

Prognostic Precipitation in the Lokal-Modell (LM)

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COSMO-Meeting, Mailand, 22.09.2004

COSMO, Work Package 2.1.1:

Task:

replacement of the **diagnostic scheme** for rain/snow in LM 3.5
by a **prognostic scheme**
in operational use since 26.04.2004 (LM 3.9)

Aim:

improvement of the precipitation distribution in orographically structured areas
due to horizontal **drifting** of rain/snow (solving the ‚windward-lee-problem‘)

Conservation equation for humidity variables

current LM: diagnostic
scheme for rain/snow

$$0 = -\nabla \cdot \mathbf{P}^x - \nabla \cdot \mathbf{F}^x + S^x$$

,column-
equilibrium‘

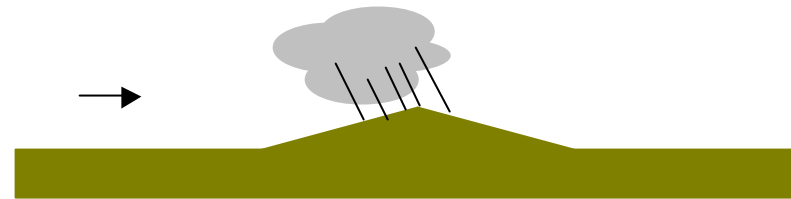
\mathbf{r}	[kg/m ³]	density of air
$q^x = \mathbf{r}^x/\mathbf{r}$	[kg/kg]	specific mass
\mathbf{P}^x	[kg/m ² /s]	sedimentation flux of x (only $x=r,s$)
\mathbf{F}^x	[kg/m ² /s]	turbulent flux of x
S^x	[kg/m ³ /s]	sources/sinks of x (cloud physics)

$x=v$	water vapour
$x=c$	cloud water
$x=i$	cloud ice
$x=r$	rain drops, $v_{\text{sedim}} \approx 5$ m/s
$x=s$	snow, $v_{\text{sedim}} \approx 1..2$ m/s

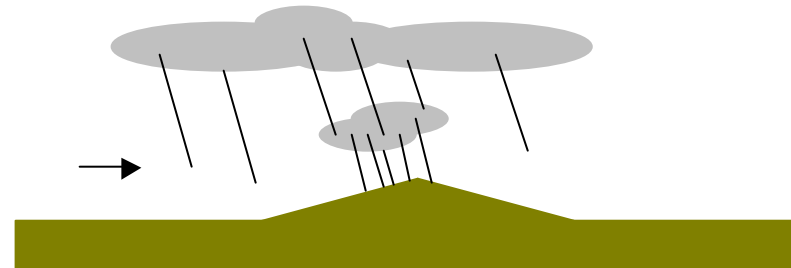
Mechanisms of orographic precipitation generation

(Smith, 1979)

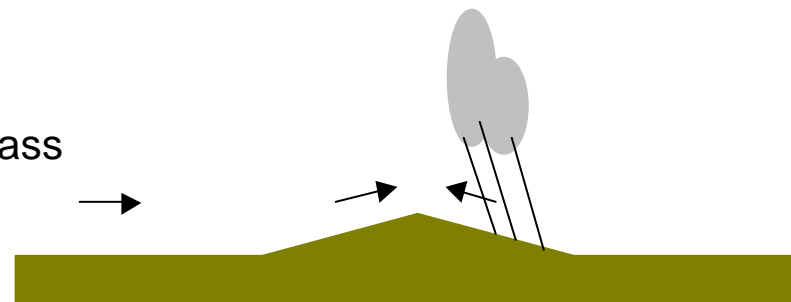
Large-scale upslope precipitation



Seeder-Feeder-mechanism



Cumulonimbus in conditionally unstable airmass



Semi-Lagrange-schemes

Advection-equation (1-dim.)

$$\frac{\partial \phi}{\partial t} + u \frac{\partial \phi}{\partial x} = 0$$

or

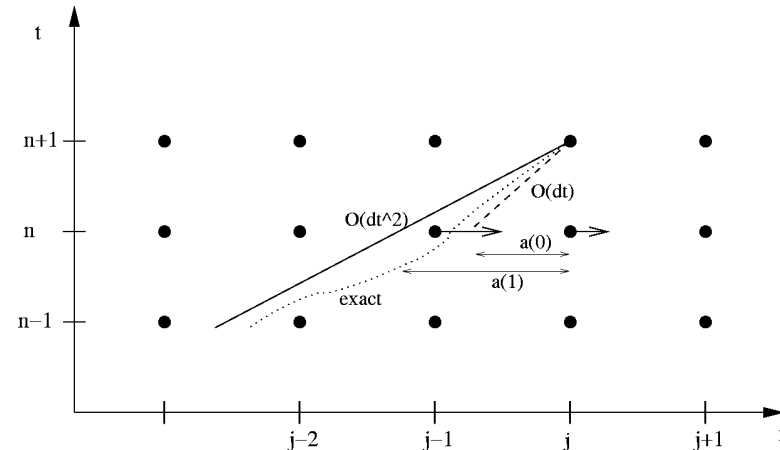
$$\frac{d\phi}{dt} = 0, \quad \frac{dx}{dt} = u$$

Numeric formulation

$$\phi(x_j, t^{n+1}) = \phi(\tilde{x}_j^{n-1}, t^{n-1})$$

Properties:

- unconditionally stable (for $u=\text{const.}$, without source terms)
- simple use in irregular grids
- avoids non-linear instabilities by advection



- 1.) determine the backtrajectory
- 2.) interpolate f at the starting point

Lit.: e.g. Staniforth, Côté (1991)

In LM 3.9 used for prognostic precipitation:

Semi-Lagrange Advection

- backtrajectory in 2. order $O(\Delta t^2)$ (about 80% comp. time)
- trilinear interpolation (about 20% comp. time)

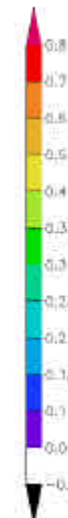
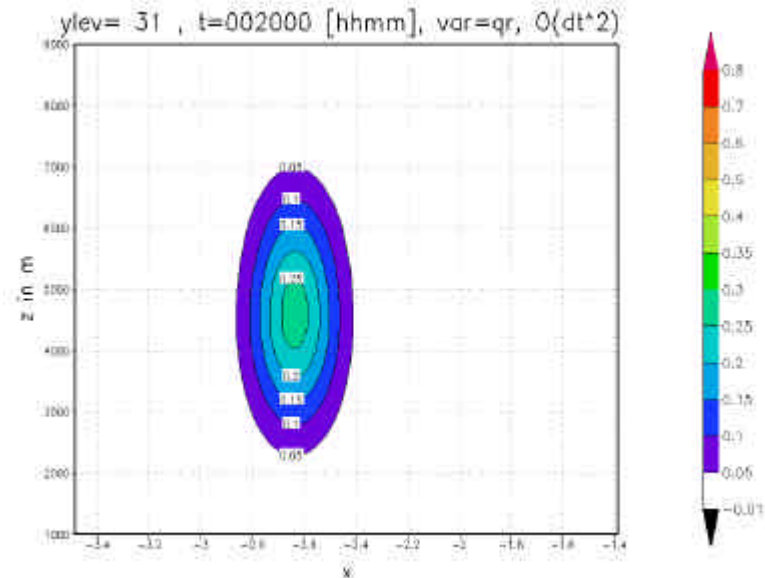
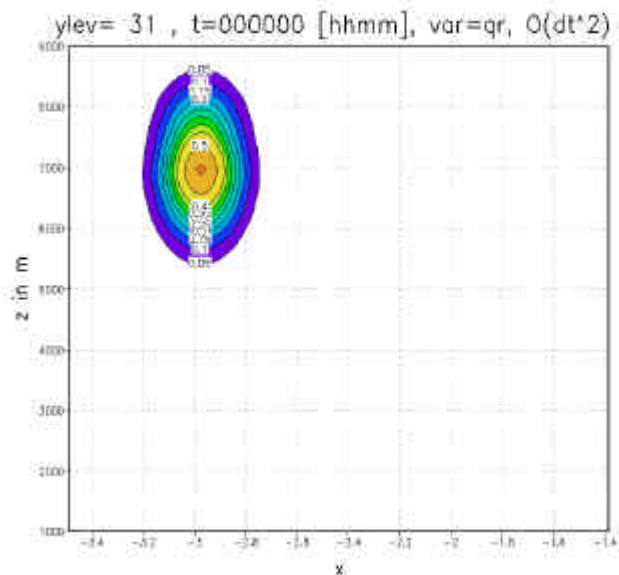
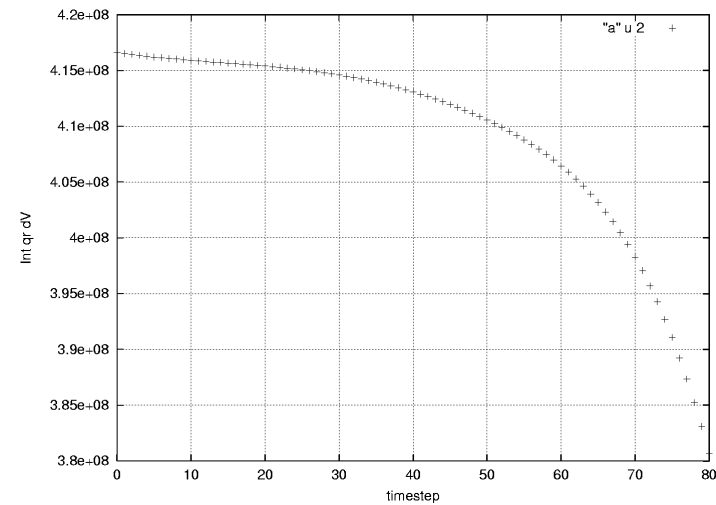
Properties:

- positive definite
- conservation properties sufficient for rain/snow
- relatively strong numerical diffusion

Test of Semi-Lagrange-Adv. in LM

backtrajectory in 2. order $O(\Delta t^2)$,
trilinear interpolation

plane, $(u,v,w) = (30, 0, -2)$ m/s = const.

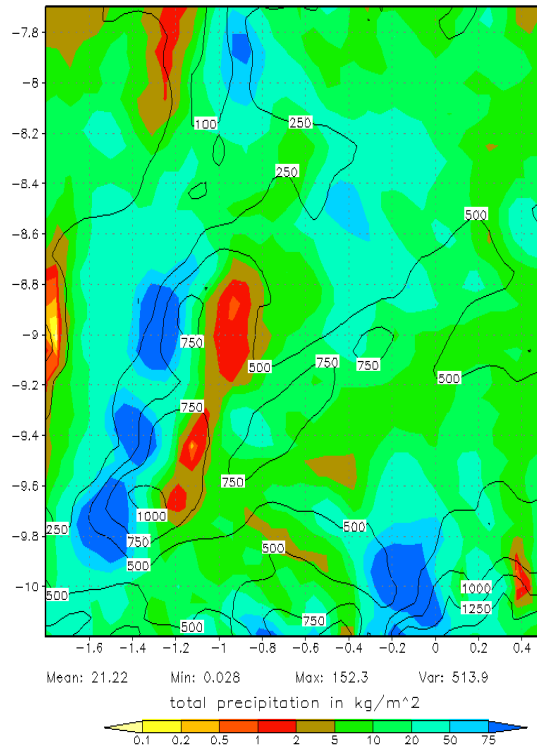


Test case: 20.02.2002 +06-30 h

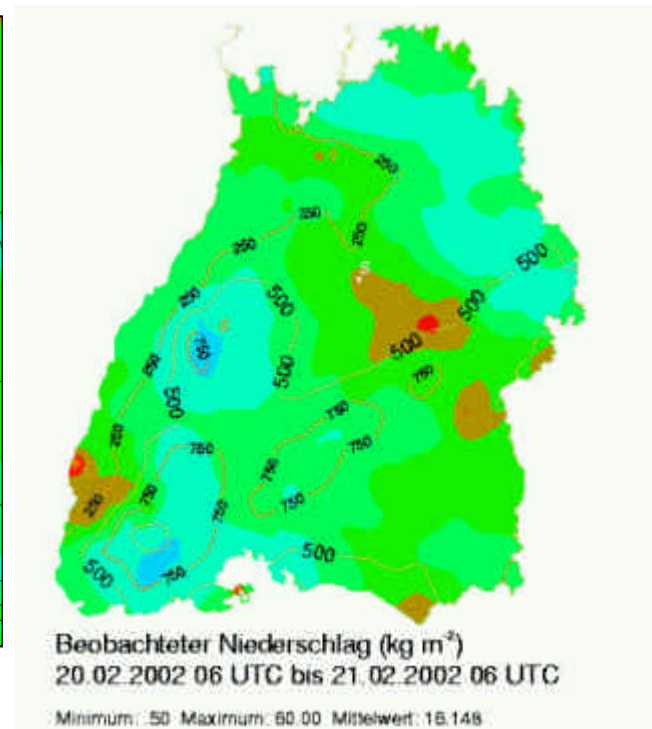
total precipitation in 24 h

LM with diagnostic precip.

20.02.2002 +6-30 h, LM_3TL

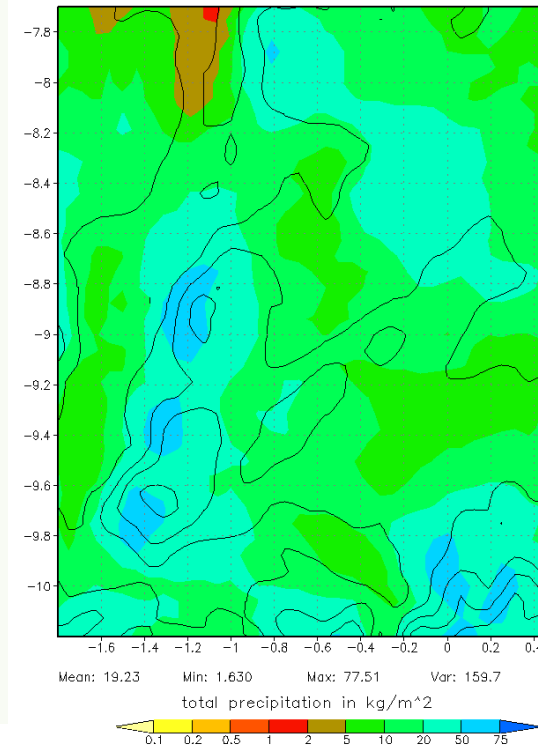


observations



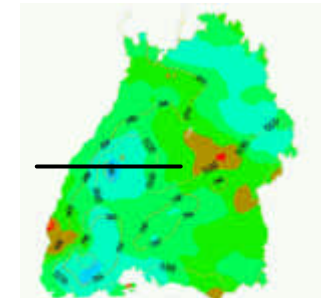
LM with progn. precip.

20.02.2002 +6-30 h, LF_SL, prec



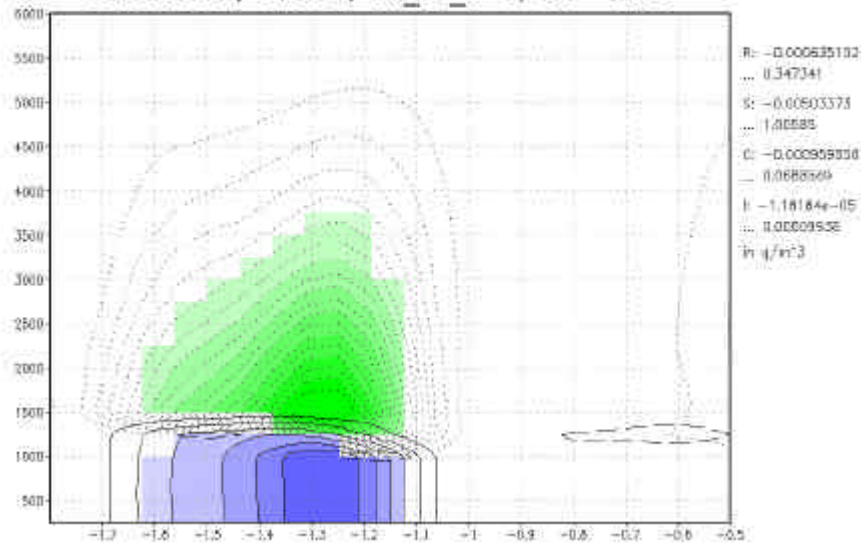
Test case: 20.02.2002

vertical cut (t=16:00)



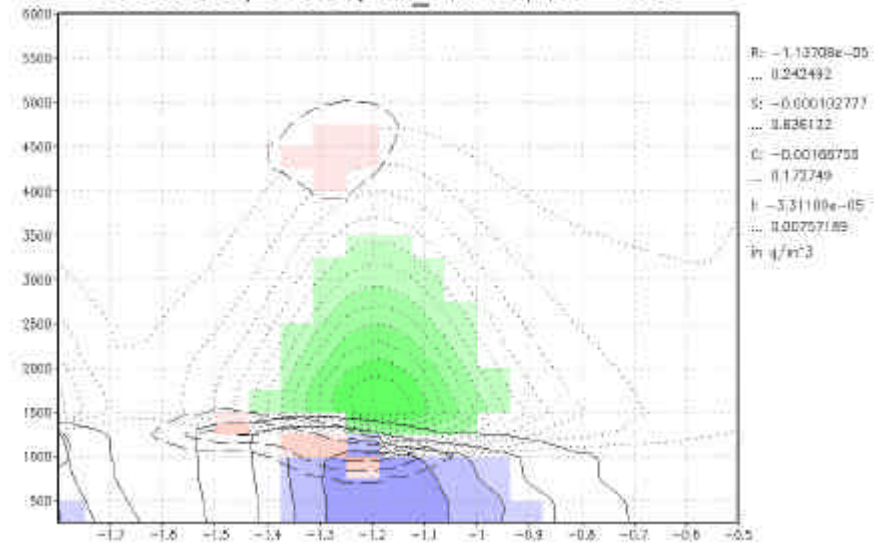
Prognostic precip. with $v=0$

20.02.2002, 016:00, LM_SL_v=0, lat=-8.93'



Prognostic precip.

20.02.2002, 016:00, LM_3TL+SL, lat=-8.93'



ρ_c

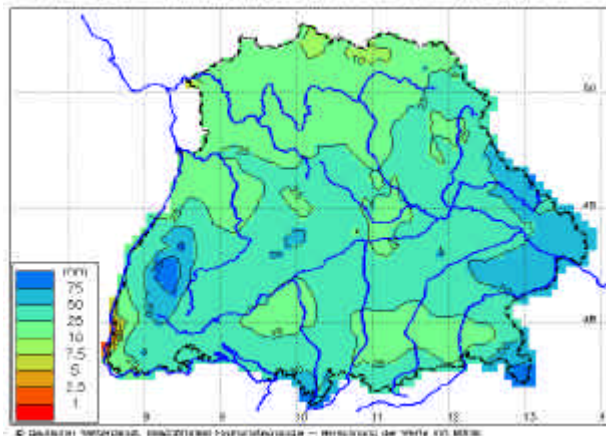
ρ_r

ρ_s

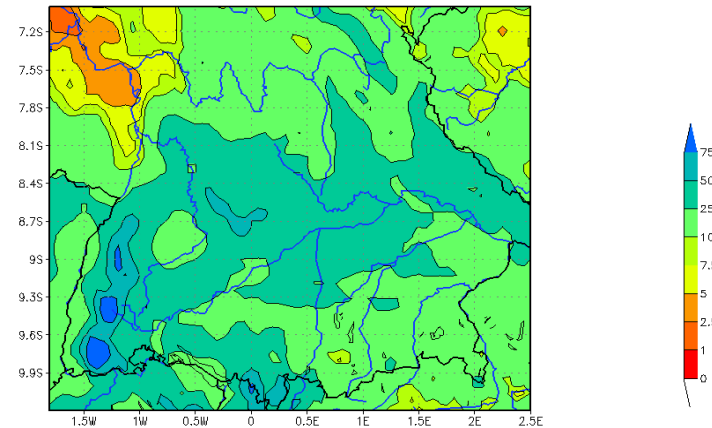
Numeric experiment:
day 13.01.2004 +06-30 h

BONIE-Analysis

Niederschlagshöhen vom 13.01.2004, 6 Uhr UTC bis zum 14.01.2004, 6 Uhr UTC

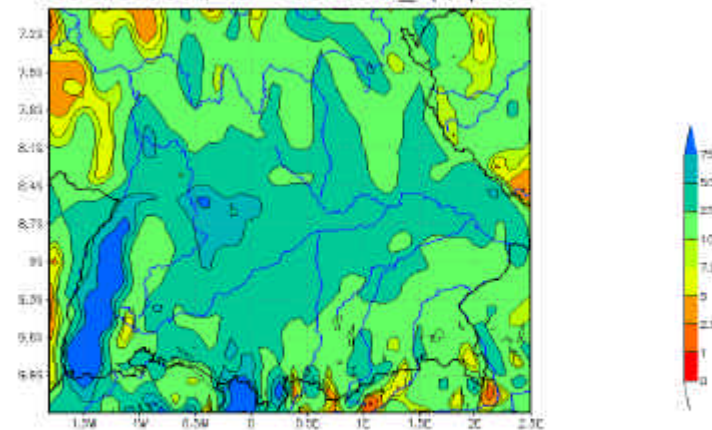


2004011300, +6-30 h, LF_SL_106, prec



Mean: 22.97 Min: 1.226 Max: 123.0 Var: 171.8
total precipitation in kg/m²

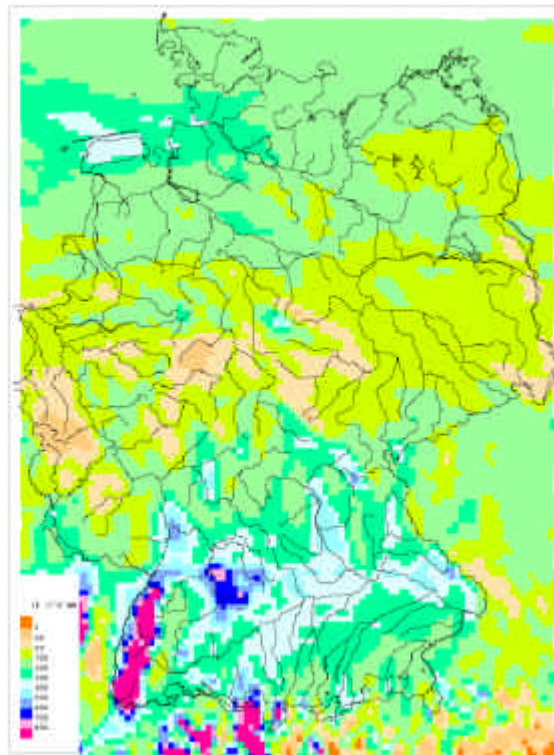
2004011300, +6-30 h, LM_op, prec



Mean: 26.47 Min: 0.486 Max: 182.5 Var: 415.0
total precipitation in kg/m²

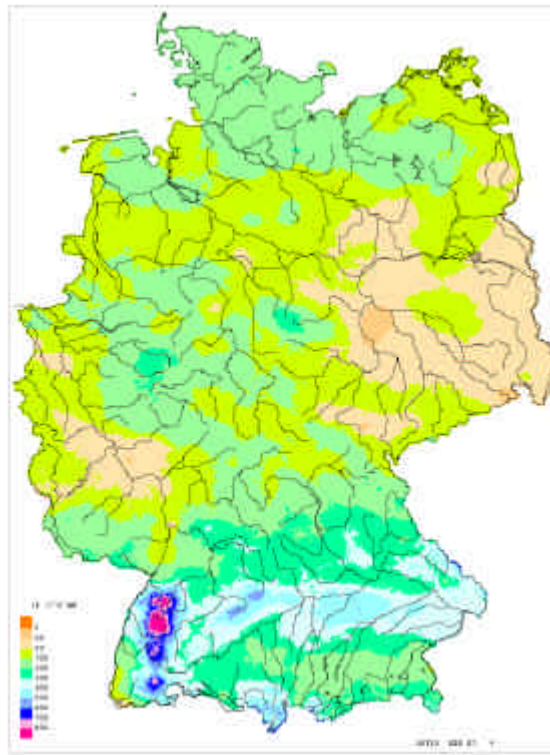
Numeric experiment:
day 13.01.2004 +06-30 h

LM with diagnostic precipitation



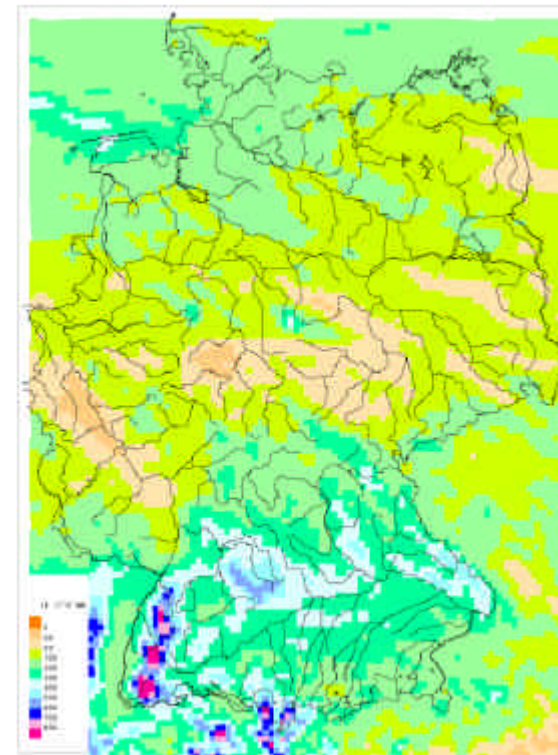
LM_13.01.2004_06UTC bis 06 UTC_FT

REGNIE-Analysis



24...STD...NO...HOERE...GEMESSEN AM 14.01.2004 06UTC

with prognostic precipitation

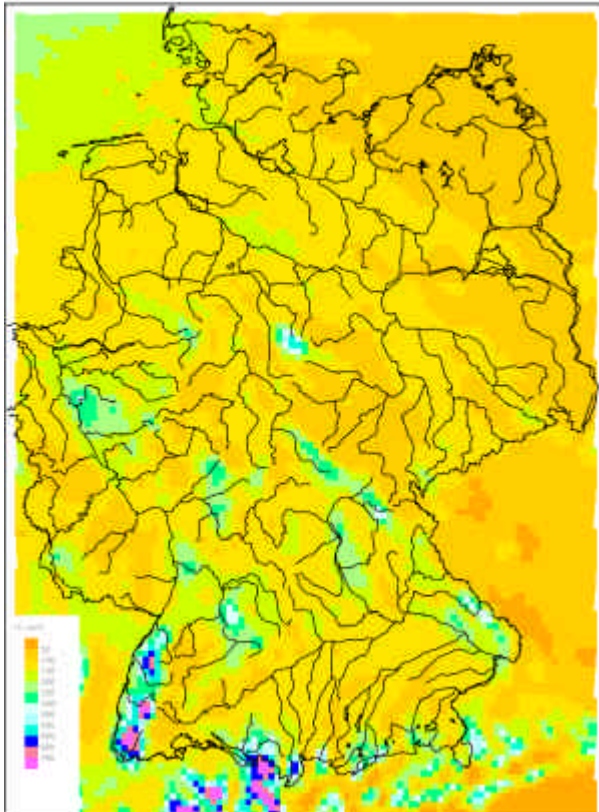


LF_SU_13.01.2004_06 UTC bis 06 UTC_FT

24 h - mean values of precipitation for 06.-31.Jan 2004

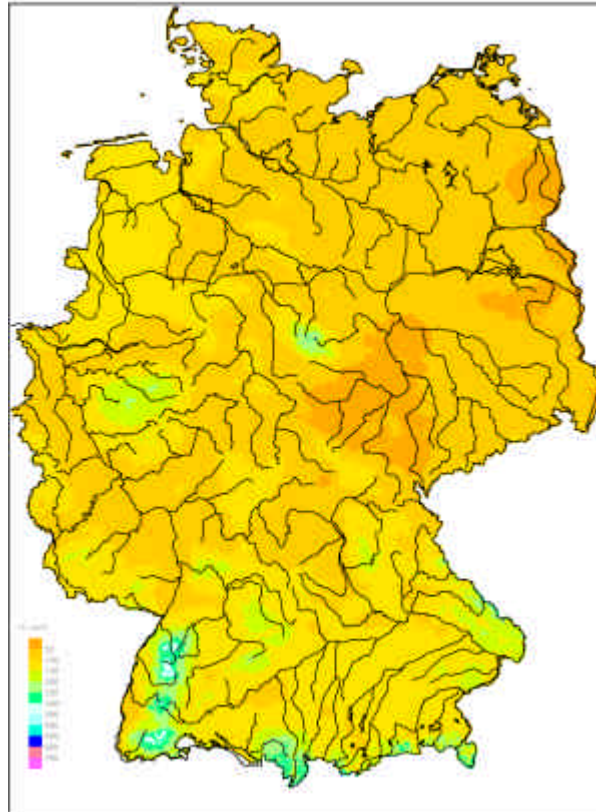
LM 3.5 with diagn. precip.

LM-Routine Vorhers. 06-30.01.04, vom 06. bis 31.01.2004



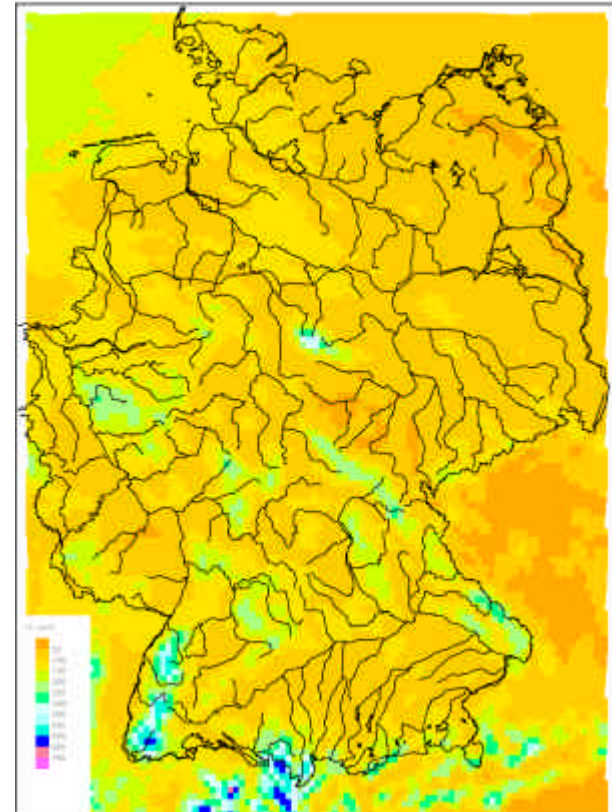
Beobachtungen (REGNIE)

gem. Nied. (Synop und QRR50) vom 06. bis 31.01.2004

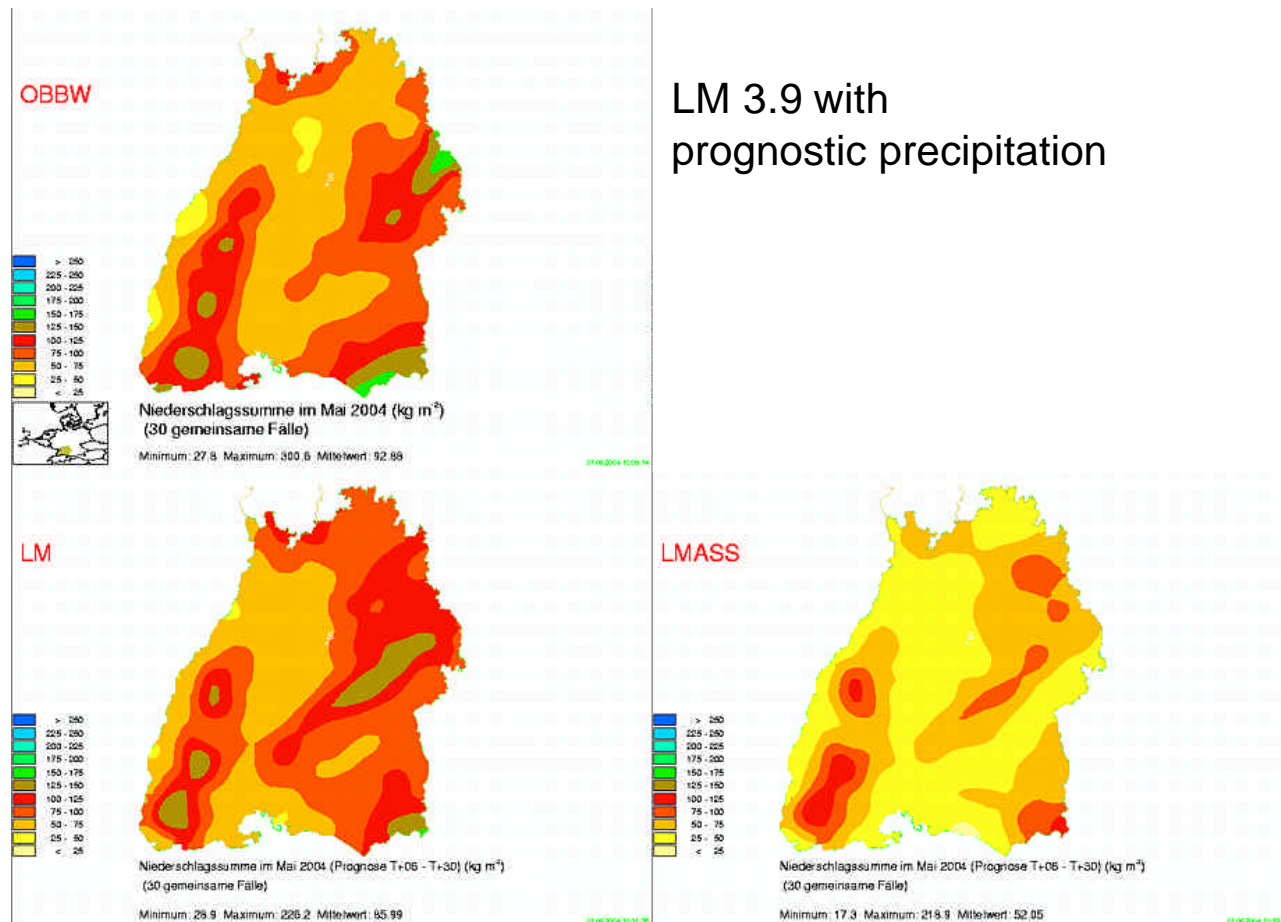


LM 3.9 with progn. precip.

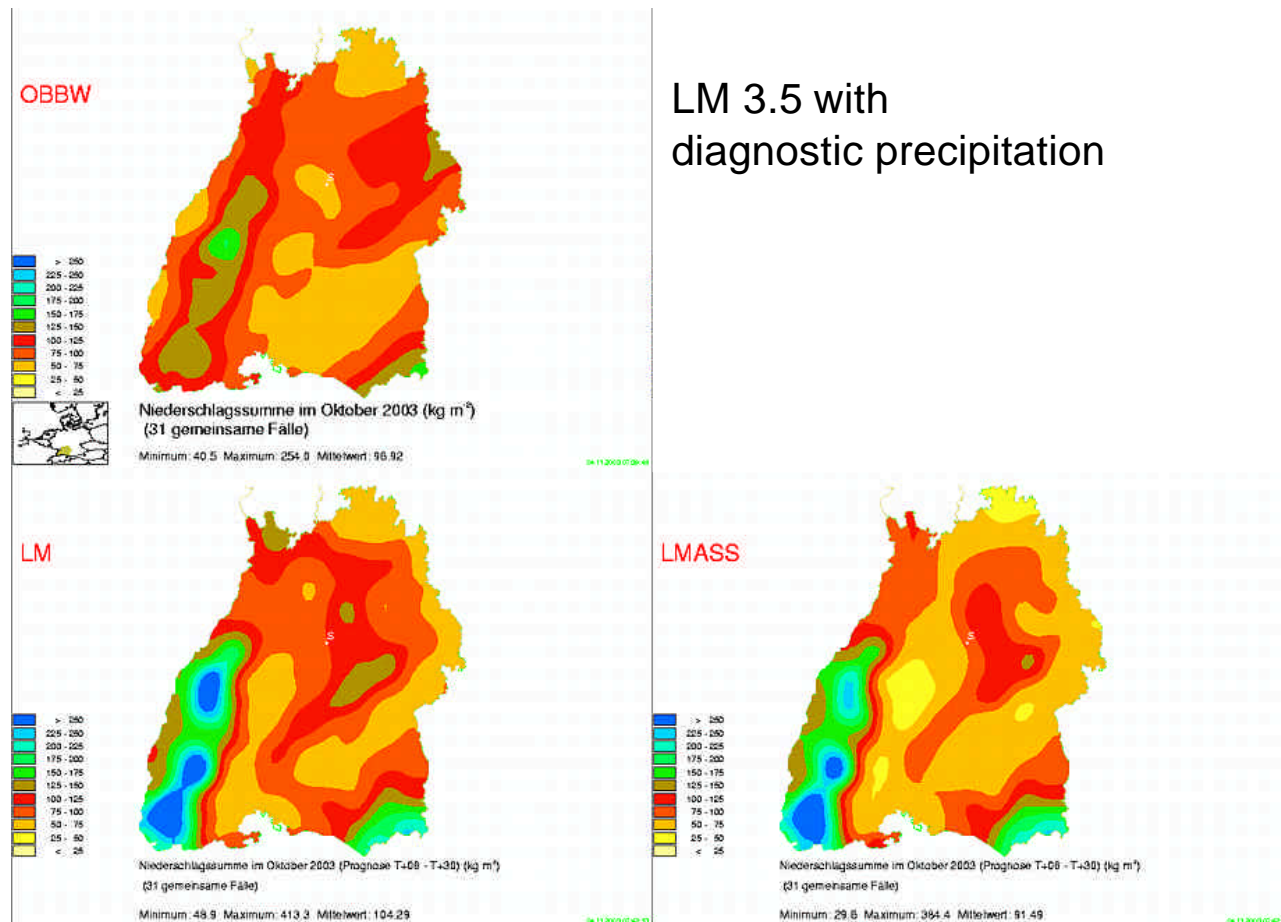
LM-Exp.107 Vorhers. 06-30.01.04, vom 06. bis 31.01.2004



Monthly precipitation sum over Baden-Württemberg (SW Germany) in Mai 2004



Monthly precipitation sum over Baden-Württemberg (SW Germany) in October 2003



Results

from the actual numeric experiment
(analysis over South-Germany in 06.01.-08.02.2004)

compared to the LM 3.5:

- Windward-Lee-distribution improved in most cases
- spatial averaged precipitation is reduced by about 15-25%
- precipitation maxima are reduced by about 20-40%
- computation time increased by about 20%



Verification

BONIE (Bodenniederschlag)

- learning strategy derived from theory of artificial intelligence
- derivation of statistical properties of the spatial distribution patterns
- interpolation in analogy to Kriging-method

data base:

- measurements at the stations of DWD and AWGeophysBDBw
- additional about 100 ombrometer measurements in Baden-Württemberg

DWD, Geschäftsbereich VB/HM, Dr. T. Reich

Homepage: <http://inet1.dwd.de/vb/hm/BONIE/index.htm>

REGNIE (Regionalisierung räumlicher Niederschlagsverteilungen)

- use of regionalised, monthly averaged precipitation values (1961-1990)
- distance dependent interpolation (background field-method)

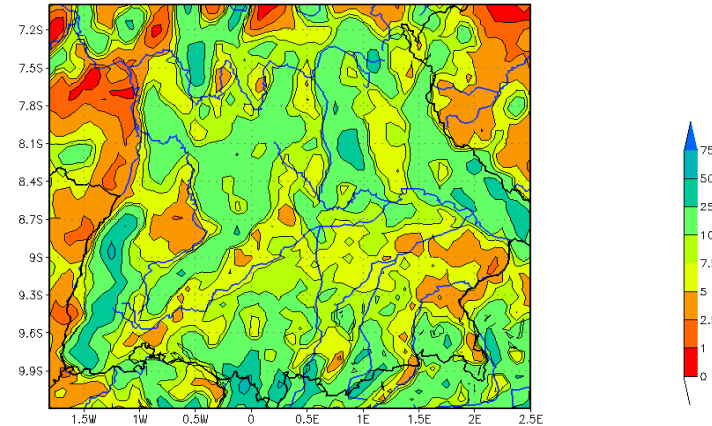
data base:

- about 600 stations in Germany

DWD, Geschäftsbereich VB/HM 1, Dr. B. Dietzer

Numeric experiment:
day 08.02.2004 +06-30 h

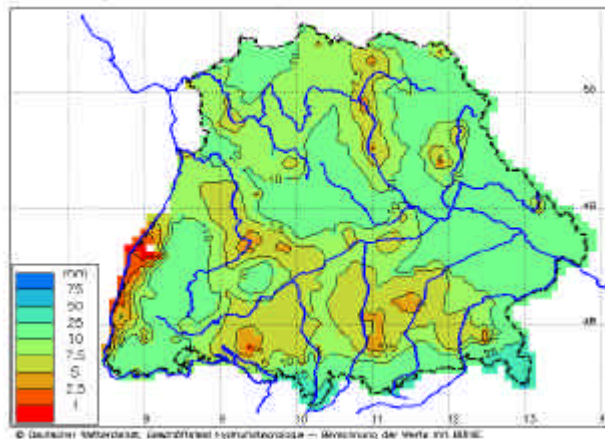
2004020800, +6-30 h, LF_SL_106, prec



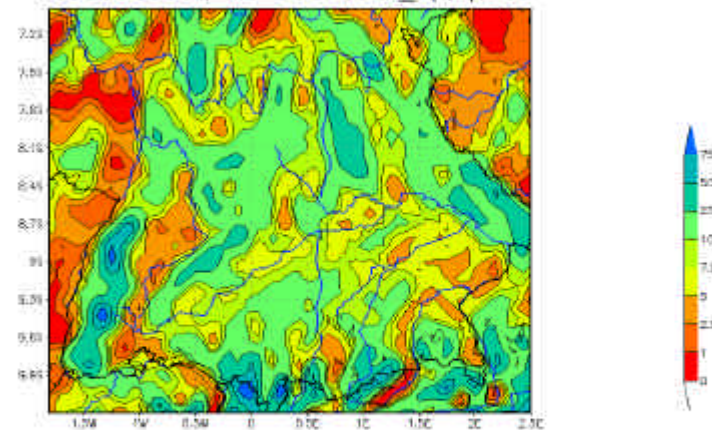
Mean: 10.50 Min: 0.251 Max: 59.81 Var: 65.43
total precipitation in kg/m²

BONIE-Analysis

Niederschlagsintensitäten vom 8.02.2004, 6 Uhr UTC bis zum 09.02.2004, 6 Uhr UTC



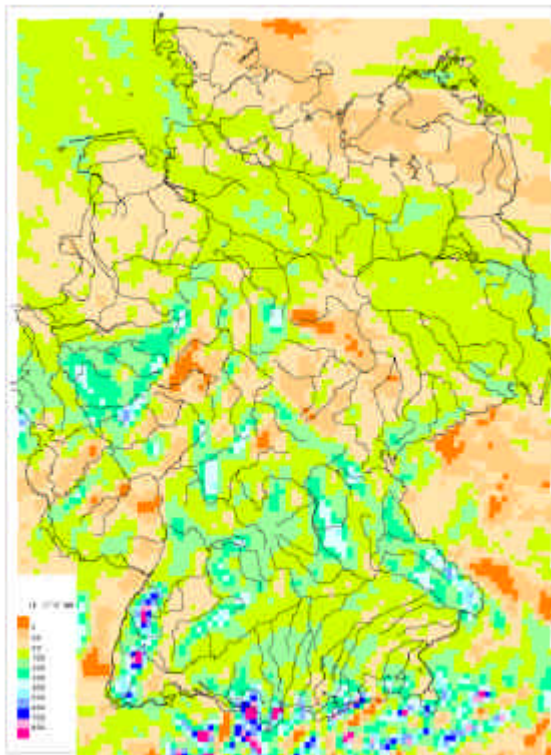
2004020800, +6-30 h, LM_op, prec



Mean: 12.53 Min: 0 Max: 113.2 Var: 154.6
total precipitation in kg/m²

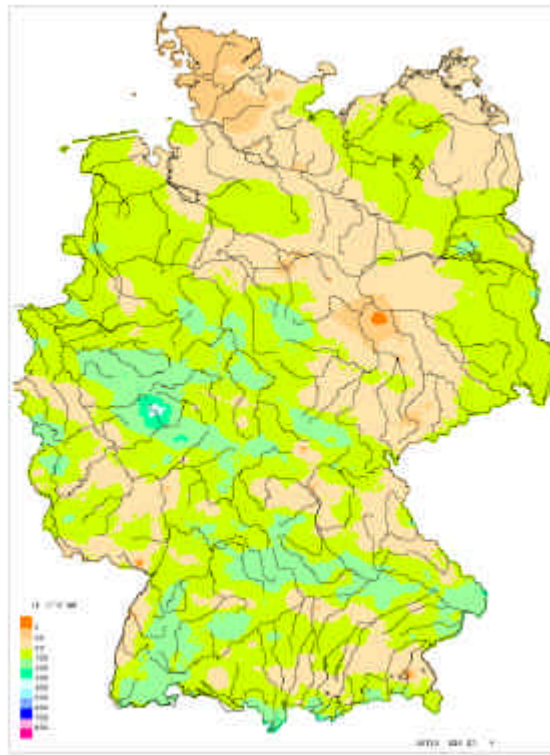
Numeric experiment:
day 08.02.2004 +06-30 h

LM 3.5 with diagnostic precipitation



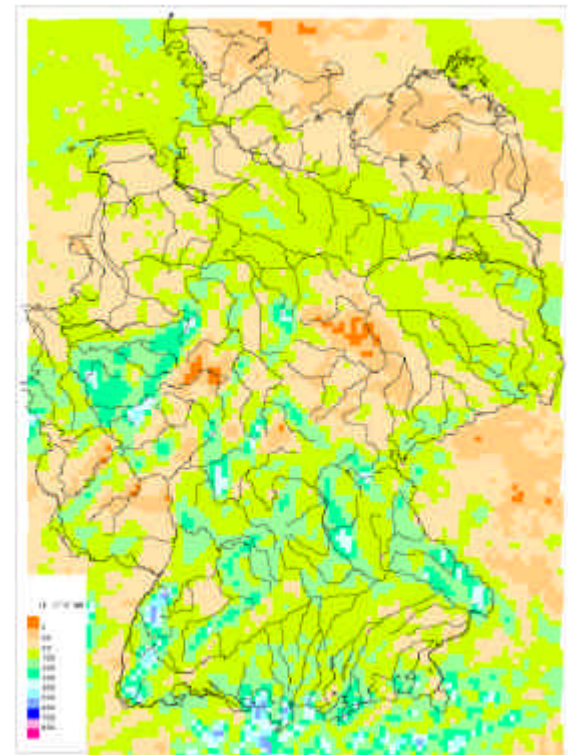
LM_08.02.2004_00UTC_06UTC_bis_06_UTC_FT

REGNIE-Analyse



24...STD...NO...HOEHE...GEMESSEN AM 08.02.2004 06UTC

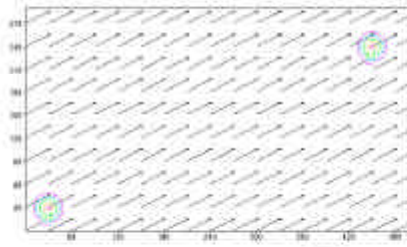
LM 3.9 with prognostic precipitation



LF_5L_08.02.2004_06_UTC_bis_06_UTC_FT

Advection tests

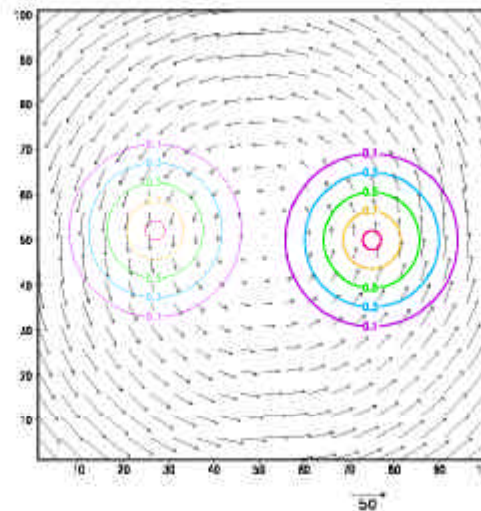
‘constant v’



Courant numbers

$$C_x = 0.4, C_y = 0.2$$

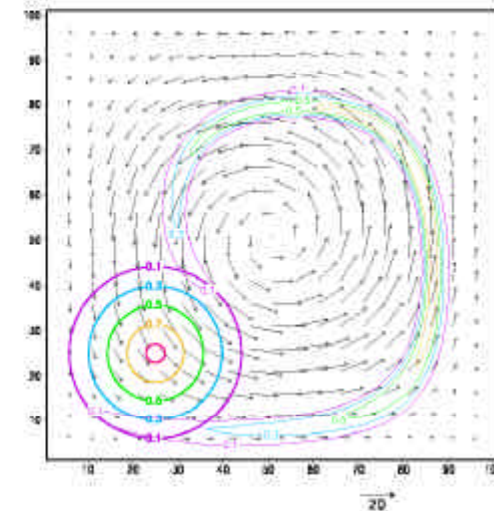
‘solid body rotation’



Courant numbers

$$C_{cone} = 0.4, C_{max} = 0.8$$

‘LeVeque (1996)’

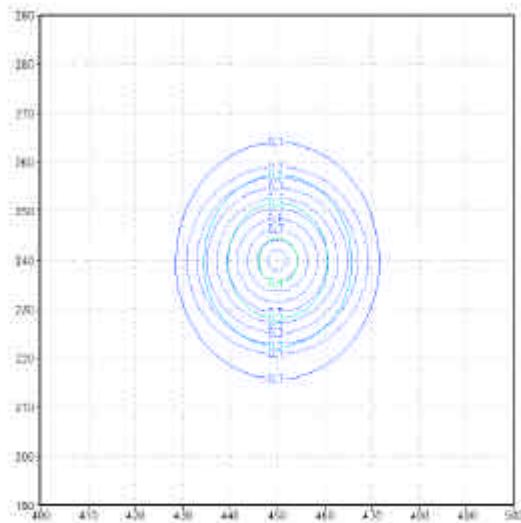


Courant numbers

$$C = 0 \dots 0.4$$

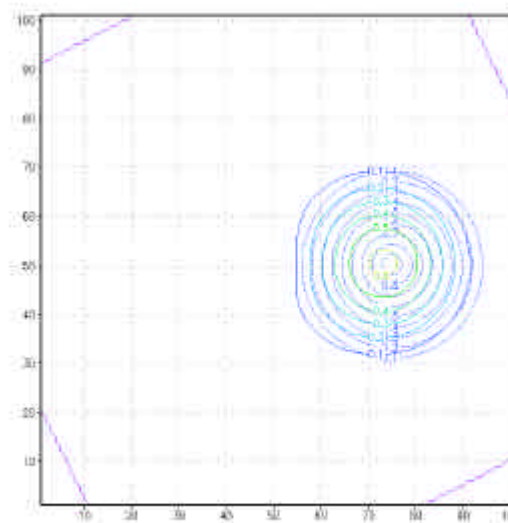
Semi-Lagrange-advection, backtrajectory $O(\Delta t)$, bilinear interpolation

„constant v“



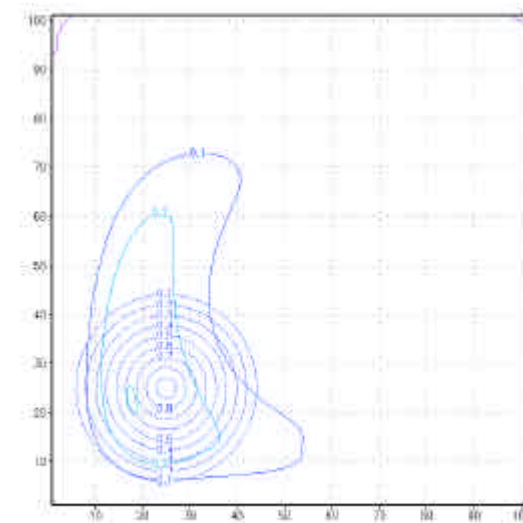
Min. = 0.0
Max. = 0.4204
rel. cons. = -0.000079

„solid body rotation“



Min. = 0.0
Max. = 0.62
rel. cons. = -0.18

„LeVeque“

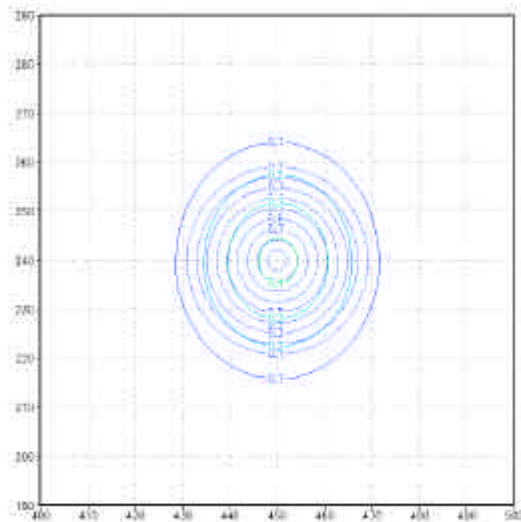


Min. = 0.0
Max. = 0.3018
rel. cons. = -0.0027

computer time relative to upwind 1. order = 2.5

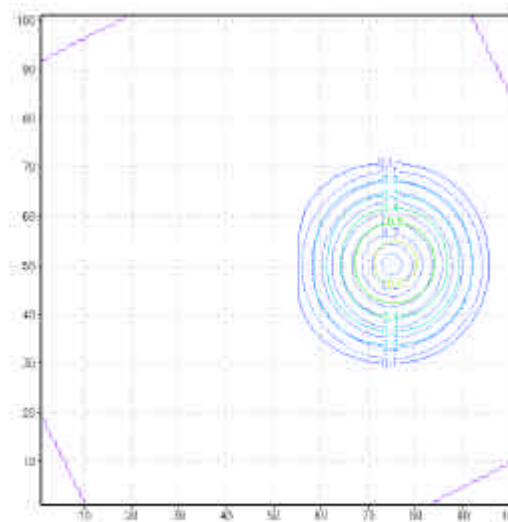
Semi-Lagrange-advection, backtrajectory $O(Dt^2)$, bilinear interpolation

‚constant v‘



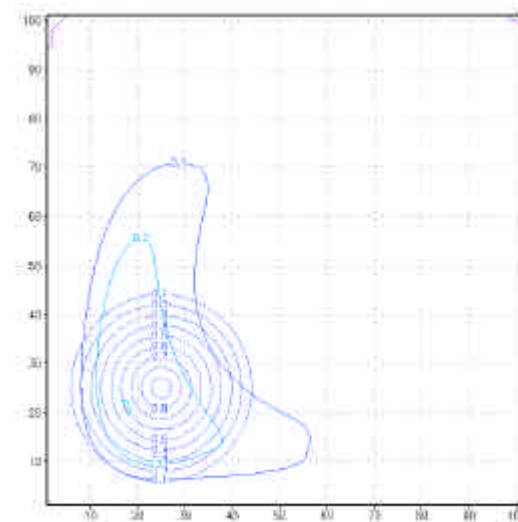
Min. = 0.0
Max. = 0.4204
rel. cons. = -0.000079

‚solid body rotation‘



Min. = 0.0
Max. = 0.6437
rel. cons. = -0.0049

‚LeVeque‘

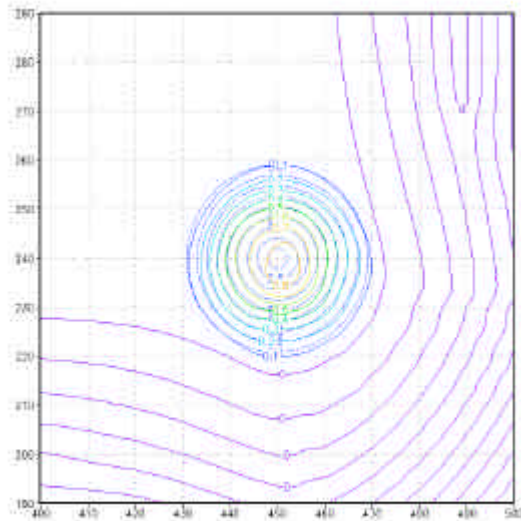


Min. = 0.0
Max. = 0.301
rel. cons. = -0.059

computer time relative to upwind 1. order = 3.75

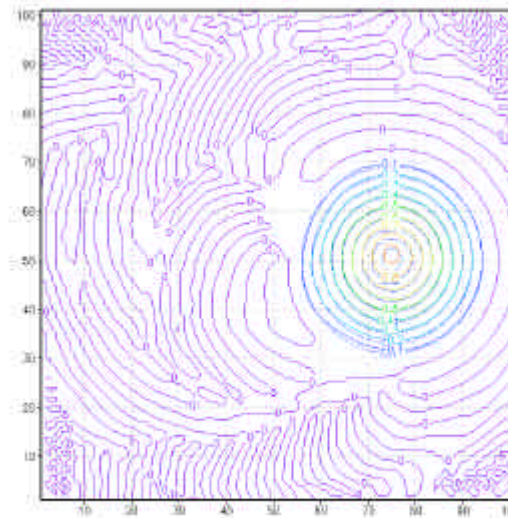
Semi-Lagrange-advection, backtrajectory $O(\Delta t^2)$, biquadratic interpolation

„constant v“



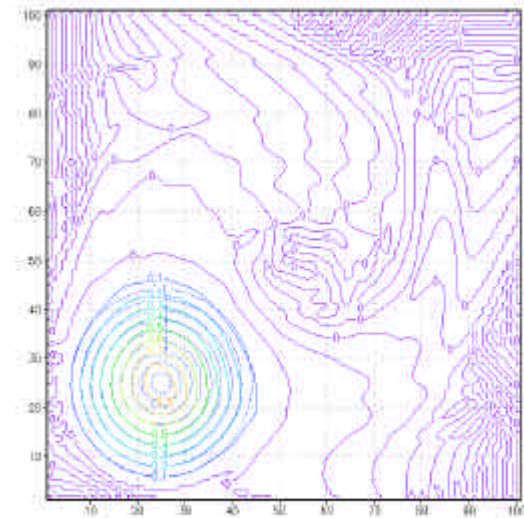
Min. = -0.053
Max. = 0.875
rel. cons. = -0.000061

„solid body rotation“



Min. = -0.026
Max. = 0.9263
rel. cons. = -0.00020

„LeVeque“



Min. = -0.0263
Max. = 0.8652
rel. cons. = 0.000019

computer time relative to upwind 1. order = 5.3