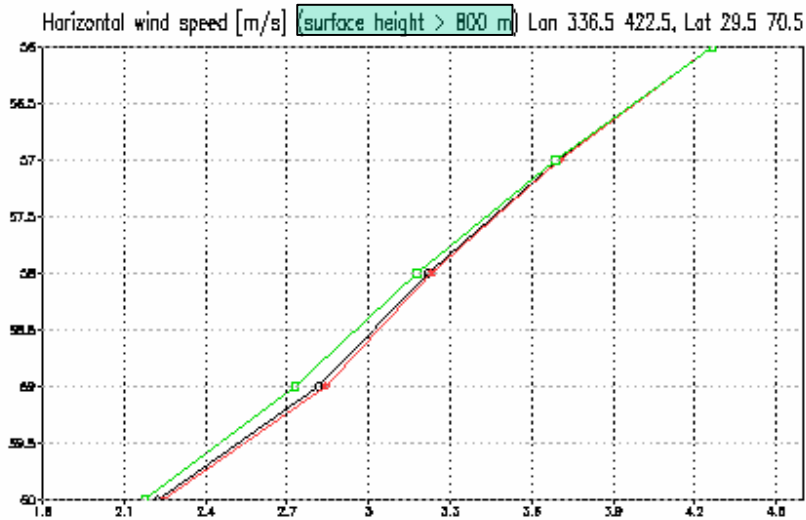
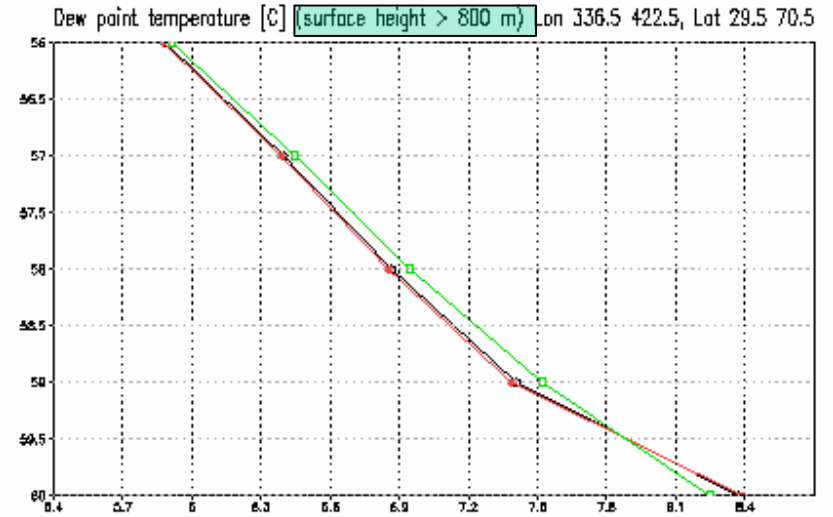
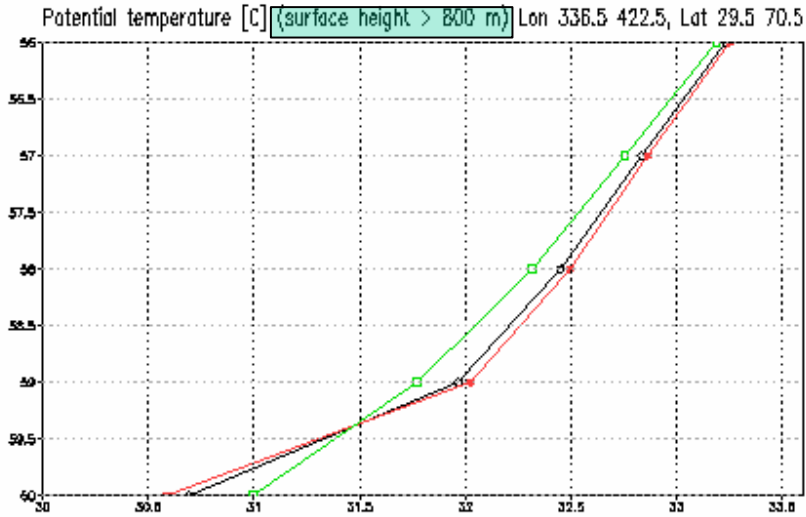
new therm. SSO term with unity-scaling

out_ic02-imp1-new_srf_cpl-pat_len=0.0-a_hssso=1.0 - ana_ice rout



or time=03Z23JUN2016 or hour=3hr

Nocturnal effect of new SI-term from thermal SSO



— out_ic02-imp1-new_srf_cpl
 — out_ic02-imp1-new_srf_cpl-pat_len=0.0
 — out_ic02-imp1-new_srf_cpl-pat_len=0.0-a_hss0=1.0

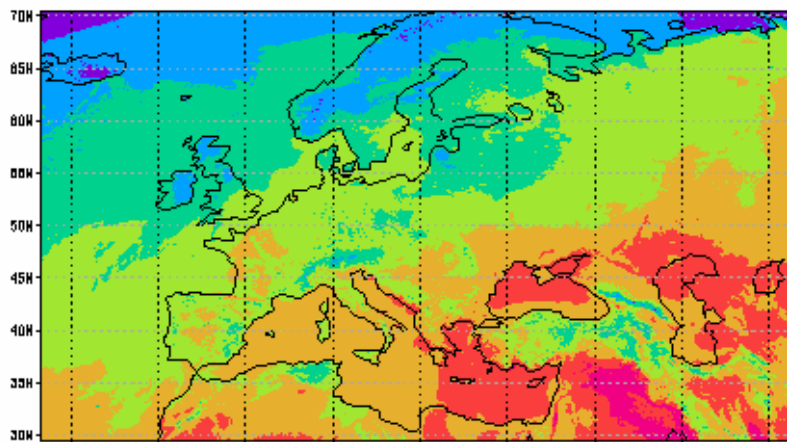
current circ.-term with strong SSO-limitation
 no thermal circulation term at all
 new therm. SSO term with unity-scaling

or time=03Z23JUN2016 or hour=3hr

2m-temperature [C]

Nocturnal effect of minimal diffusion coefficients

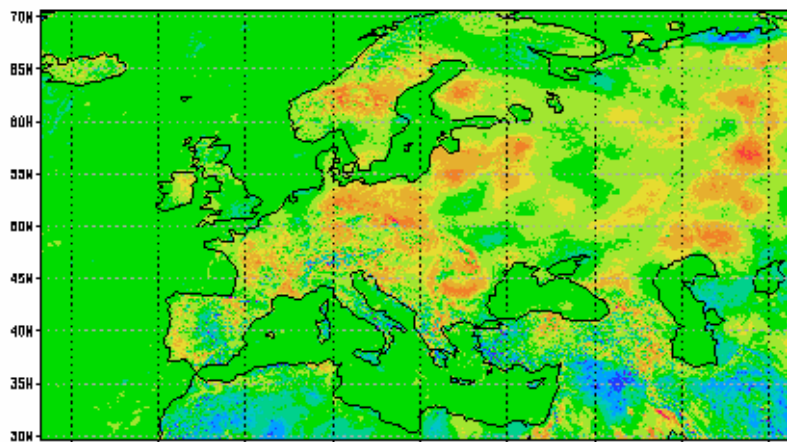
ana_icre_rout



MIN = -1.54884 MAX = 34.2832 AVE = 17.2751 SIG = 5.80114 SOP = 333.253

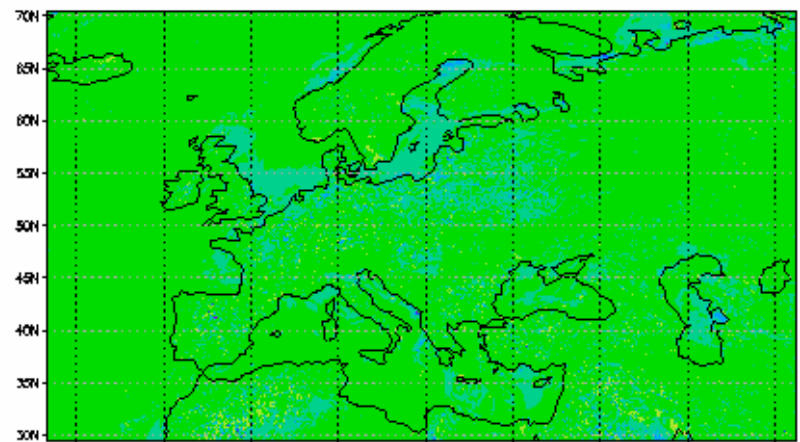
active minimal diff.-coeff. (operational)

out_ic02-imp1-new_srf_cpl - ana_icre_rout



MIN = -6.94481 MAX = 5.76833 AVE = 0.257303 SIG = 0.983543 SOP = 1.05333

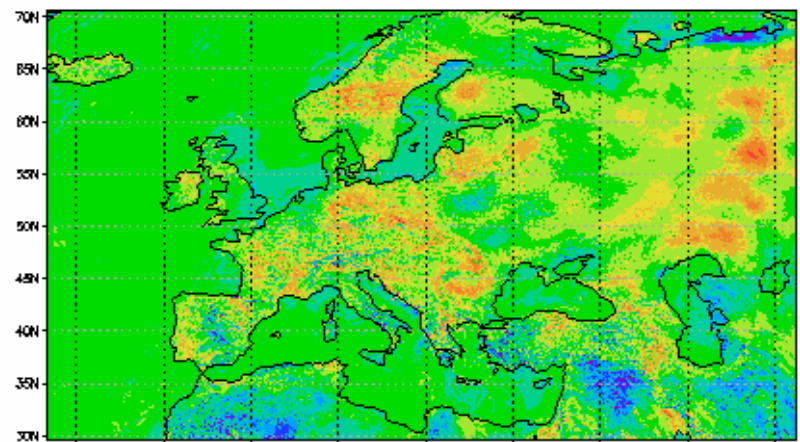
out_ic02-imp1-new_srf_cpl-tkmin=0.0 - out_ic02-imp1-new_srf_cpl



MIN = -6.81588 MAX = 2.28754 AVE = -0.277202 SIG = 0.431257 SOP = 0.262824

without minimal diff.-coeff.

out_ic02-imp1-new_srf_cpl-tkmin=0.0 - ana_icre_rout



MIN = -6.98818 MAX = 6.11734 AVE = -0.0188998 SIG = 1.07749 SOP = 1.18139

or time=03Z23JUN2016 or hour=3hr

Effect of hyperbolic profile for turbulent velocity at stable stratification:

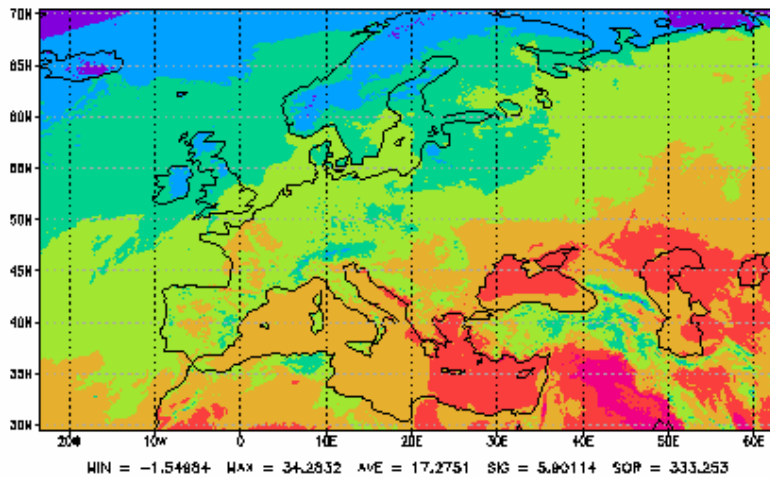
- **Right correction for nocturnal coupling**
 - **Smaller transfer velocities**
 - **Reduction of too excessive nocturnal BL-cooling**

- **Below clouds and at vegetated surfaces during summertime**
 - **positive nocturnal T2m-bias gets even larger**

2m-temperature [C]

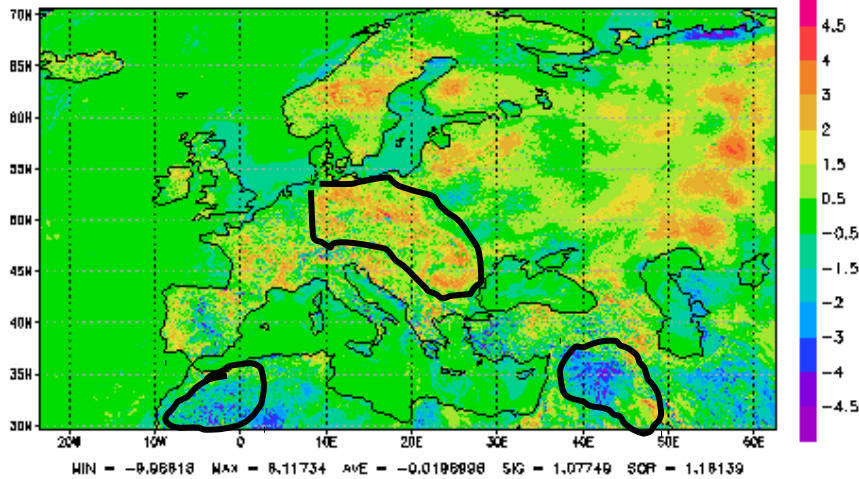
Nocturnal effect of hyperbolic profile for stable turbulent velocity scale

ana_icre_rout

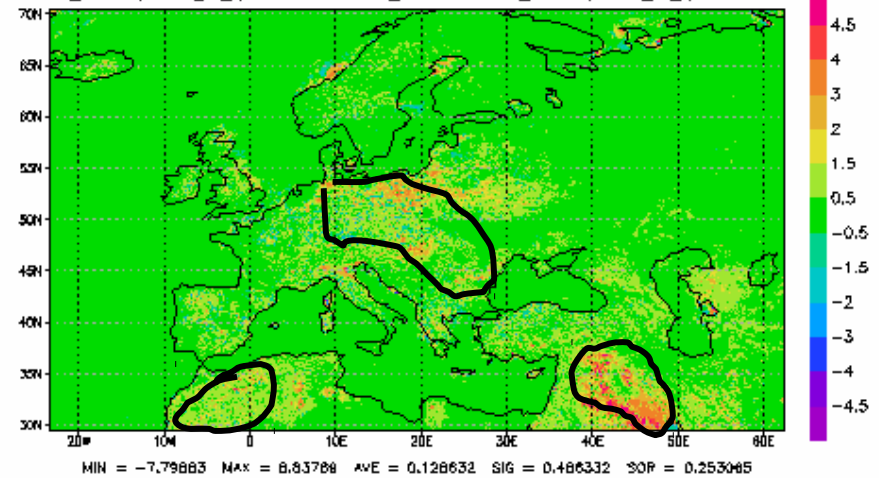


always with linear profile (operational)

out_ic02-imp1-new_srf_cpl-tkmin=0.0 - ana_icre_rout

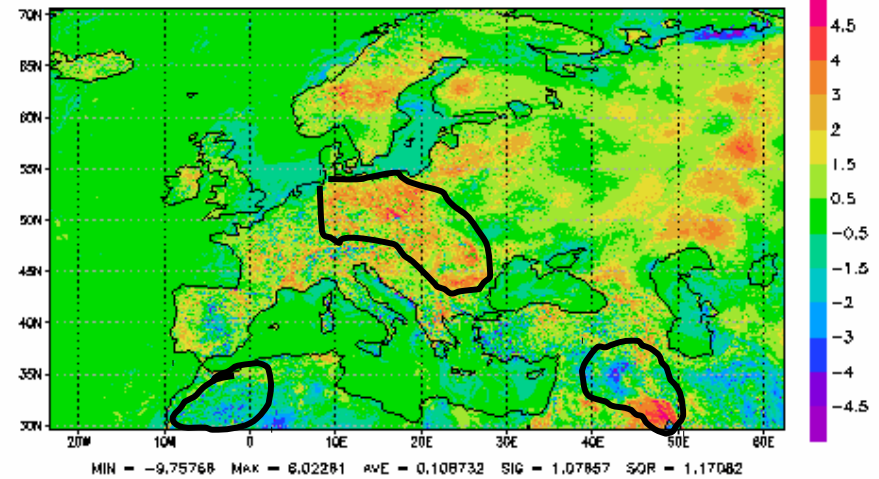


out_ic02-imp1-new_srf_cpl-tkmin=0.0-imode_trancnf=3 - out_ic02-imp1-new_srf_cpl-tkmin=0.0



with hyperbolic profile for stable start.

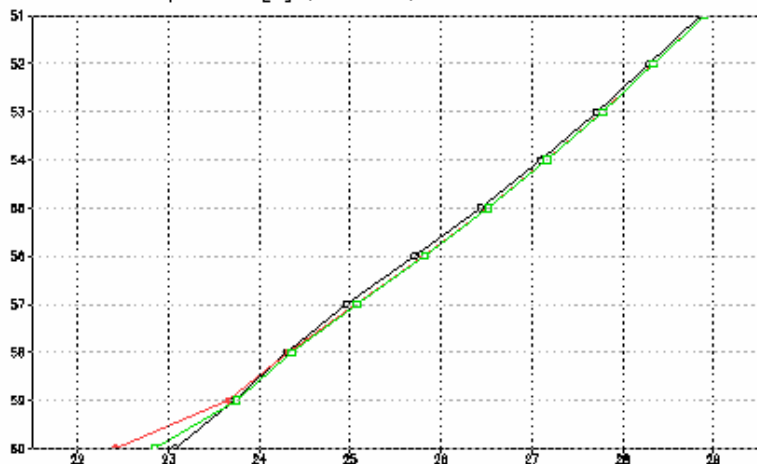
out_ic02-imp1-new_srf_cpl-tkmin=0.0-imode_trancnf=3 - ana_icre_rout



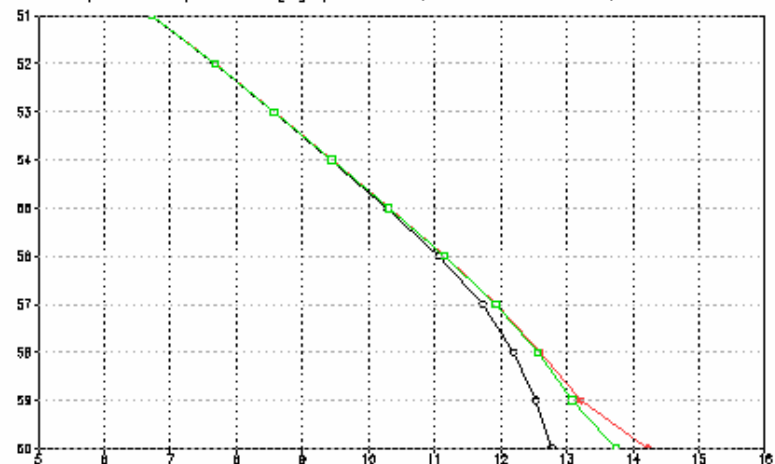
or time=03Z23JUN2016 or hour=3hr

Nocturnal effect of hyperbolic profile for stable turbulent velocity scale

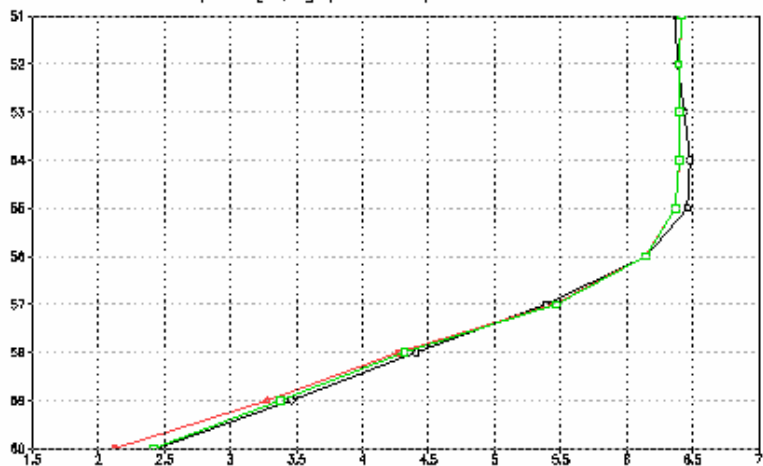
Potential temperature [C] (over land) Lon 336.5 422.5, Lat 29.5 70.5



Dew point temperature [C] (over land) Lon 336.5 422.5, Lat 29.5 70.5



Horizontal wind speed [m/s] (over land) Lon 336.5 422.5, Lat 29.5 70.5



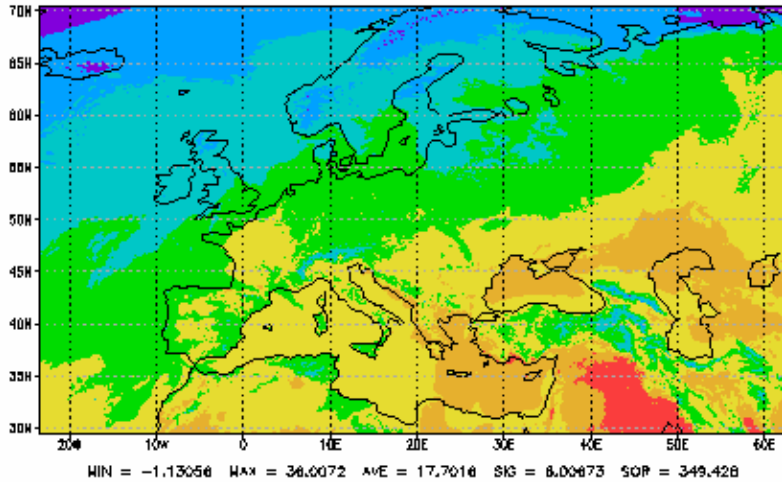
— **assimilation** — **always with linear profile (operational)** — **with hyperbolic profile for stable stratif.**
— ana_ircr_rout — out_ic02=imp1-new_srf_cpl-tkmin=0.0 — out_ic02=imp1-new_srf_cpl-tkmin=0.0-imode_trancnf=3

pr time=03Z23JUN2016 pr hour=3hr

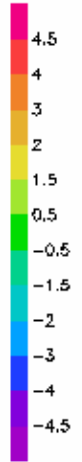
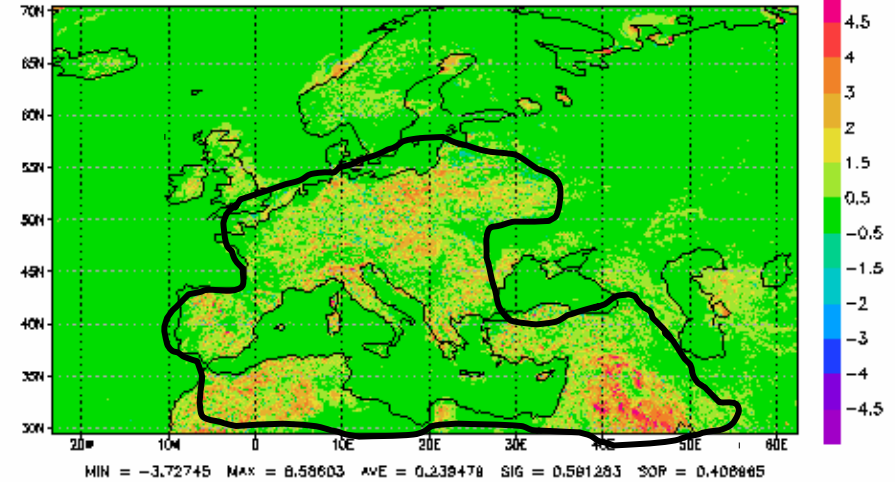
temperature [C]

Nocturnal effect of hyperbolic profile for stable turbulent velocity scale

ana_icre_rout

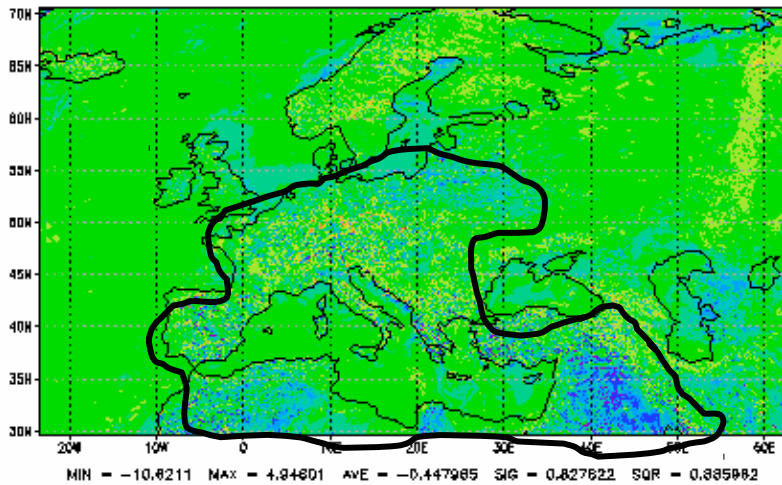


out_ic02-imp1-new_srf_cpl-tkmin=0.0-imode_trancnf=3 - out_ic02-imp1-new_srf_cpl-tkmin=0.0



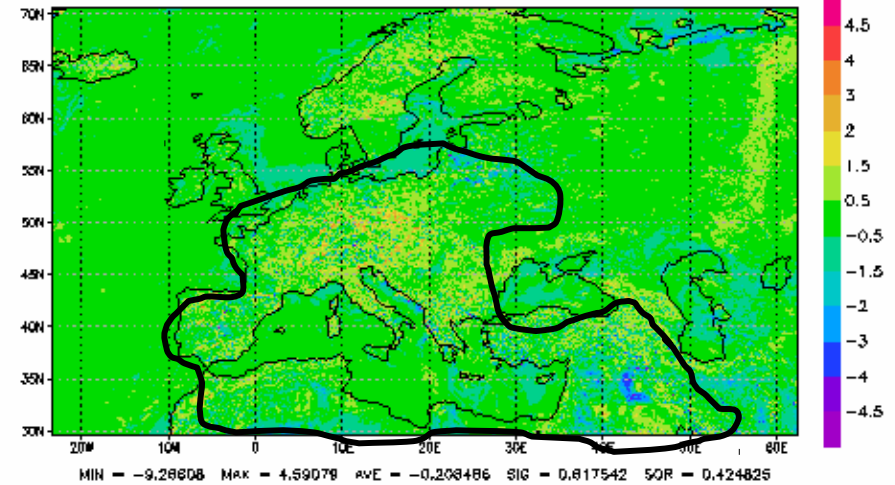
always with linear profile (operational)

out_ic02-imp1-new_srf_cpl-tkmin=0.0 - ana_icre_rout



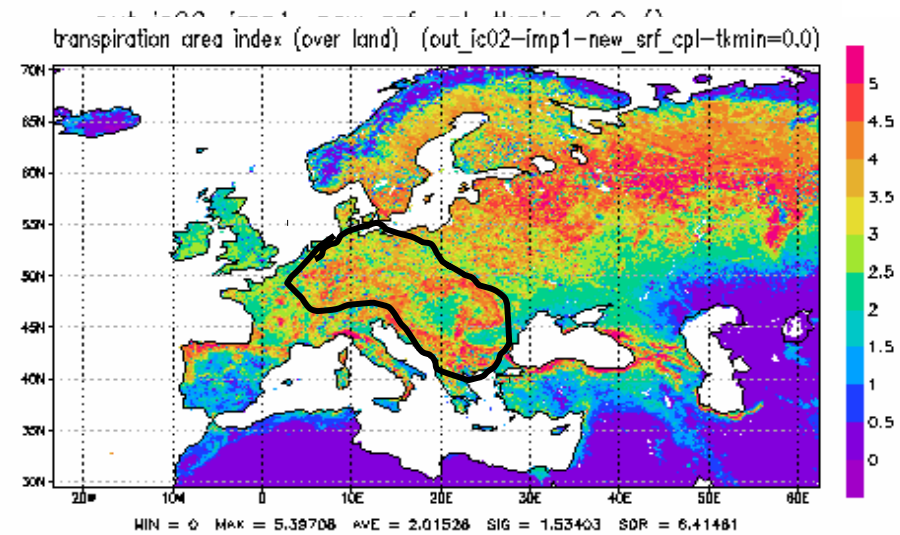
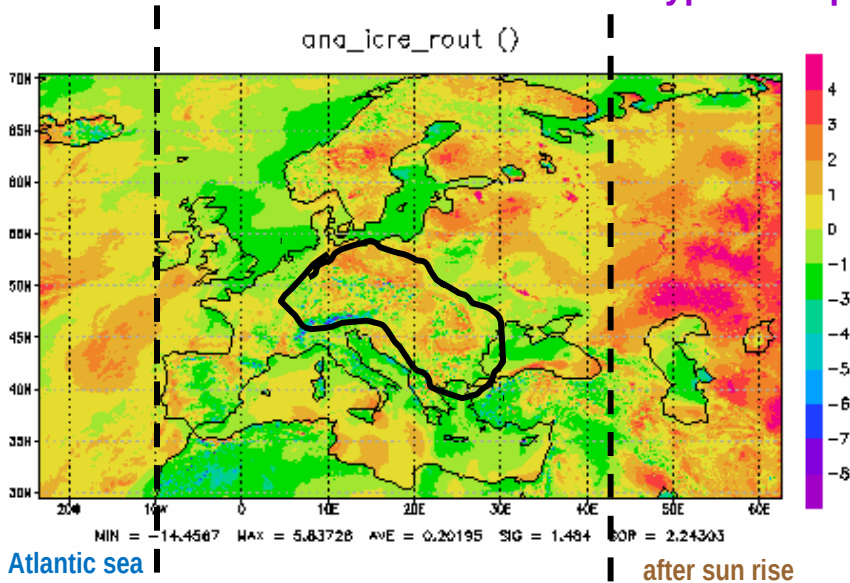
with hyperbolic profile for stable startif.

out_ic02-imp1-new_srf_cpl-tkmin=0.0-imode_trancnf=3 - ana_icre_rout



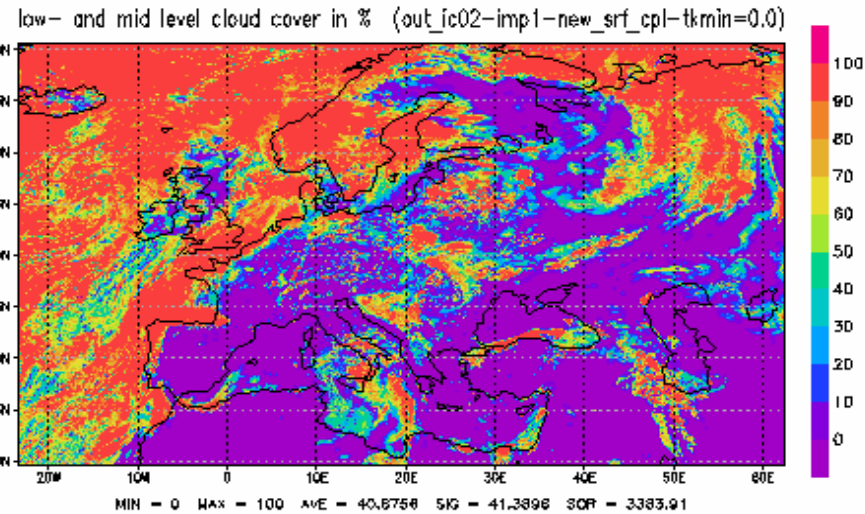
$$t_g - t_{2m} [C]$$

Nocturnal effect of hyperbolic profile for stable turbulent velocity scale



Attention:

- Nocturnal surface-temperature during the assimilation run is warmer than measured T2m!
- Not only below some sheltering clouds
- But correlated with the amount of leaves
 - Missing decoupling of plant-surfaces with the still warm soil mass!?
 - Radiative cooling is almost compensated by heat form the soil
 - Warmer nocturnal BL with hyperbolic profiles causes (although this is an improvement) an even increased positive T2m-bials.



- Semi-transparent and decoupled cover-layer in TERRA -> is being done

pr time=03Z23JUN2016 pr hour=3hr

Outlook:

- Implementing a semi-transparent substantial cover-layer built from R-elements being thermally decoupled from the rigid soil
 - Larger amplitude of diurnal cycle
 - Reduction of evaporating surface
 - Treatment of snow below a plant canopy

- Expressing missing transport parameterized sub-grid circulations
 - Additional vertical and horizontal diffusion at circulation scales

- Expressing the effect of turbulence on circulations
 - Substitution of dissipation-like scale-transfer expressing the related shear term directly
 - Automatically introduces turbulent feedback:
 - Dependency on turbulent length scale and thermal stratification

- Describing near surface thermal circulations caused by land use roughness
 - Kata- and anabatic circulations at buildings and vegetation
 - Nocturnal labialization and daytime stabilization of transfer between soil and canopy

▪ Another lesson from previous ConSAT tasks:

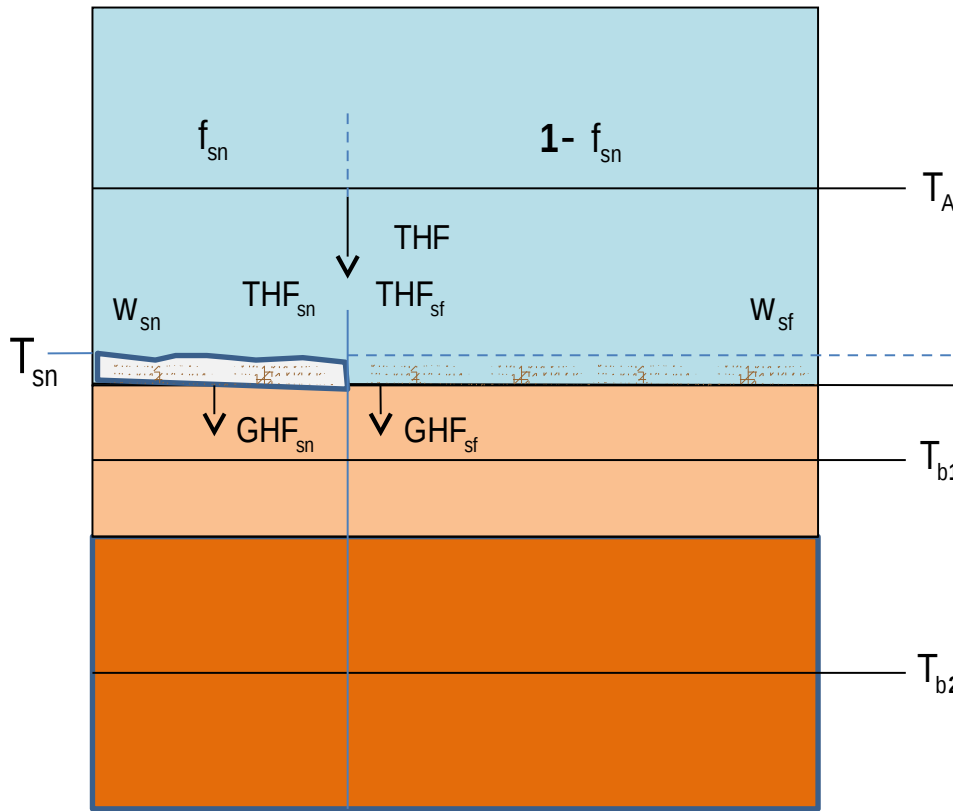
- Pure modifications in the description of the **turbulent Prandtl-layer** can hardly correct the main sources of current **model-errors** of the **diurnal cycle of near surface variables** and **of numerical instability of near-surface temperatures!**
- The description of **surface processes** provides by far the largest potential for improvement!!



Efforts towards a **substantial, semi-transparent** cover-layer (canopy) **thermally loosely coupled** to the dense soil:

1. **Additional thermal equation for snow-free skin**
2. **Linearization of surface processes**
3. **Thermal equations for skin, snow and soil coupled through implicit temperatures => extended linear system of equations**
4. **Related adaptations for snow-cover diagnostic, dynamic tiles and initialization**
5. **Merge with various work-arounds and extensions in ICON-TERRA**
6. **Including phase-transitions of precipitation (as well as soil water and the snow-cover) into the implicit treatment**
7. **Merge with prepared canopy-extension of skin-layer**
8. **Canopy-interception of snow and related adaptation of snow-tiles**
9. **Transfer of ICON-development into COSMO?**

New linear-implicitly coupled budget equations at the surface : (completely implemented)



$$\begin{aligned} \text{THF}_{sf} - \text{GHF}_{sf} &= [\rho_c c_c]^0 \frac{T_{cm} - T_{cm}^0}{\Delta t} \rightarrow 0 && \text{mean cover-temp. (of lin. vert. prof.)} \\ \text{THF}_{sn} - \text{GHF}_{sn} &= [\rho_{sn} c_{sn}]^0 \frac{T_{sm} - T_{sm}^0}{\Delta t} \rightarrow 0 && \text{mean snow-temp (of lin. vert. prof.)} \end{aligned}$$

substantial, loosely coupled, semi-transparent C-layer \rightarrow idealized, infinite-thin S-layer
 $T_b \rightarrow T_{sf}$

$$\text{GHF}_{sf} = -\alpha_{b1}^b \cdot (T_{sf} - T_{b1})$$

so far substituted by $T_{sf} = T_{b1}$

$$\text{GHF}_{sn} = -\frac{\alpha_b^{sn}}{\alpha_b^{sn} + \alpha_{b1}^b} \cdot (T_{sn} - T_{b1})$$

so far only explicit and resistance of soil-half-layer not considered

singularity for vanishing snow-depth

$$\begin{aligned} \text{THF}_{sx} &= [\text{PHF} + \text{SRF} + \text{LRF}_d + \text{LRF}_u + \text{SHF} + \text{LHF}]_{sx} \\ &= \text{THF}_{sx}^0 + \partial_{T_{sx}} [\text{LRF}_u + \text{SHF} + \text{LHF}]_{sx}^0 \cdot (T_{sx} - T_{sx}^0) \end{aligned}$$

so far only explicit contribution considered

\rightarrow so far no budget equation for T_{sf} in favour of setting $T_{sf} = T_{b1}$

$$\partial_{T_{sx}} [\text{LRF}_u]_{sx}^0 = -4\sigma\epsilon_0 [T_{sx}^3]^0$$

$$\partial_{T_{sx}} [\text{SHF}]_{sx}^0 = -[\rho_s u_{SA}^H]^0 \cdot c_p$$

$$\partial_{T_{sx}} [\text{LHF}]_{sx}^0 = -[\rho_s u_{SA}^H \cdot f_{sx}^{red} \cdot d_T q_v^{sat}(T_{sx}) \cdot L_{ev}(T_{sx})]_{sx}^0$$

New linear-implicitly coupled budget equations at the surface : (completely implemented)

$$THF_{Sx} = [PHF + SRF + LRF_d + LRF_u + SHF + LHF]_{Sx} \quad \text{total implicit heat flux-density towards the surface}$$

$$= THF_{Sx}^0 + \partial_{T_{Sx}} [LRF_u + SHF + LHF]_{Sx}^0 \cdot (T_{Sx} - T_{Sx}^0) \quad \text{explicit flux-density + implicit extension}$$

total (virtual) conductivity

$$\partial_{T_{Sx}} [LRF_u]_{Sx}^0 = -4\sigma\epsilon_0 \cdot (T_{Sx}^0)^3$$

atmospheric transfer-velocity for scalars

$$\partial_{T_{Sx}} [SHF]_{Sx}^0 = -[\rho_S u_{SA}^H]^0 \cdot c_p$$

specific humidity at saturation

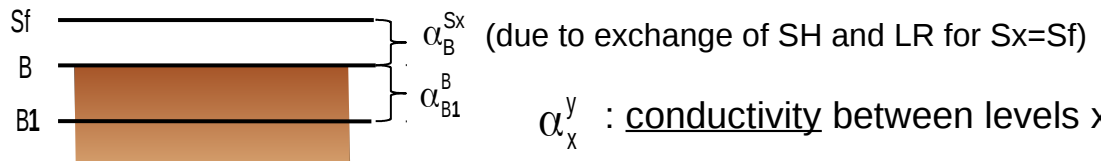
specific latent heat of evaporation

$$\partial_{T_{Sx}} [LHF]_{Sx}^0 = -[\rho_S u_{SA}^H \cdot f_{Sx}^{red} \cdot d_T \cdot \alpha_v^{sat} \cdot L_{ev}]_{Sx}^0 (T_{Sx}^0)$$

specific reduction of actual evaporation

concatenation of resistances

$$GHF_{Sx} = - \frac{\alpha_B^{Sx} \cdot \alpha_{B1}^B}{\alpha_B^{Sx} + \alpha_{B1}^B} \cdot (T_{Sx} - T_{B1})$$



$$THF_{Sn} - GHF_{Sn} = [\rho_{Sn} c_{Sn}]^0 \frac{T_{Sm} - T_{Sm}^0}{\Delta t} \xrightarrow{h_{Sn \rightarrow 0}} 0$$

reduces to **implicit flux-balance** for vanishing snow-depth

$$T_{Sm} = \frac{1}{2} \cdot (T_{Sn} + T_B) \quad \text{linear vertical T-profile of snow-pack}$$

$$THF_{Sf} - GHF_{Sf} = [\rho_c c_c]^0 \frac{T_{Cm} - T_{Cm}^0}{\Delta t} \xrightarrow{C_c \rightarrow 0} 0$$

reduces to **implicit flux-balance** for **currently applied skin-layer approximation**

$$T_{Cm} = \frac{1}{2} \cdot (T_C + T_B) \quad \text{linear vertical T-profile of R-layer}$$

$$\begin{matrix} C_c & \rightarrow & 0 \\ \alpha_B^{Sf} & \rightarrow & \infty \\ T_C & \rightarrow & T_B \end{matrix}$$



Implicit increments of atmospheric transfer velocities: (already implemented)

- Considering the **hidden T_{sx} -dependency** of the **transfer velocity for heat** u_{SA}^H , which controls the **virtual conductivities** of SHF_{Sx} and LHF_{Sx} :

$$\partial_{T_{Sx}} [SHF]_{Sx}^0 = - [\rho_S u_{SA}^H]^0 \cdot c_p \quad \partial_{T_{Sx}} [LHF]_{Sx}^0 = - [\rho_S u_{SA}^H \cdot f_{Sx}^{red} \cdot d_T q_v^{sat} \cdot L_{ev}]^0$$

$$[u_{SA}^H]^0 \rightarrow u_{SA}^H := [u_{SA}^H]^0 + \partial_{T_{Sx}} [u_{SA}^H]^0 \cdot (T_{Sx} - T_{Sx}^0)$$

- The implicit heat budgets for Sf and Sn become **quadratic** in T_{Sx} :
- From **solutions** T_{Sx}^* of the **decoupled** versions of these **implicit quadratic** equations:

$$[u_{SA}^H]^* = [u_{SA}^H]^0 + \partial_{T_{Sx}} [u_{SA}^H]^0 \cdot (T_{Sx}^* - T_{Sx}^0)$$

- This **updated transfer velocity** $[u_{SA}^H]^*$ is used in the **subsequent linear system**.
- The factor of the **linear T_{Sx} -dependency of the transfer-velocity** is estimated by **registration**:

$$\partial_{T_{Sx}} [u_{SA}^H]^0 \approx \frac{[u_{SA}^H]^0 - [u_{SA}^H]^{-1}}{T_s^0 - T_s^{-1}} \quad T_s := (1 - f_{Sn}) \cdot T_{Sf} + f_{Sn} \cdot T_{Sn}$$



Resulting matrix of the extended linear system:

- All 2 + k soil budgets are always present (even for $f_{sn}=0$ or $f_{sn}=1$)
- They are linearly coupled in the temperatures:

altered

created

	Sn	Sf	B1	B2	B3	...		
isc	a_{Sn}^{Sn}		a_{Sn}^{B1}				T_{Sn}	d_{Sn}
fes		a_{Sf}^{Sf}	a_{Sf}^{b1}				T_{Sf}	d_{Sf}
ifb	a_{B1}^{Sn}	a_{B1}^{Sf}	a_{B1}^{B1}	a_{B1}^{B2}			T_{B1}	d_{B1}
			a_{B2}^{B1}	a_{B2}^{B2}	a_{B2}^{B1}		T_{B2}	d_{B2}
	\vdots			a_{B3}^{b2}	a_{B3}^{B3}	a_{B3}^{B4}	\vdots	\vdots

• =

- Can easily be tri-diagonalized by matrix-operations and solved by the standard solver
- Partly reducible by parameters:

isc: degree of corrected implicit coupling of T_{Sn} to the soil- and atm. temperatures

fes: degree of considered flux-equilibrium in diagnostics of T_{Sf}

ifb: degree of implicitness for effective surface fluxes used in the heat budgets

Default for test: **isc=1; fes=1; ifb=1** (full implicit solution active) - modified for diagnostic points



Scheme for snow-covered fraction and snow-depth :

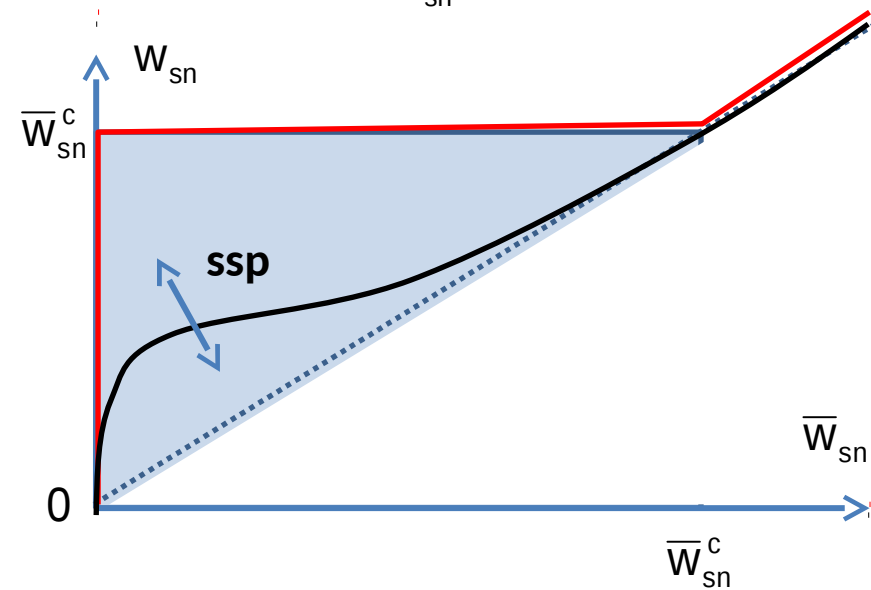
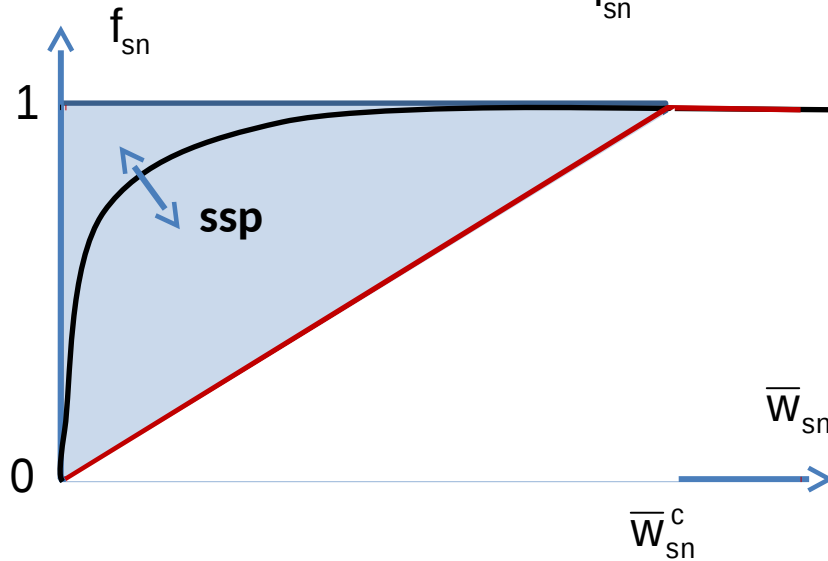
- Snow is not equally distributed along the grid-cell surface, due to various sources of inhomogeneity:

Snow-covered fraction f_{sn}

increases monotonically with mean snow-water level of a grid cell \bar{W}_{sn}

until a critical mean snow-water level \bar{W}_{sn}^c is reached.

- Specific snow-water-level $W_{sn} = \frac{\bar{W}_{sn}}{f_{sn}}$ is prop. to specific snow-depth h_{sn}



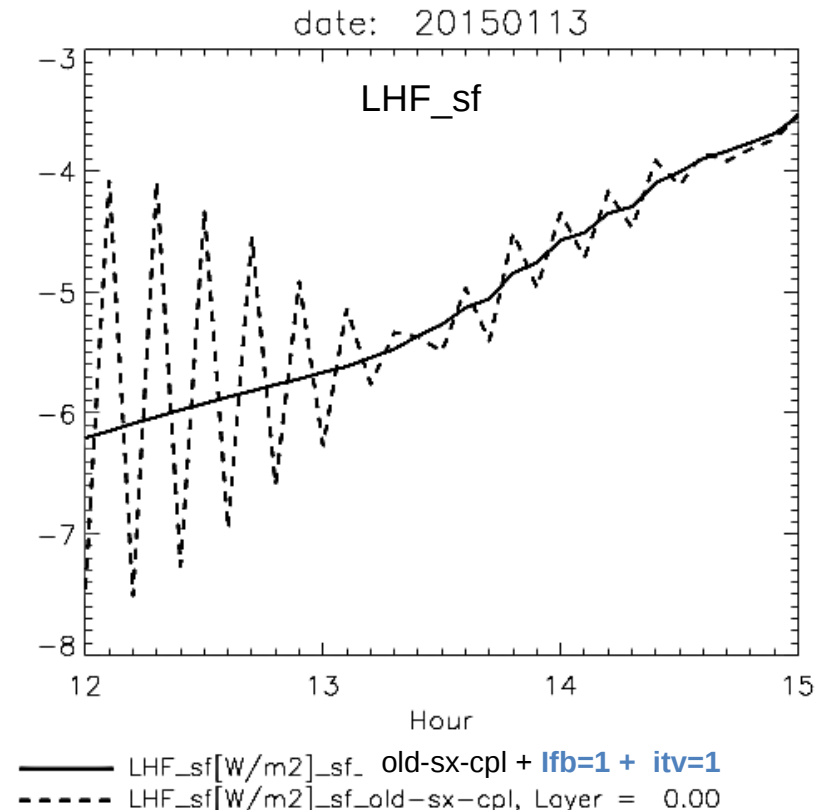
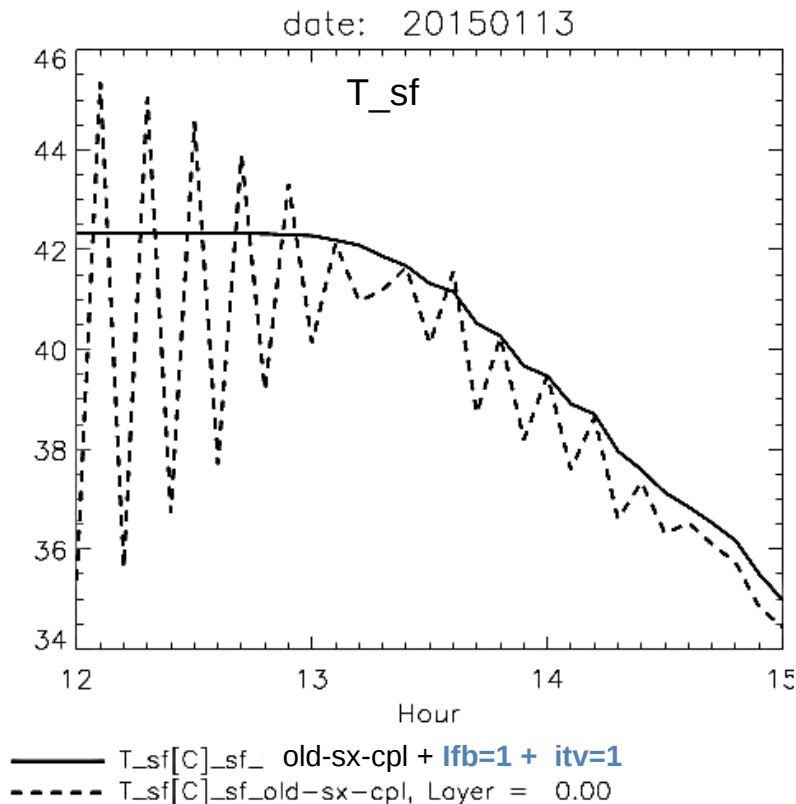
- New control-parameter : **ssp**: spreading efficiency

ssp=0: so far operational version; not steady; it is always $W_{sn} \geq \bar{W}_{sn}^c$!!

ssp=1: full snow-spreading; always full snow-cover!!

Test-grid-point Kenia (+33.71 +7.89) :

- After-noon situation; tropical hot with strong radiation forcing
- 3 hour ICON-global test-run (R2B6, dt=6min) with
- **implicit defaults** of the new development version of SAT-formulation (mainly TERRA)
- Emulation of so far operational **explicit surface coupling** only for a special grid-point



- **Oscillations almost completely eliminated by** **ifb=1 + itv=1**
- **Similar result but a bit larger daily amplitudes** **ifb=1 + itv=1 + fes=1 (not shown)**
itv=1: full consideration of implicit T_{sx}-dependency in atmospheric transfer velocity
fes=1: full consideration of flux-equilibrium at the sf surface



Current state :

- **Major adaptations** in TERRA, TURBTRAN (and related interfaces) introduced into **ICON-branch**:
 - **Restructuring** the **sequence of processes**
 - **Removal** of various, now **detrimental limitations** all over the code
 - **Reformulations** related to **variable-redistribution** for **dynamic snow-tiles**
 - **Generalization** of **snow-cover diagnostics**
 - **Substitution** of previous descriptions by **new formulations**
 - **Implementation** of **new features**
 - **Sanity-checks** performed:
 - **numerically stable** even for **large time steps**
 - some **remaining oscillations** due to **phase-transitions of snow or soil-water**
 - almost **minor differences** compared to operational version, **but:**
 - the so far **inconsistent** treatment of **rime as part of w_{sf}** had to be **removed!**
 - **positive effect of this feature no longer present!**
- ➔
- ❖ **consistent formulation of a 2-phase interception-store**
 - ❖ **together with the so far missing implicit formulation of w_{sf} -evolution**



New implicit and simultaneous incrementation of interception water: (partly implemented)

$$\frac{W_{Sf} - W_{Sf}^0}{\Delta t} = PWF_{Sf} + VWF_{Sf} + DWF_{Sf} \quad \text{PWF : given precipitation-water flux-density}$$

$$VWF_{Sf} = - f_{Sf}^{cov}(w_{Sf}) \cdot VWF_{Sf}^{pot}(T_{Sf}^0) \quad \text{: current water-vapour flux-density}$$

explicit potential evaporation (negative for dew- or rime-fall, where $f_{Sf}^{cov}(w_{Sf}) \equiv 1$)

linear cover-function: $f_{Sf}^{cov}(0) = 0$ $f_{Sf}^{cov}(w_{Sf}^{max}) = 1$ (for real evaporation)

$$DWF_{Sf} = - f_{Sf}^{drp}(w_{Sf}) \cdot DWF_{Sf}^{ref} \quad \text{: current drip-water flux-density}$$

explicit reference value at $f_{Sf}^{drp} = 1$ (parameter of the scheme)

rational drip-function: $f_{Sf}^{drp}(0) = 0$ $f_{Sf}^{drp} \xrightarrow{w_{Sf} \rightarrow w_{Sf}^{max}} \infty$



❖ **Quadratic equation for $0 \leq w_{Sf} \leq w_{Sf}^{max}$; automatically positive-definite and limited**
Simultaneous consideration of all sources and sinks

❖ still depends on previous surface temperature

➤ **No implicit coupling between hydrological and thermal equations yet!**

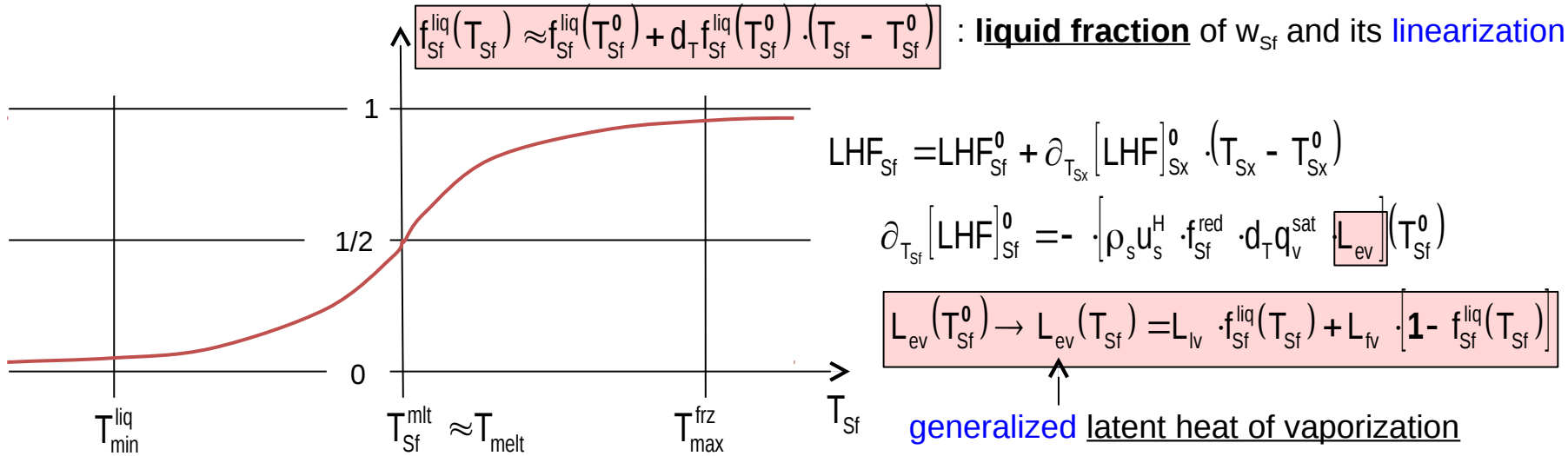
➤ Lower atmosph. BC: **explicit** VWF_{Sx}^0 and **corrected** VWF_{Sx}^0 !!

$$SHF_{Sx} = SHF_{Sx}^0 + \Delta THF_{Sx}$$



Implicit freezing and melting of interception water and precipitation: (being implemented)

- At least for $T_{\min}^{\text{liq}} \leq T_{\text{Sf}} \leq T_{\max}^{\text{frz}}$ **liquid and frozen interception-water coexists** with a **smooth transition**.



$$\text{PHF}_{\text{Sf}} = \text{PHF}_{\text{Sf}}^0 + \partial_{T_{\text{Sf}}} [\text{PHF}]_{\text{Sf}}^0 \cdot (T_{\text{Sf}} - T_{\text{Sf}}^0) \quad : \text{latent heat flux-density due to rain} \leftrightarrow \text{snow transition including implicit extension}$$

$$\text{PHF}_{\text{Sf}}^0 = L_{\text{fl}} \cdot \left[\text{RWF}_{\text{Sf}} - (\text{RWF}_{\text{Sf}} + \text{SWF}_{\text{Sf}}) \cdot \boxed{f_{\text{Sf}}^{\text{liq}}(T_{\text{Sf}}^0)} \right] \quad : \text{related explicit part}$$

$$\partial_{T_{\text{Sx}}} [\text{PHF}]_{\text{Sx}}^0 = - L_{\text{fl}} \cdot \left[\text{RWF}_{\text{Sf}} + \text{SWF}_{\text{Sf}} + \frac{W_{\text{Sf}}^0}{\Delta t} \cdot \boxed{d_T f_{\text{Sf}}^{\text{liq}}(T_{\text{Sf}}^0)} \right] \quad : \text{related virtual conductivity including associated phase transition of present interception water } W_{\text{Sf}}^0$$

❖ Introducing LHF_{Sf} and PHF_{Sf} in **decoupled** T_{Sf} -equation and solving this in **quadratic approximation**:

- **Correct** and **implicit** treatment of **liquid and frozen interception water**
- Final T_{Sf} is in **dynamical accordance** with **complete turnover of latent heat**.



Next steps:

- **Completion** of **running implementations** related to **interception water**
- **Running** chain of **test-cases**
- **Performing** some **code-optimizations** in terms of **vectorization** ➡ ❖ **1-st official ICON-release -> COSMO**
- **Adding** **melting of snow** and **freezing/melting of soil-ice** into the **implicit heat budgets** ➡ ❖ **2-nd official ICON-release -> COSMO**
- **Incorporation** of a **multi-layer snow-model**
- **Introducing** the extension with a **decoupled, substantial and semi-transparent cover-layer**, including
 - the **partitioning of fluxes** into those related to B and C
 - expressions for the **additional conductivity** α_B^C
and the **additional heat capacity** C_c :

$$\text{THF}_C - \text{GHF}_C = [\rho_c C_c]^0 \frac{T_{Cm} - T_{Cm}^0}{\Delta t}$$

$$T_{Cm} = \frac{1}{2} \cdot (T_C + T_B) \quad \text{linear vertical T-profile of R-layer}$$

$$\text{GHF}_C = - \frac{\alpha_B^C \cdot \alpha_{B1}^B}{\alpha_B^C + \alpha_{B1}^B} \cdot (T_C - T_{B1})$$

C_c due **mass of R-elements and interception water**

α_B^C due to **exchange of SH and LR between B and C**

- based on an **already developed prototype**, present in an **older test-version of COSMO!**
- largely **prepared just by the current implementations** into ICON!
- **removal** of remaining conceptual deficiencies!
- **significant impact** on simulated properties!



- n cover layers** including the **surface of the dense soil** (n=0) are connected by long-wave radiation interaction and sensible heat exchange

→ **thermally decoupled roughness elements (shading)**

- Only **a part of the inner surfaces is connected to A** by the resistance chain, the **other part is for the inter- surface exchange**

→ strongly effects the **LAI-impact of transpiration!**

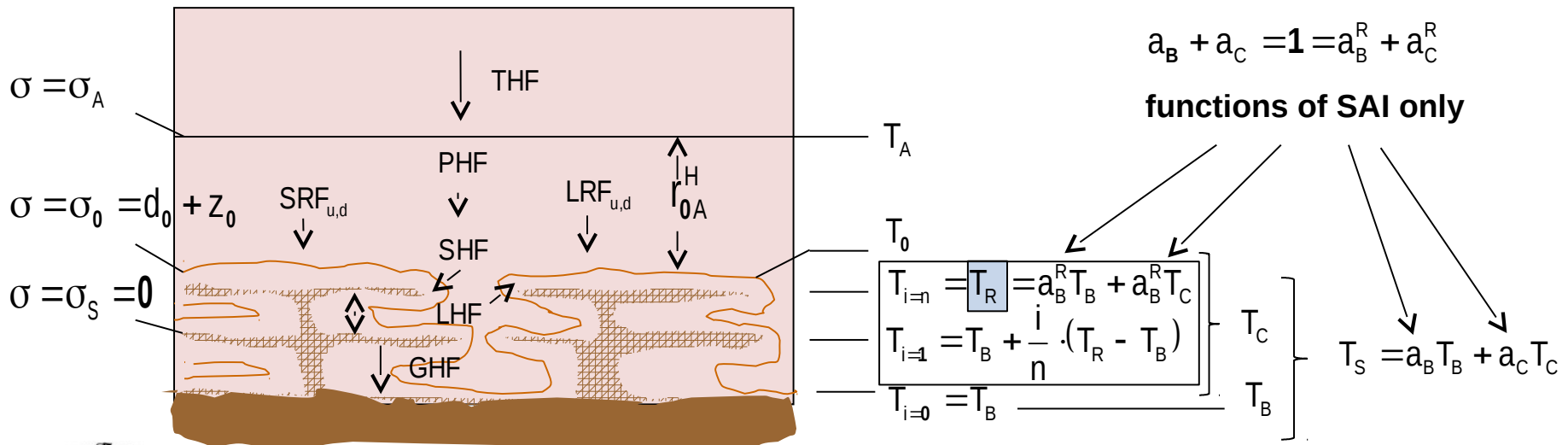
$$r_{SA}^H = r_{S0}^H + r_{0A}^H$$

$$r_{S0}^H = \frac{1}{\kappa S_0 \cdot u_0^H} \cdot \left[\lambda^H + \ln \frac{\kappa Z_0 u_0^H}{k^H} \right] = \frac{1}{\kappa u_0^H} \cdot \ln \left[\frac{Z_0}{Z_0^H} \right]$$

$$SAI = 2n + 1 = 2 \cdot LAI + c_{Ind}$$

$$S_0 = \frac{(SAI - 1) \cdot (SAI_\infty - 1)}{(SAI - 1) + (SAI_\infty - 1)} + 1$$

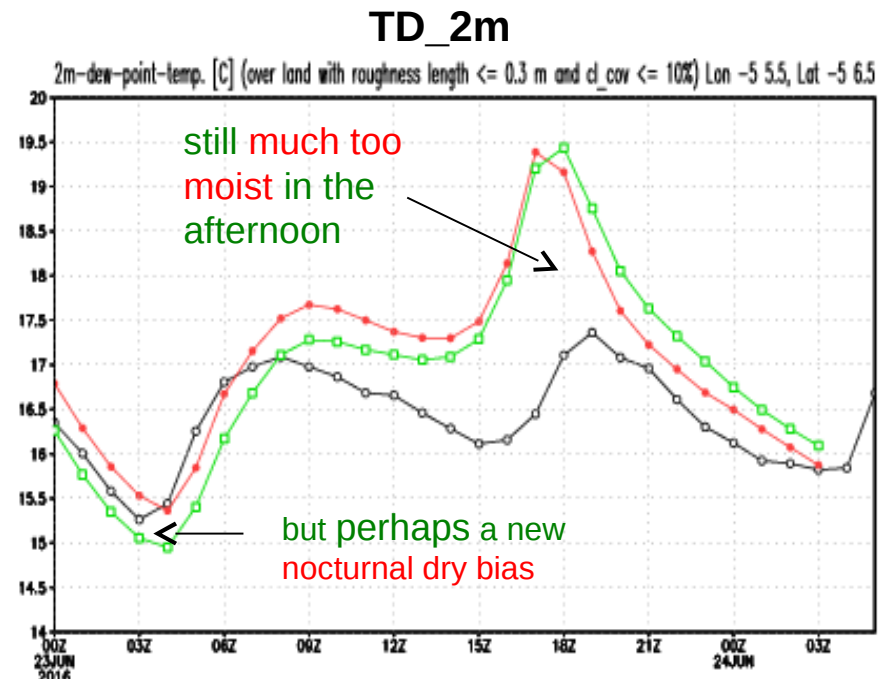
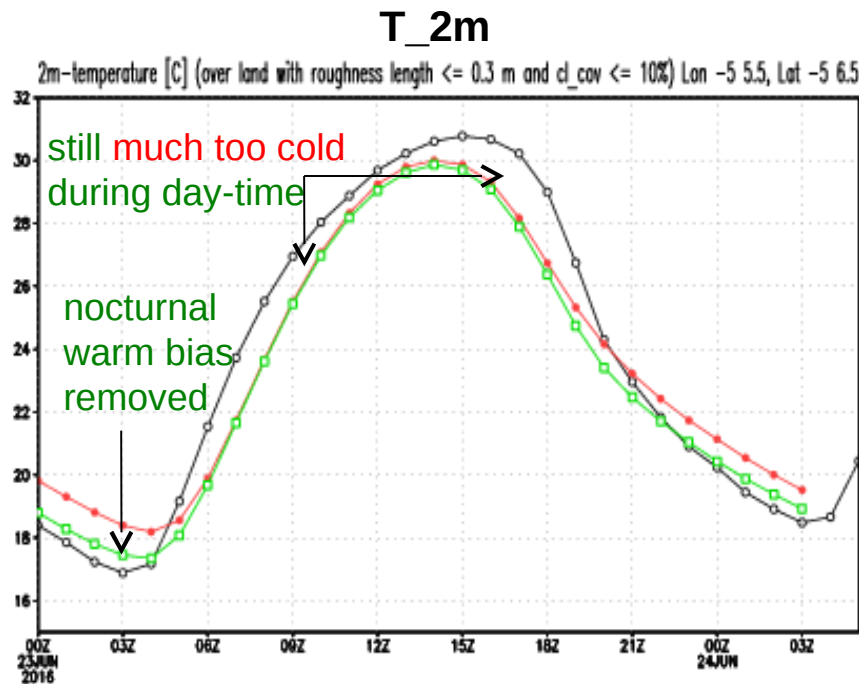
$\left[\begin{array}{l} = 1 \\ \rightarrow SAI_\infty \end{array} \right], SAI = 1$
 $\left[\begin{array}{l} = 1 \\ \rightarrow SAI_\infty \end{array} \right], SAI \rightarrow \infty$



COSMO-DE with lateral boundaries from ICON-EU

- ✓ only for rather smooth surfaces; **applied filter**
- ✓ almost saturated soil due to long standing rain period before
- ✓ almost no clouds due to high pressure situation; + **applied filter**

domain averaged daily cycles of near-surface variables



— ana_lm3_exp_10279 — out_lm3_rout — out_lm3_exp_10279
 direct analysis of operational revised TURBDIFF
 T_{2m} and TD_{2m} configuration imported from ICON



COSMO-DE with lateral boundaries from ICON-EU

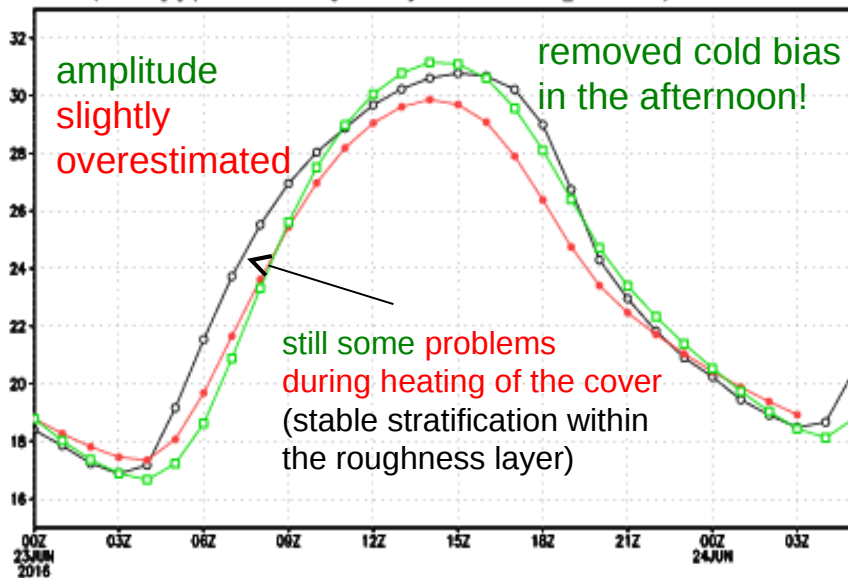
- ✓ only for rather smooth surfaces; **applied filter**
- ✓ almost saturated soil due to long standing rain period before
- ✓ almost no clouds due to high pressure situation; + **applied filter**

domain averaged daily cycles of near-surface variables

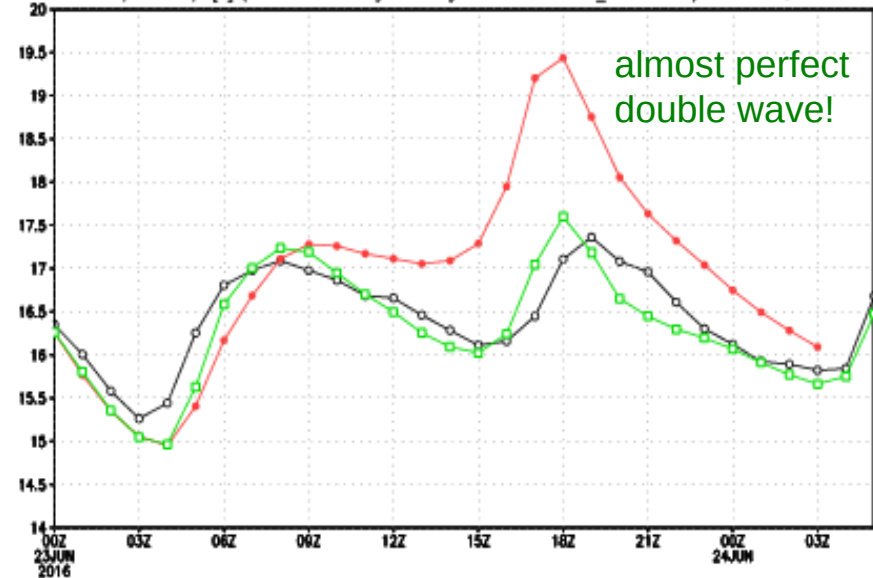
T_{2m}

TD_{2m}

2m-temperature [C] (over land with roughness length <= 0.3 m and cl_cov <= 10%) Lon -5 5.5, Lat -5 6.5



2m-dew-point-temp. [C] (over land with roughness length <= 0.3 m and cl_cov <= 10%) Lon -5 5.5, Lat -5 6.5



— ana_lm3_exp_10279

— out_lm3_exp_10279

— out_lm3_rlmk_new_surf-
icon-
icon-itype_surf=1-lsfluse=T-e_surf=10-c_soil=2-itype_vdif=1

direct analysis of
T_{2m} and TD_{2m}

revised TURBDIFF
imported from ICON

revised TURBDIFF imported from ICON
+ new decoupled surface cover: SAI_∞ = 10



Curing the interpolation problem:

- Changing linear u^ϕ -profile above roughness layer by a hyperbolic function in case of stable stratification (which is in accordance with solution from turbulence model)

$$\gamma_s^\phi := \frac{z_0}{h_p} \frac{u_p^\phi}{u_0^\phi} - 1 \quad s = \begin{cases} 1 & \text{unstable} \\ -1 & \text{stable} \end{cases} \quad h_x := z_x - z_0$$

$$r_{0A}^\phi = \frac{1}{\kappa} \int_{\ell_0}^{\ell_A} \frac{d\ell}{\ell \cdot u^H} = \frac{1}{\kappa u_0^\phi} \cdot \begin{cases} \frac{1}{1 - \gamma_1^\phi} \ln \frac{z_A}{z_0 + \gamma_1^\phi \cdot h_A} \\ (1 - \gamma_{-1}^\phi) \ln \frac{z_A}{z_0} + \gamma_{-1}^\phi \frac{h_A}{z_0} \end{cases} \xrightarrow{\gamma_1^\phi \rightarrow 0 \text{ (neutral)}} \ln \frac{z_A}{z_0} \quad \begin{matrix} u_p^\phi \geq u_0^\phi & \text{(unstable)} \\ u_p^\phi < u_0^\phi & \text{(stable)} \end{matrix}$$

new branch

Curing the vertical-discretization and neutral RL problem:

- Resistance formulation based on revised profile functions
 - without the interpolation node at level z_p
 - down through the RL
 - using the assumed constant profile properties u_* , θ_* and Γ

Iterative solution for TKE and the stability-functions:

$$r_p = \frac{\bar{p}}{\bar{p}_r} \frac{R_d}{c_{pd}}$$

$$r_v := 1 + \frac{R_v}{R_d} - 1 \hat{q}_v - \hat{q}_c$$

$$T_c = \frac{L_c}{c_{pd}}$$

$$\alpha := \partial_T q_{vs}(\hat{T})$$

$$r_T := \frac{1}{1 + \alpha T_c}$$

saturation fraction

$$\vartheta_v := r_T \cdot \left[r_v \vartheta_c - \frac{R_v}{R_d} \hat{T} \right]$$

$$\vartheta_w := \left[\frac{R_v}{R_d} - 1 \right] \cdot \hat{\theta} + \frac{r_c}{r_p} \cdot \vartheta_v$$

$$r_\theta := r_v - r_c \alpha \vartheta_v$$

$$F_T^M := (\partial_z \hat{u})^2 + (\partial_z \hat{v})^2 + \underline{F_C^M}$$

normal to grid scale surface additional shear

$$F^H := \frac{g}{\hat{\theta}_v} \cdot (\vartheta_w \partial_h \hat{q}_w + r_\theta \partial_h \hat{\theta}_w)$$

normal to horizontal surface

$$\frac{1}{\ell(z)} \approx \frac{1}{\kappa z} + \frac{1}{\ell_m} + a_{stab} \frac{\sqrt{F^H}}{q}$$

$$\partial_t \left[\frac{1}{2} \bar{\rho} q^2 \right] + \partial_z \left[-\bar{\rho} \ell S^q q \partial_z \left[\frac{1}{2} q^2 \right] \right] = \bar{\rho} q \ell \cdot \left[S^M r^M F_T^M - S^H F^H \right] - \frac{q^3}{\alpha^{MM} \ell} \rightarrow G_T^M := \frac{\ell^2}{q^2} \cdot F_T^M \geq 0 \quad G^H := \frac{\ell^2}{q^2} \cdot F^H$$

$$\left[\frac{1}{\alpha^H} + (3r^H \alpha^{HH} + 12\alpha^M) \cdot G^H \right] \cdot S^H + \left[6r^M \alpha^M G_T^M \right] \cdot S^M = 1 - 3c^H = b_H$$

$$\left[(9r^H \alpha^{HH} + 12\alpha^M) \cdot G^H \right] \cdot S^H + \left[\frac{1}{\alpha^M} + 9r^M \alpha^H G^H + 6r^M \alpha^M G_T^M \right] \cdot S^M = 1 - 3c^M = b_M$$

$\equiv a_{MH}$ $\equiv a_{MM}$

$$\alpha^M = 0.92, \quad \alpha^H = 0.74, \quad c^M = 0.08, \quad c^H = 0.0, \quad \alpha^{MM} = 16.6, \quad \alpha^{HH} = 10.1$$

$$r^\phi := \Gamma \cdot \left[1 + \frac{k^\phi}{K^\phi} \right] \cdot \left[\frac{1}{(1 + c_{di} S^2)} \right], \quad \phi \text{ a scalar}$$

SAI LCF DAI

$$S^H = \frac{b_H a_{MM} - b_M a_{MH}}{a_{HH} a_{MM} - a_{HM} a_{MH}}$$

$$S^M = \frac{b_M a_{HH} - b_H a_{MH}}{a_{HH} a_{MM} - a_{HM} a_{MH}}$$

Positive definite solution of prognostic TKE-equation:

VDif and optionally also HDif

optional vertical smoothing controlled by 'frcsmot'

$$\frac{q^2 - q_0^2}{2 \cdot \Delta t} \approx \left[\text{Adv}(q_0) + \text{Dif}(q_0) + \ell \cdot q \cdot (S^M r^M F_T^M - S^H F^H) \right] \cdot q - \frac{q_0}{\alpha^{MM} \ell} q^2$$

$$S_0^{M,H} = S^{M,H}$$

$$\frac{1}{\tau} := \frac{1}{2\Delta t} + \frac{q_0}{\alpha^{MM} \ell} \quad q_1 := \frac{\tau}{2} \cdot \left[\text{Adv}(q_0) + \text{Dif}(q_0) + \ell \cdot (S_0^M F_T^M - S_0^H F^H) \right] \quad q_2 := \tau \frac{q_0^2}{2\Delta t} \geq 0$$

$$> \text{'frcsecu'} R_f^c \cdot F_T^M$$

$$q_0 = q \quad t = t_0 + \Delta t \quad S^{M,H} = \text{'stbsmot'} S_0^{M,H} + (1 - \text{'stbsmot'}) \cdot S^{M,H}$$

$$q = q_1 + \sqrt{q_1^2 + q_2^2} > 0$$

always a positive solution of TKE equation

~~$$\text{'frcsecu'} \rightarrow -\infty$$~~

~~$$\text{'tkesecu'} \rightarrow 0$$~~

$$\frac{\ell^2}{q_c^2} (S^M F_T^M - S^H F^H) = \gamma_{|R_i=0}^c = \frac{\alpha^H (1 - 3c^M)}{f^H(1)}$$

$$q = \text{MAX}(\text{'tkesecu'} \cdot \text{'vel_min'}, \text{'tkesecu'} q_c, \text{'tkesmot'} q_0 + (1 - \text{'tkesmot'}) \cdot q)$$

Calculation of stability functions:

$$S^M, S^H$$

The STIC-scheme including empirical parameterization extensions:

Matthias Raschendorfer, Günther Zängl (DWD)

partly substituting artificial security limits and related stratification damping

Ri-number dependent scaling factor

optionally contributing to physical horizontal diffusion

with optional positive definite solution of prognostic TKE-equation and optional vertical smoothing of F_T^M F^H

laminar-, tilted surface- and roughness-layer-correction

STIC-impact:

additional SGS shear by :

- SHS circulation
- SSO wakes,
- SSO density currents
- plumes of SGS convection

$$r_M \cdot (F^M + F_C^M)$$

$$\frac{q^2 - q_0^2}{2 \cdot \Delta t} \approx [Adv(q_0) + Dif(q_0) + \ell \cdot (S^M F_T^M - S^H F^H)] \cdot q - \frac{q_0}{\alpha_{MM}^M \ell} q^2$$

≥ 0 restrictions for very stable stratification < 0

including non-gradient diffusion

now more flexible

potentially reducing stable stratification-damping

artificial treatment of possible singularities

$$q = \max\{v_{min}, q\}$$

minimal turbulent velocity scale with a stability dependent correction (near the surface)

diagnostic (linear) system dependent on

$$TKE = q^2/2$$

and mean vert. gradients

$$F_T^M \quad F^H$$

$$S^M \quad S^H$$

(for all other 2-nd order moments)

=>

stability functions:

Implicit vertical diffusion update for mean vert. gradients using

$$\text{restricted vertical diffusion coefficients } K^{M,H} = \max\{k^{M,H}, \ell q S^{M,H}\}$$

Ri-number dependent minimal diffusion coefficients

Current realization:

- We usually apply parameterizations of effects on 1-st order budgets due to different processes (turbulence, convection, SSO wakes) without using a clear separation procedure
 - Each scheme for a specific SGS process would only be valid, if all the other sub grid scale processes were in accordance with the specific closure assumptions, what is in CONTRADICTION to the need of DIFFERENT SGS models!!
 - Problems with incomplete description: **double-counting, non-realizability**
- Some **SGS contributions of source terms** in 1-st order budgets as well as in the budgets for SGS motions are only **considered partly or inconsistently**
 - Some direct and indirect **SGS effects are missing or are poorly described**
- Some **coupling between local parameterizations is missing**
 - Partly **unrealistic or contradicting model results**

Conditional-Domain (CD) budgets for description of sub-grid circulations:

$$\bar{\zeta}_{|G}(\mathbf{r}, t) := \frac{1}{|G(\mathbf{r}, t)|} \int_{s \in G(\mathbf{r}, t)} \zeta(\mathbf{s}, t) d^3s \quad \text{conditional average (representing e.g. the convective } \mathbf{G}_+ \text{ or } \mathbf{G}_- \text{ updraft or downdraft)}$$

- budget for a conditional averaged property:

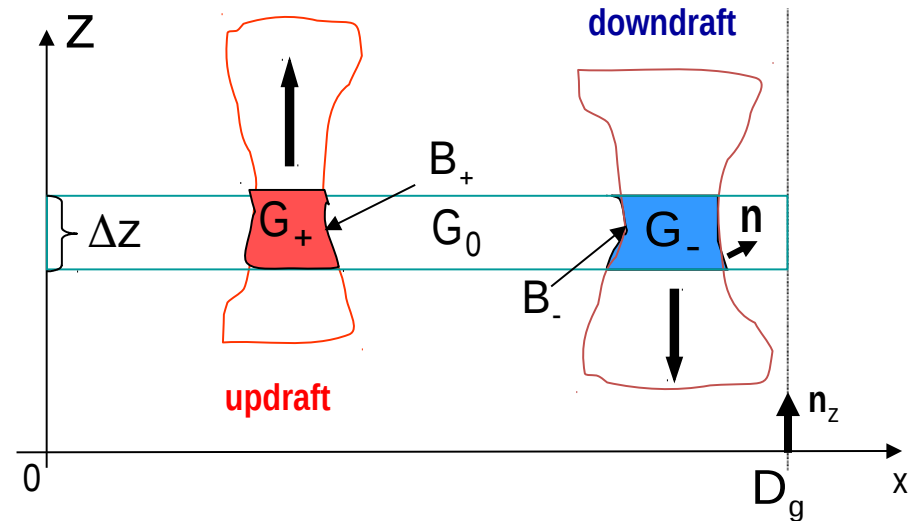
$$\partial_t(a\bar{\rho}\hat{\phi}) + \nabla \cdot \left[a\bar{\rho}\phi\mathbf{v} \right] = a \cdot (Q_{\text{sur}}^\phi + Q^\phi) \quad Q_{\text{sur}}^\phi := - \frac{1}{|G|} \int_{s \in B} \rho\phi \cdot (\mathbf{v}^\phi - \partial_t \mathbf{s}) \cdot \mathbf{n} d^2s \quad \text{inflow via the inner boundary surface}$$

↑
volume fraction of the related subdomain

- continuity equation:

$$\partial_t \ln a = \frac{1}{|G|} \int_{s \in B} \partial_t \mathbf{s} \cdot \mathbf{n} d^2s = \frac{|B|}{|G|} \overline{\partial_t s_n|_B}$$

↑
Inner boundary surface of the subdomain



Equations to be solved under simplifying assumptions

- stationarity, same horizontal advection for each subdomain, ...

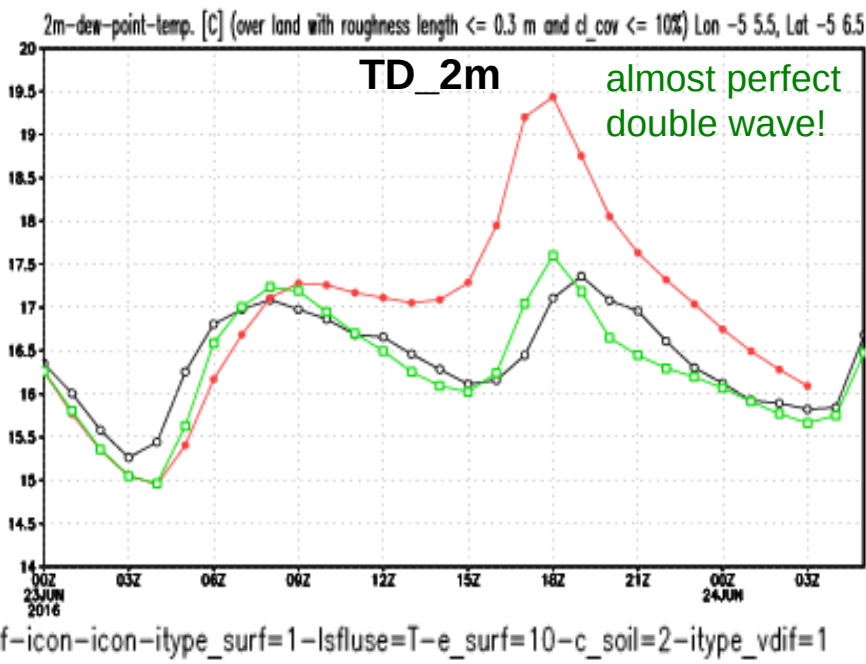
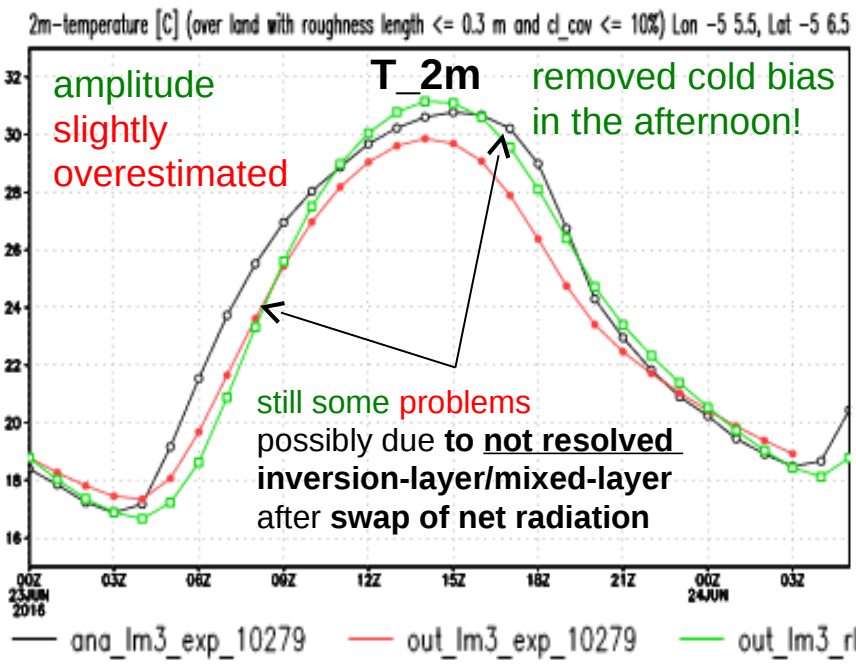
- A more advanced **semi-transparent C-layer extension** (by M. Raschendorfer) with **parameterized heat-conduction** and **heat storage** of the **full roughness cover** (e.g. plant canopy) is **being adapted** from an existing test-version prepared last year within COSMO.
 - The **final combination** with the **reformulated budgets** will **include all related partial development!**

2) Experiment with **the existing test-version in COSMO:**

- COSMO-DE with lateral boundaries from ICON-EU
- domain averaged daily cycles of near-surface variables
- almost saturated soil** due to long standing rain period before
- only for rather smooth surfaces: applied filter**
- almost no clouds** due to high pressure situation + **applied filter**

already shown last year

conditional diagnostic

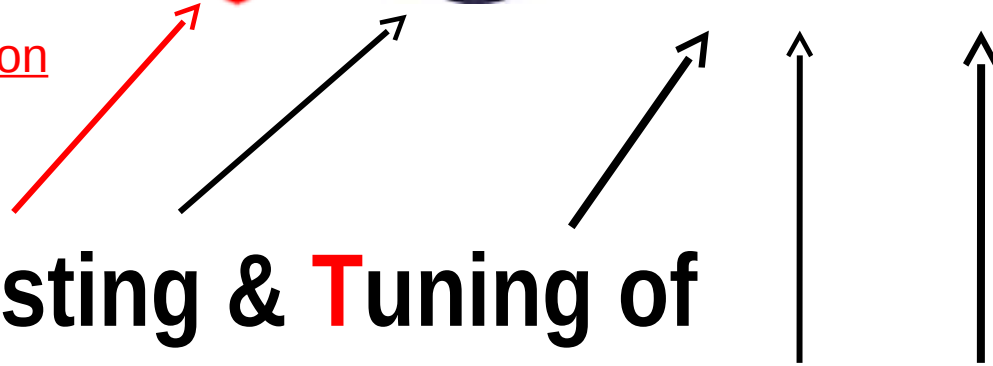


direct analysis of T_{2m} and TD_{2m} revised TURBDIFF imported from ICON

full C-layer treatment : semi-transparent + loosely coupled + heat-storage + adapted evapo-transpiration



- effect of single-precision radiation calculations on results



Testing & Tuning of (Revised Cloud Radiation Coupling)

T²(RC)² :

Harel Muskatel (HM)

Uli Blahak (UB), Pavel Khain (PK), Alon Shtivelman (AS),

Matthias Raschendorfer (MR), Daniel Rieger (DR),

Simon Gruber (SG), Martin Koehler (MK),

Xavier Lapillonne (XL), Oliver Fuhrer (OF), Gdaly Rivin (GR),

Natalia Chubarova (NC), Marina Shatunova (MS),

Alexey Poliukov (AP), Alexander Kirsanov (AK).

▪ New Optical Properties (OP) of ice & cloud droplets after Fu et al. / Hu & Stamnes:

- ✓ OP as function of **wave length** and **Effective Arguments (EA)**: R_{eff} , particl. Length (L) and Depth (D)
- ✓ EAs deduced from particle size distribution $N(L)$ and mass-size relation $m(L)$
- ✓ Theoretical relation between OPs as function of EAs fitted in terms of **rational functions** for 8 distinctive spectral bands

UB, HM



- ✓ **Implementation into ICON radiation-code**
- ✓ **test runs with ICON-global performed**
- **Tests with ICON-LAM at IMS / Russia**

SG

SG, MK

▪ ICON-ART dust as input for COSMO radiation:

- ✓ Successfully implemented
- ✓ Few clear-sky comparisons against CLIRAD-model and Nes-Tziona AERONET station with positive results
- Further testing

DR, HM

DR, NC

▪ CAMS prognostic aerosols in water in scheme for water-droplet nucleation :

- ✓ Derivation of cloud NC as function of aerosol NC according Segal & Khain
- ✓ Expression vertical Reff-profile dependent on cloud NC including sub-grid effects through turbulence and convection

UB

- ✓ Successfully implemented in COSMO (1-mom. microph. and radiation)
- ✓ Few-days case study performed:
 - Calculated Cloud NC available in microph. effects LWC and CLC
 - Reff has large impact on radiation heating rates
 - T2m, precip. and integr. cloud-cover are strongly effected
- Further testing and verification with mixed aerosol types

HM

▪ Tuning 4 sub-versions for cloud-radiation interaction in COSMO :

- i. Standard scheme with constant R_{eff}
- ii. Parameterized R_{eff} based on Tegen-climatology
- iii. Parameterized R_{eff} based on CAMS-aerosols
- iv. Parameterized R_{eff} based on Tegen-climatology
+ special extension for shallow cumulus clouds

PK

- ✓ Comparison of global radiation-simulation with local measurements and CM-SAF for a 4-month period in 2016
- ✓ Improvement of RMSE for global radiation by several %

PK

▪ Reviewing current shallow-cumulus parameterization :

- Comparison of LWC through shallow-convection with Pavel's approach of pure adiabatic lifting
- Employing LWC from shallow convection for Pavel's extended parameterization of R_{eff} for convective clouds.

